

# Searching for the Equity Premium

Hang Bai\*  
University of Connecticut

Lu Zhang<sup>†</sup>  
Ohio State and NBER

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## Abstract

Labor market frictions are crucial for the equity premium in production economies. A dynamic stochastic general equilibrium model with recursive utility, search frictions, and capital accumulation yields a high equity premium of 4.26% per annum, a stock market volatility of 11.8%, and a low average interest rate of 1.59%, while simultaneously retaining plausible business cycle dynamics. The equity premium and stock market volatility are strongly countercyclical, while the interest rate and consumption growth are largely unpredictable. Because of wage inertia, dividends are procyclical despite consumption smoothing via capital investment. The welfare cost of business cycles is huge, 29%.

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\*School of Business, University of Connecticut, 2100 Hillside Road, Unit 1041F, Storrs, CT 06269. Tel: (510) 725-8868. E-mail: hang.bai@uconn.edu.

<sup>†</sup>Fisher College of Business, The Ohio State University, 760A Fisher Hall, 2100 Neil Avenue, Columbus OH 43210; and NBER. Tel: (614) 292-8644. E-mail: zhanglu@fisher.osu.edu.

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# 1 Introduction

Mehra and Prescott (1985) show that the equity premium (the average difference between the stock market return and risk-free interest rate) in the Arrow-Debreu economy is negligible relative to its historical average. Subsequent studies have largely succeeded in specifying preferences and cash flow dynamics to explain the equity premium in endowment economies (Campbell and Cochrane 1999; Bansal and Yaron 2004; Barro 2006). Unfortunately, explaining the equity premium in general equilibrium production economies, in which cash flows are endogenously determined, has proven more challenging.<sup>1</sup> To date, no consensus general equilibrium framework has emerged. Consequently, finance and macroeconomics have largely developed in a dichotomic fashion. Finance specifies “exotic” preferences and exogenous cash flow dynamics to match asset prices but ignore firms, whereas macroeconomics analyzes full-fledged general equilibrium production economies but ignore asset prices with simple preferences (Christiano, Eichenbaum, and Evans 2005; Smets and Wouters 2007).

This macro-finance dichotomy has left many important questions unanswered. What are the microeconomic foundations underlying the exogenously specified, often complicated cash flow dynamics in finance models (Bansal, Kiku, and Yaron 2012; Nakamura, Steinsson, Barro, and Ursua 2013)? What are the essential ingredients in the production side that can endogenize the key elements of cash flow dynamics necessary to explain the equity premium? To what extent do time-varying risk premiums matter quantitatively for macroeconomic dynamics? How large is the welfare cost of business cycles in an equilibrium production economy that replicates the equity premium?

Our long-term objective is to formulate a unified equilibrium theory that explains the equity

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<sup>1</sup>Rouwenhorst (1995) shows that the standard real business cycle model cannot explain the equity premium because optimal investment of firms provides a powerful mechanism for the representative household to smooth consumption, yielding little consumption risks. With internal habit preferences, Jermann (1998) and Boldrin, Christiano, and Fisher (2001) adopt capital adjustment costs and cross-sector immobility, respectively, to restrict consumption smoothing to match the equity premium. However, both models struggle with excessively high interest rate volatilities because of low elasticities of intertemporal substitution. Using recursive utility, Tallarini (2000) shows that increasing risk aversion in a real business cycle model improves its fit with the market Sharpe ratio but does not materially affect macro quantities. However, the model fails to match the equity premium and its volatility. Kaltenbrunner and Lochstoer (2010) show that long-run consumption risks arise endogenously from consumption smoothing in a real business cycle model, but the model falls short in explaining the equity premium and stock market volatility.

premium puzzle, while simultaneously retaining plausible business cycle dynamics. We embed the standard Diamond-Mortensen-Pissarides search model of equilibrium unemployment into a dynamic stochastic general equilibrium framework with recursive utility and capital accumulation. When calibrated to the consumption growth volatility in the Jordà-Schularick-Taylor macrohistory database, the model succeeds in yielding an equity premium (adjusted for financial leverage) of 4.26% per annum, which is close to 4.36% in the historical data. The average interest rate is 1.59%, which is not far from 0.82% in the data (the difference is insignificant). However, the stock market volatility is 11.8% in the model, which, although sizeable, is still significantly lower than 16% in the data. Also, the model implies strong time series predictability for stock market excess returns and volatilities, some predictability for consumption volatility, and weak to no predictability for consumption growth and the real interest rate. Quantitatively, the model explains stock market predictability but somewhat overstates consumption growth predictability in the historical data.

Wage inertia plays a key role in our model. To keep the model parsimonious, we work with the Nash wage that features a low bargaining weight of workers and a high flow value of unemployment. This calibration implies a wage elasticity to labor productivity of 0.256 in the model. Hagedorn and Manovskii (2008) estimate this elasticity to be 0.449 in the U.S. postwar 1951–2004 sample. Drawing from historical sources (Kendrick 1961; Officer 2009), we extend the Hagedorn-Manovskii evidence and estimate the wage elasticity to be 0.267 in the historical 1890–2015 sample.

Unlike endowment economies, in which cash flows can be exogenously specified to fit the equity premium, the main challenge facing general equilibrium production economies is that cash flows are often endogenously countercyclical. With frictionless labor market, wages equal the marginal product of labor, which is almost as procyclical as output and profits (output minus wages). Alas, investment is more procyclical than output because of consumption smoothing, making dividends (profits minus investment) countercyclical (Kaltenbrunner and Lochstoer 2010). With wage inertia, profits are more procyclical than output. The magnified procyclicality of profits is sufficient to overcome the procyclicality of investment (and vacancy costs) to render dividends procyclical. In

addition, wage inertia is stronger in bad times, with smaller profits. This time-varying wage inertia amplifies risks and risk premiums in bad times, giving rise to time series predictability of the equity premium and stock market volatility. Finally, despite adjustment costs, investment still absorbs a large amount of shocks, making consumption growth and the interest rate largely unpredictable.

Risk aversion strongly affects quantity dynamics, in contrast to Tallarini (2000). In comparative statics, reducing risk aversion from 10 to 5 lowers the equity premium to 0.54% per annum. More important, consumption volatility falls from 5.13% to 3.93%, and consumption disaster probability from 5.83% to 3.82%. A lower discount rate raises the marginal benefit of hiring and reduces the unemployment rate from 8.63% to 4.63%. Echoing Hall's (2017) partial equilibrium analysis, our general equilibrium results indicate that it is imperative to study quantity and price dynamics jointly.

Our model predicts downward-sloping term structures of the equity premium and equity volatility, consistent with Binsbergen, Brandt, and Koijen (2012). Intuitively, when the search economy slides into a disaster, short-maturity dividend strips take a big hit because of inertial wages. In contrast, long-maturity strips are less impacted because disasters are followed by subsequent recoveries. Also, despite recursive utility calibrated to feature the early resolution of uncertainty, the timing premium (the fraction of the consumption stream that the investor is willing to trade for the early resolution) is only 15.3% in our model. Intuitively, the expected consumption growth and conditional consumption volatility in our search economy are much less persistent than those typically calibrated in the long-run risks model, thereby avoiding its pitfall of implausibly high timing premiums.

Finally, the average welfare cost of business cycles is huge, 28.7%, which is more than 550 times of 0.05% in Lucas (2003). More important, the welfare cost is countercyclical with a long, right tail. In simulations, its 5th percentile of 18.2% is not far below its median of 24.6%, but its 95th percentile is substantially higher, 54.9%. As such, countercyclical policies aimed to dampen disaster risks are even more important than what the average welfare cost estimate of 28.7% would suggest.

We view this work as a solid progress report toward a unified theory of asset prices and business

cycles. This holy grail of macro-finance has proven elusive for decades. Petrosky-Nadeau, Zhang, and Kuehn (2018) show that the standard search model exhibits disaster dynamics. However, their asset pricing results are very limited because of no capital. Capital is particularly important for asset prices because it represents the core challenge of endogenizing procyclical dividends in production economies (Jermann 1998). We embed capital and recursive utility simultaneously to study asset prices with production, while overcoming ensuing heavy computational burden. Bai (2020) incorporates defaultable bonds to study the credit spread. We instead focus on the equity premium puzzle.

Embedding rare disasters per Rietz (1988) and Barro (2006) into a real business cycle model, Gourio (2012) shows that aggregate risks significantly affect quantity dynamics. Echoing Gourio, we show that Tallarini’s (2000) separation between prices and quantities does not hold under more general settings. However, we differ from Gourio in that disasters arise endogenously from labor market frictions. We also endogenize operating leverage via wage inertia to explain the equity premium and stock market volatility. In contrast, Gourio relies on exogenous leverage to generate volatile cash flows but “does not address the volatility of the unlevered return on capital (p. 2737).” Kilic and Wachter (2018) embed the exogenous Rietz-Barro disasters into the search model of unemployment to yield a high unemployment volatility and examine its relation with a high stock market volatility. While our work differs from Kilic and Wachter’s in many details, the most important distinction is, again, the endogenous nature of disasters in our setting.<sup>2</sup>

The rest of the paper is organized as follows. Section 2 constructs the general equilibrium model. Section 3 presents the model’s key quantitative results, including the equity premium, stock market volatility, and their predictability. Section 4 examines several additional implications of the model, including the welfare cost of business cycles. Section 5 concludes. Appendix A describes

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<sup>2</sup>Several recent studies have examined the equity premium in general equilibrium production economies but outside the disasters framework. Croce (2014) embeds exogenous long-run productivity risks into a production model. While long-run risks increase the equity premium, the return volatility is only about one quarter of that in the data. Kung and Schmid (2015) endogenize long-run productivity risks via firms’ research and development in an endogenous growth model. Favilukis and Lin (2016) examine the impact of infrequent wage renegotiations in a stochastic growth model with long-run productivity risks. Finally, Chen (2017) examines a general equilibrium production model with external habit and emphasizes the role of endogenous consumption volatility risks.

our algorithm. A separate Internet Appendix details data, derivations, and supplementary results.

## 2 A General Equilibrium Production Economy

The economy is populated by a representative household and a representative firm. Following Merz (1995), we assume that the household has perfect consumption insurance. A continuum of mass one of members is either employed or unemployed at any point in time. The fractions of employed and unemployed workers are representative of the population at large. The household pools the income of all the members together before choosing per capita consumption.

The household maximizes recursive utility, denoted  $J_t$ , given by:

$$J_t = \left[ (1 - \beta)C_t^{1-\frac{1}{\psi}} + \beta \left( E_t \left[ J_{t+1}^{1-\gamma} \right] \right)^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}}, \quad (1)$$

in which  $C_t$  is consumption,  $\beta$  time preference,  $\psi$  the elasticity of intertemporal substitution, and  $\gamma$  relative risk aversion (Epstein and Zin 1989; Weil 1990). The consumption Euler equation is:

$$1 = E_t[M_{t+1}r_{St+1}], \quad (2)$$

in which  $r_{St+1}$  is the firm's stock return, and  $M_{t+1}$  the household's stochastic discount factor:

$$M_{t+1} \equiv \beta \left( \frac{C_{t+1}}{C_t} \right)^{-\frac{1}{\psi}} \left( \frac{J_{t+1}}{E_t \left[ J_{t+1}^{1-\gamma} \right]^{\frac{1}{1-\gamma}}} \right)^{\frac{1}{\psi}-\gamma}. \quad (3)$$

The riskfree rate is  $r_{ft+1} = 1/E_t[M_{t+1}]$ , which is known at the beginning of  $t$ .

The representative firm uses capital,  $K_t$ , and labor,  $N_t$ , to product output,  $Y_t$ , with a constant elasticity of substitution (CES) production technology (Arrow et al. 1961):

$$Y_t = X_t \left[ \alpha \left( \frac{K_t}{K_0} \right)^\omega + (1 - \alpha)N_t^\omega \right]^{\frac{1}{\omega}}, \quad (4)$$

in which  $\alpha$  is the distribution parameter, and  $e \equiv 1/(1 - \omega)$  the elasticity of substitution between capital and labor. When  $\omega$  approaches zero in the limit, equation (4) reduces to the special case of

the Cobb-Douglas production function with a unitary elasticity. To facilitate the model’s calibration, we work with the “normalized” CES function in equation (4), in which  $K_0 > 0$  is a scalar that makes the unit of  $K_t/K_0$  comparable to the unit of  $N_t$  (Klump and La Grandville 2000). Specifically, we calibrate  $K_0$  to ensure that  $1 - \alpha$  matches the average labor share in the data (Section 3.2). Doing so eliminates the distribution parameter,  $\alpha$ , as a free parameter.<sup>3</sup> Finally, the CES production function is of constant returns to scale,  $Y_t = K_t \partial Y_t / \partial K_t + N_t \partial Y_t / \partial N_t$  (the Internet Appendix).

The firm takes the aggregate productivity,  $X_t$ , as given, with  $x_t \equiv \log(X_t)$  governed by:

$$x_{t+1} = (1 - \rho_x)\bar{x} + \rho_x x_t + \sigma_x \epsilon_{t+1}, \quad (5)$$

in which  $\bar{x}$  is unconditional mean,  $0 < \rho_x < 1$  persistence,  $\sigma_x > 0$  conditional volatility, and  $\epsilon_{t+1}$  an independently and identically distributed (i.i.d.) standard normal shock. We scale  $\bar{x}$  to make the average marginal product of labor around one in simulations to ease the interpretation of parameters.

The representative firm posts a number of job vacancies,  $V_t$ , to attract unemployed workers,  $U_t$ . Vacancies are filled via the Den Haan-Ramey-Watson (2000) matching function:

$$G(U_t, V_t) = \frac{U_t V_t}{(U_t^\iota + V_t^\iota)^{1/\iota}}, \quad (6)$$

in which  $\iota > 0$ . This matching function has the desirable property that matching probabilities fall between zero and one. In particular, define  $\theta_t \equiv V_t/U_t$  as the vacancy-unemployment ( $V/U$ ) ratio. The probability for an unemployed worker to find a job per unit of time (the job finding rate) is  $f(\theta_t) \equiv G(U_t, V_t)/U_t = (1 + \theta_t^{-\iota})^{-1/\iota}$ . The probability for a vacancy to be filled per unit of time (the vacancy filling rate) is  $q(\theta_t) \equiv G(U_t, V_t)/V_t = (1 + \theta_t^\iota)^{-1/\iota}$ . It follows that  $f(\theta_t) = \theta_t q(\theta_t)$  and  $q'(\theta_t) < 0$ . An increase in the scarcity of unemployed workers relative to vacancies makes it harder to fill a vacancy. As such,  $\theta_t$  is labor market tightness, and  $1/q(\theta_t)$  the average duration of vacancies.

The representative firm incurs costs in posting vacancies. The unit cost per vacancy is given by

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<sup>3</sup>In contrast, in prior applications of the CES production function in asset pricing, the distribution parameter,  $\alpha$ , is largely treated as a free parameter (Favilukis and Lin 2016; Kilic and Wachter 2018; Bai 2020).

$\kappa > 0$ . The marginal cost of hiring,  $\kappa/q(\theta_t)$ , increases with the mean duration of vacancies,  $1/q(\theta_t)$ . In expansions, the labor market is tighter for the firm ( $\theta_t$  is higher), and the vacancy filling rate,  $q(\theta_t)$ , is lower. As such, the marginal cost of hiring is procyclical.

Jobs are destroyed at a constant rate of  $s$  per period. Employment,  $N_t$ , evolves as:

$$N_{t+1} = (1 - s)N_t + q(\theta_t)V_t, \quad (7)$$

in which  $q(\theta_t)V_t$  is the number of new hires. Population is normalized to be one,  $U_t + N_t = 1$ , meaning that  $N_t$  and  $U_t$  are also the rates of employment and unemployment, respectively.

The firm incurs adjustment costs when investing. Capital accumulates as:

$$K_{t+1} = (1 - \delta)K_t + \Phi(I_t, K_t), \quad (8)$$

in which  $\delta$  is the capital depreciation rate,  $I_t$  is investment, and

$$\Phi_t \equiv \Phi(I_t, K_t) = \left[ a_1 + \frac{a_2}{1 - 1/\nu} \left( \frac{I_t}{K_t} \right)^{1-1/\nu} \right] K_t, \quad (9)$$

is the installation function with the supply elasticity of capital  $\nu > 0$ . We set  $a_1 = \delta/(1 - \nu)$  and  $a_2 = \delta^{1/\nu}$  to ensure no adjustment costs in the deterministic steady state (Jermann 1998). This parsimonious parametrization involves only one free parameter,  $\nu$ .

The dividends to the firm's shareholders are given by:

$$D_t = Y_t - W_t N_t - \kappa V_t - I_t, \quad (10)$$

in which  $W_t$  is the equilibrium wage rate. Taking  $W_t$ , the household's stochastic discount factor,  $M_{t+1}$ , and the vacancy filling rate,  $q(\theta_t)$ , as given, the firm chooses optimal investment and the optimal number of vacancies to maximize the cum-dividend market value of equity,  $S_t$ :

$$S_t \equiv \max_{\{V_{t+\tau}, N_{t+\tau+1}, I_{t+\tau}, K_{t+\tau+1}\}_{\tau=0}^{\infty}} E_t \left[ \sum_{\tau=0}^{\infty} M_{t+\tau} D_{t+\tau} \right], \quad (11)$$



subject to equations (7) and (8) as well as a nonnegativity constraint on vacancies,  $V_t \geq 0$ . Because  $q(\theta_t) > 0$ ,  $V_t \geq 0$  is equivalent to  $q(\theta_t)V_t \geq 0$ . In contrast, equation (9) implies that  $\partial\Phi_t/\partial I_t = a_2(I_t/K_t)^{-1/\nu}$ , which goes to infinity as investment,  $I_t$ , goes to zero. As such,  $I_t$  is always positive.

From the first-order conditions for  $I_t$  and  $K_{t+1}$ , we obtain the investment Euler equation:

$$\frac{1}{a_2} \left( \frac{I_t}{K_t} \right)^{1/\nu} = E_t \left[ M_{t+1} \left[ \frac{\partial Y_{t+1}}{\partial K_{t+1}} + \frac{1}{a_2} \left( \frac{I_{t+1}}{K_{t+1}} \right)^{1/\nu} (1 - \delta + a_1) + \frac{1}{\nu - 1} \frac{I_{t+1}}{K_{t+1}} \right] \right]. \quad (12)$$

Equivalently,  $E_t[M_{t+1}r_{Kt+1}] = 1$ , in which  $r_{Kt+1}$  is the investment return:

$$r_{Kt+1} \equiv \frac{\partial Y_{t+1}/\partial K_{t+1} + (1/a_2)(1 - \delta + a_1)(I_{t+1}/K_{t+1})^{1/\nu} + (1/(\nu - 1))(I_{t+1}/K_{t+1})}{(1/a_2)(I_t/K_t)^{1/\nu}}. \quad (13)$$

Let  $\lambda_t$  be the multiplier on  $q(\theta_t)V_t \geq 0$ . From the first-order conditions with respect to  $V_t$  and  $N_{t+1}$ , we obtain the intertemporal job creation condition:

$$\frac{\kappa}{q(\theta_t)} - \lambda_t = E_t \left[ M_{t+1} \left[ \frac{\partial Y_{t+1}}{\partial N_{t+1}} - W_{t+1} + (1 - s) \left( \frac{\kappa}{q(\theta_{t+1})} - \lambda_{t+1} \right) \right] \right]. \quad (14)$$

Equation (14) implies that  $E_t[M_{t+1}r_{Nt+1}] = 1$ , in which  $r_{Nt+1}$  is the hiring return:

$$r_{Nt+1} \equiv \frac{\partial Y_{t+1}/\partial N_{t+1} - W_{t+1} + (1 - s)(\kappa/q(\theta_{t+1}) - \lambda_{t+1})}{\kappa/q(\theta_t) - \lambda_t}. \quad (15)$$

Finally, the optimal vacancy policy also satisfies the Kuhn-Tucker conditions:

$$q(\theta_t)V_t \geq 0, \quad \lambda_t \geq 0, \quad \text{and} \quad \lambda_t q(\theta_t)V_t = 0. \quad (16)$$

Under constant returns to scale, the stock return of the representative firm,  $r_{St+1}$ , is a weighted average of the investment return and the hiring return (the Internet Appendix):

$$r_{St+1} = \frac{\mu_{Kt}K_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}}r_{Kt+1} + \frac{\mu_{Nt}N_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}}r_{Nt+1}, \quad (17)$$

in which the shadow value of capital,  $\mu_{Kt}$ , equals the marginal cost of investment,  $(1/a_2)(I_t/K_t)^{1/\nu}$ , and the shadow value of labor,  $\mu_{Nt}$ , equals the marginal cost of hiring,  $\kappa/q(\theta_t) - \lambda_t$ .

The equilibrium wage rate is determined endogenously by applying the sharing rule per the outcome of a generalized Nash bargaining process between employed workers and the firm (Pissarides 2000). Let  $\eta \in (0, 1)$  be the workers' relative bargaining weight and  $b$  the workers' flow value of unemployment. The equilibrium wage rate is given by (the Internet Appendix):

$$W_t = \eta \left( \frac{\partial Y_t}{\partial N_t} + \kappa \theta_t \right) + (1 - \eta)b. \quad (18)$$

The wage rate increases with the marginal product of labor,  $\partial Y_t / \partial N_t$ , and the vacancy cost per unemployed worker,  $\kappa \theta_t$ . Intuitively, the more productive the workers are, and the more costly for the firm to fill a vacancy, the higher the wage rate is for the employed workers. In addition, the workers' bargaining weight,  $\eta$ , affects the wage elasticity to labor productivity. The lower  $\eta$  is, the more the equilibrium wage is tied with the constant  $b$ , reducing the wage elasticity to productivity.

The competitive equilibrium consists of optimal investment,  $I_t$ , vacancy posting,  $V_t$ , multiplier,  $\lambda_t$ , and consumption,  $C_t$ , such that (i)  $C_t$  satisfies the consumption Euler equation (2); (ii)  $I_t$  satisfies the investment Euler equation (12), and  $V_t$  and  $\lambda_t$  satisfy the intertemporal job creation condition (14) and the Kuhn-Tucker conditions (16), while taking the stochastic discount factor,  $M_{t+1}$ , in equation (3), and the equilibrium wage in equation (18) as given; and (iii) the goods market clears:

$$C_t + \kappa V_t + I_t = Y_t. \quad (19)$$

Solving for the competitive equilibrium is computationally challenging. We adapt Petrosky-Nadeau and Zhang's (2017) globally nonlinear projection method with parameterized expectations to our setting (Appendix A). The state space consists of employment, capital, and productivity. We parameterize the conditional expectation in the right-hand side of equation (14) and solve for the indirect utility, investment, and conditional expectation functions from equations (1), (12), and (14). We use Rouwenhorst's (1995) discrete state method to approximate the log productivity with 17 grid points. We use the finite element method with cubic splines on 50 nodes on the employ-

ment space and 50 nodes on the capital space and take their tensor product on each grid point of productivity. To solve the resulting system of 127,500 equations, we use the derivative-free fixed point iteration with a small damping parameter (Judd, Maliar, Maliar, and Valero 2014).

### 3 Quantitative Results

We describe our data in Section 3.1 and calibrate the model in Section 3.2. We examine the model’s unconditional moments in Section 3.3, sources of the equity premium in Section 3.4, and time-varying risks and risk premiums in Section 3.5. Finally, we report comparative statics in Section 3.6.

#### 3.1 Data

For business cycle moments, we use the historical cross-country panel of output, consumption, and investment from Jordà, Schularick, and Taylor (2017), who in turn build on Barro and Ursúa (2008). For asset pricing moments, we use the Jordà et al. (2019) cross-country panel. We obtain the data from the Jordà-Schularick-Taylor macrohistory database.<sup>4</sup> The database contains macro and return series for 17 developed countries. The only missing series are returns for Canada, which we supplement from the Dimson-Marsh-Staunton (2002) database purchased from Morningstar. Although the Dimson-Marsh-Staunton database contains asset prices and the Barro-Ursúa database provides consumption and output series for more countries, we mainly rely on the Jordà-Schularick-Taylor database because it provides quantities and asset prices for the same set of countries. More important, it also contains investment series. The sample starts as early as 1871 and ends in 2015.<sup>5</sup>

Table 1 shows the properties of log growth rates of real consumption, output, and investment per capita in the historical panel. From Panel A, the consumption growth is on average 1.62% per annum, with a volatility of 5.45%, and a skewness of  $-0.67$ , all averaged across 17 countries. The first-order autocorrelation is 0.12. The consumption volatility exhibits a substantial amount

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<sup>4</sup><http://www.macrohistory.net/data>.

<sup>5</sup>More precisely, in the Jordà-Schularick-Taylor database, the consumption, output, and investment series start in 1870, meaning that their growth rates start in 1871. The quantities series end in 2016, but asset prices end in 2015.

of cross-country variation, ranging from 2.76% in UK to 8.72% in Belgium. The first-order autocorrelations also varies widely across countries, ranging from  $-0.2$  in Switzerland to 0.39 in France.

From Panel B, averaged across countries, the output growth has a mean of 1.78% per annum, a volatility of 5.1%, a skewness of  $-1.06$ , and a first-order autocorrelation of 0.18. The output volatility of 5.1% is lower than the consumption volatility of 5.45%.<sup>6</sup> Finally, Panel C shows that the investment growth volatility is high on average, 13.5% per annum, varying from 8.2% in Netherlands to 24.4% in the United States. Its first-order autocorrelation is 0.13.

Following Barro (2006), we calculate leverage-adjusted equity premium as one minus financial leverage times the unadjusted equity premium and calculate leverage-adjusted market volatility as the standard deviation of the leverage-weighted average of stock market and bill returns. We set leverage to be 0.29, which is the mean market leverage ratio in a cross-country panel reported in Fan, Titman, and Twite (2012). From Panel D, the leverage-adjusted equity premium is 4.36% per annum on average, varying from 2.71% in Portugal to 6.8% in Finland. The leverage-adjusted stock market volatility is on average 16%, ranging from 11.9% in Denmark to 23% in Finland. For the real interest rate, the mean is only 0.82% across countries. Finland has the lowest mean interest rate of  $-0.74\%$ , whereas Denmark has the highest of 3.08%. Finally, the real interest rate volatility is on average 7.3%, ranging from 4.32% in Australia to 13.22% in Germany.<sup>7</sup>

The asset pricing literature has traditionally focused only on the postwar U.S. data. Table S2 in the Internet Appendix reports basic macro and asset pricing moments in the 1950–2015 cross-country sample. The real consumption, output, and investment growth rates are less volatile, with standard deviations of 2.4%, 2.47%, and 7.06% per annum, respectively, averaged across countries. The U.S. macro volatilities are lower still at 1.73%, 2.21%, and 4.98%, respectively. Relatedly,

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<sup>6</sup>As explained in Barro and Ursúa (2008), government purchases rise sharply in wartime, decrease consumption relative to output, and raise the consumption volatility relative to the output volatility.

<sup>7</sup>When calculating the return moments, we require stock, bond, and bill returns to be nonmissing for a given year in a given country. Relaxing this restriction has little impact on the moments. In Table S1 in the Internet Appendix, we recalculate the moments with the longest sample possible for each series. The leverage-adjusted equity premium remains at 4.36% per annum, and the leverage-adjusted stock market volatility rises lightly from 16.04% to 16.08%. The mean real interest rate increases somewhat from 0.82% to 1.05%, and its volatility from 7.3% to 7.53%.

the consumption, output, and investment growth rates are more persistent in the postwar sample, with the first-order autocorrelations of 0.46, 0.39, and 0.29, respectively. However, the postwar leverage-adjusted equity premium is higher than the historical equity premium, 5.38% versus 4.36%. The leverage-adjusted stock market volatility is also higher in the postwar sample, 17.15% versus 16.04%. The evidence indicates that the postwar U.S. sample might not be representative. As such, we mostly rely on the historical cross-country panel to calibrate our model.

For labor market moments, to our knowledge, a historical cross-country panel is unavailable. As such, we work with the U.S. historical monthly series compiled by Petrosky-Nadeau and Zhang (2020).<sup>8</sup> Following Weir (1992), in addition to civilian unemployment rates, Petrosky-Nadeau and Zhang construct a separate series of private nonfarm unemployment rates, by subtracting farm and government employment from both civilian labor force and civilian employment. Because this unemployment series better depicts the functioning of the private economy (Lebergott 1964), we focus our calibration on this series. This series dates back to 1890, and the vacancy rate series to 1919.

From January 1890 to December 2015, the mean private nonfarm unemployment rate is 8.94%. The skewness and kurtosis of the unemployment rates are 2.13 and 9.5, respectively. In the postwar sample from January 1950 to December 2015, the mean unemployment rate is lower, 7.65%. Skewness is also smaller, 0.55, and kurtosis is close to that of the normal distribution, 2.92.

To calculate the second moments, we follow Shimer (2005) to take quarterly averages of monthly unemployment and vacancy rates to convert to quarterly series, which are detrended as Hodrick-Prescott (1997, HP) filtered proportional deviations from the mean with a smoothing parameter of 1,600. We do not take log deviations from the HP trend because the  $V \geq 0$  constraint can be occasionally binding in the model. From 1890 onward, the private nonfarm unemployment volatility is 24.43% per quarter (25.9% with log deviations). From 1919 onward, the vacancy rate volatility is 18.98% (17.36% with log deviations). For labor market tightness (the ratio of the vacancy rate over the private nonfarm unemployment rate), the volatility is 61.62% (but only 38.38% with log devia-

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<sup>8</sup>The series are available at <https://ars.els-cdn.com/content/image/1-s2.0-S0304393220300064-mmc2.csv>.

tions). The  $U$ - $V$  correlations are  $-0.57$  and  $-0.79$  across the two detrending methods, respectively.<sup>9</sup>

### 3.2 Calibration

We calibrate the model in monthly frequency. We set the time discount factor  $\beta = 0.9976$  to help match the mean real interest rate. We set the risk aversion,  $\gamma$ , to 10 per the long-run risks literature (Bansal and Yaron 2004). We set the elasticity of intertemporal substitution,  $\psi$ , to 2 per Barro (2009), who is in part based on Gruber’s (2013) microeconomic estimates. Following Gertler and Trigari (2009), we set the persistence of the log productivity,  $\rho_x$ , to be  $0.95^{1/3}$ , and set its conditional volatility,  $\sigma_x$ , to match the consumption growth volatility in the data. Instead of the output volatility, we target the consumption volatility, which is more important for the model’s asset pricing properties. This procedure yields a value of 0.015 for  $\sigma_x$ . This value implies a consumption volatility of 5.13% per annum, which is close to but lower than 5.45% in the data (Table 1). However, the output volatility is 6.43%, which is higher than 5.1% in the data.

For the CES production function, we set  $\omega = -1.5$ . This  $\omega$  value implies an elasticity of capital-labor substitution of 0.4, which is the point estimate in Chirinko and Mallick (2017). When calibrating the distribution parameter,  $\alpha$ , we target the average labor share. Gollin (2002) shows that factor shares are approximately constant across time and space. Table S3 in the Internet Appendix reports the labor shares for the 12 countries that are in both the Gollin and the Jordà-Schularick-Taylor databases. The average labor shares across the countries from Gollin’s first two adjustment methods are 0.765 and 0.72, respectively, with an average of 0.743. Gollin emphasizes that these two adjustments “give estimated labor shares that are essentially flat across countries and over time (p. 471).” As such, we set  $\alpha = 0.25$ , which yields an average labor share of 0.746 in simulations.

The distribution parameter,  $\alpha$ , is close to one minus the average labor share only in the “normalized” CES production function, in which the capital unit is comparable to the labor unit

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<sup>9</sup>Labor market volatilities are lower in the postwar sample. From 1950 onward, the private nonfarm unemployment volatility is 13.81% per quarter, and the vacancy rate volatility is 13.49%. The market tightness volatility is 26.17%, and the  $U$ - $V$  correlation  $-0.9$ . Detrending with log deviations from the HP trend yields very similar estimates.

(Klump and La Grandville 2000). We calibrate the capital scalar,  $K_0$ , at 13.75 to set the labor share at the deterministic steady state at 0.75. For comparison, the value of capital at the deterministic steady state is 16.14. Despite the model’s nonlinearity, the labor share is very close across the deterministic and stochastic steady states. We calibrate the long-run mean of the productivity,  $\bar{x} = 0.1887$ , to target the marginal product of labor,  $\partial Y_t / \partial N_t$ , around one on average in simulations.<sup>10</sup>

The supply elasticity of capital,  $\nu$ , governs the magnitude of adjustment costs. A lower  $\nu$  implies higher adjustment costs, which reduce the investment volatility but raise the consumption volatility. Alas, direct estimates of  $\nu$  seem scarce. We set  $\nu$  to 1.25 and the depreciation rate,  $\delta$ , to 1.25%. We set the separation rate,  $s$ , to 0.035, which is the average total nonfarm separation rate in the Job Openings and Labor Turnover Survey (JOLTS) at Bureau of Labor Statistics (BLS). The curvature of the matching function,  $\iota$ , is 1.25, which is based on Den Haan, Ramey, and Watson (2000).

### 3.2.1 Wage Inertia

We are left with the bargaining weight of workers,  $\eta$ , the flow value of unemployment activities,  $b$ , and the unit cost of vacancy posting,  $\kappa$ . To match the equity premium without overshooting the mean unemployment rate, we combine inertial wages and low vacancy costs. Specifically, we set  $\eta = 0.015$  and  $b = 0.91$ , which yield a wage elasticity to labor productivity of 0.256 in the model. We set the unit vacancy cost,  $\kappa$ , to 0.01, to obtain a mean unemployment rate of 8.63%, which is close to the average private nonfarm unemployment rate of 8.94% in the 1890–2015 sample.

Is the model implied wage elasticity to labor productivity empirically plausible? Hagedorn and Manovskii (2008), for example, estimate the wage elasticity to labor productivity to be 0.449 in the postwar 1951–2004 quarterly sample from BLS.<sup>11</sup> However, a voluminous literature on economic history documents severe wage inertia and quantifies its large impact during the Great Depression.<sup>12</sup>

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<sup>10</sup>Setting  $\partial Y_t / \partial N_t = 1$  at the deterministic steady state yields  $\bar{x} = 0.1787$ . However,  $\partial Y_t / \partial N_t$  at the stochastic steady state is somewhat lower than one. As such, we manually adjust  $\bar{x}$  to 0.1887 to yield the desired outcome.

<sup>11</sup>Both real wages and labor productivity are in logs and HP-filtered with a smoothing parameter of 1,600.

<sup>12</sup>Prominent examples include Eichengreen and Sachs (1985), Bernanke and Powell (1986), Bernanke and Carey (1996), Hanes (1996), Dighe (1997), Bordo, Erceg, and Evans (2000), Cole and Ohanian (2004), and Ohanian (2009).

As such, we extend the Hagedorn-Manovskii evidence to a historical U.S. sample.

To construct a historical series of real wages, we draw elements from Gordon (2016). From 1929 to 2015, we obtain compensation of employees from National Income and Product Accounts (NIPA) Tables 6.2A–D (line 3, private industries, minus line 5, farms) at Bureau of Economic Analysis. We obtain the number of full-time equivalent employees from NIPA Tables 6.5A–D (line 3, private industries, minus line 5, farms). Dividing the compensation of employees by the number of employees yields nominal wage rates (compensation per person). We deflate nominal wage rates with the personal consumption deflator from NIPA Table 1.1.4 (line 2) to obtain real wage rates.

From 1890 to 1929, we obtain the average (nominal) hourly compensation of production workers in manufacturing and consumer price index from measuringworth.com (Officer and Williamson 2020a, 2020b). The nominal compensation series from their Web site only has two digits after the decimal. We instead use the average hourly compensation series, with three digits after the decimal, from Officer (2009, Table 7.1). To obtain an index of hours, we divide the index of manhours by the index of persons engaged in manufacturing from Kendrick (1961, Table D-II). We multiply the average hourly compensation series with the hours index to obtain the nominal compensation per person, which we then deflate with the Officer-Williamson consumer price index to obtain the series of real wages. Finally, we splice this series in 1929 to the NIPA series from 1929 onward to yield an uninterrupted series from 1890 to 2015. Splicing means that we rescale the pre-1929 series so that its value in 1929 is identical to that for the NIPA post-1929 series.<sup>13</sup> Finally, for labor productivity, we use the historical 1890–2015 series from Petrosky-Nadeau and Zhang (2020).<sup>14</sup> We

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<sup>13</sup>We differ from Gordon (2016) in two aspects. First, Gordon measures real wages as real compensation per manhour. We instead use real compensation per person that better fits our model with no hours. This practice seems standard in the macro labor literature (Shimer 2005). Second, Gordon measures nominal compensation as total compensation of employees from NIPA Table 1.10 (line 2), which includes government and farm employees. We instead use employee compensation for the private nonfarm sector, which matches the measurement of labor productivity.

<sup>14</sup>The monthly series is the ratio of a nonfarm business real output series over a private nonfarm employment series. The real output series draws from Kendrick (1961) and NIPA (from 1929 onward) as well as monthly industrial production series (as monthly indicators) from Miron and Romer (1990) and Federal Reserve Bank of St. Louis (from 1919 onward). The private nonfarm employment series draws from Weir (1992) and Current Employment Statistics at BLS as well as monthly employment indicators from NBER macrohistory files. From January 1947 onward, the monthly labor productivity series is benchmarked to the quarterly nonfarm business real output per job series from BLS.



time-aggregate their monthly series into annual by taking the monthly average within a given year.

We detrend the annual real wages and labor productivity series as log deviations from their HP-trends with a smoothing parameter of 6.25, which is equivalent to a quarterly smoothing parameter of 1,600.<sup>15</sup> In our postwar 1950–2015 annual sample, regressing the log real wages on the log labor productivity yields a wage elasticity of 0.406, with a standard error of 0.081. The elasticity estimate is not far from the Hagedorn-Manovskii estimate of 0.449 in their 1951–2004 quarterly sample.

More important, in our 1890–2015 historical sample, the wage elasticity to labor productivity is estimated to be 0.267, with a standard error of 0.066. Deflating the pre-1929 nominal compensation series with the Johnston-Williamson (2020) implicit GDP deflator, as opposed to the Officer-Williamson (2020b) consumer price index, yields a similar wage elasticity of 0.263, with a standard error of 0.062. Our evidence that real wages are more inertial in the historical sample accords well with the economic history literature (footnote 12). In particular, the low wage elasticity to labor productivity, 0.256, in our model is empirically plausible.

Our value of  $b = 0.91$  might seem high, as the marginal product of labor is around one in the model’s simulations. However, the value of  $b$  includes unemployment benefits, the value of home production, self-employment, leisure, and disutility of work. Hagedorn and Manovskii (2008) argue that  $b$  should equal the marginal product of capital in a perfectly competitive labor market. Ljungqvist and Sargent (2017) show that to explain the unemployment volatility, a search model must diminish the fundamental surplus, which is the fraction of output allocated to the firm by the labor market. We view our high- $b$  calibration as perhaps the simplest way to achieve this goal. More important, we view our high- $b$ -low- $\eta$  calibration as a parsimonious metaphor for real wage inertia. More explicit structures of wage inertia, such as alternating offer bargaining in Hall and Milgrom (2008) or staggered multiperiod Nash bargaining in Gertler and Trigari (2009), are likely to deliver similar quantitative results but would complicate our model greatly.<sup>16</sup>

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<sup>15</sup>Ravn and Uhlig (2002) show that the smoothing parameter should be adjusted by the fourth power of the observation frequency ratio, which equals four going from the quarterly to annual frequency. In particular,  $1600/4^4 = 6.25$ .

<sup>16</sup>The high- $b$  calibration is also of contemporary interest. Ganong, Noel, and Vavra (2020) document that under

### 3.3 Unconditional Moments

We report basic business cycle, labor market, and asset pricing moments from the model economy.

#### 3.3.1 Business Cycle Moments

From the model’s stationary distribution (after a burn-in period of 1,200 months), we repeatedly simulate 10,000 artificial samples, each with 1,740 months (145 years). The length of each sample matches the length of the Jordà-Schularick-Taylor database (1871–2015). On each artificial sample, we time-aggregate monthly consumption, output, and investment into annual observations. We add up 12 monthly observations within a given year and treat the sum as the year’s annual observation. For each annual series, we compute its volatility, skewness, kurtosis, and autocorrelations of up to five lags of log growth rates. For each moment, we report the mean as well as the 5th, 50th, and 95th percentiles across the 10,000 simulations. We also report the  $p$ -value that is the fraction with which a given moment in the model is higher than its matching moment in the data. The fraction can be interpreted as the  $p$ -value for a one-sided test of our model using the moment in question.

Panel A of Table 2 shows that the model does a good job in matching consumption moments. None of the  $p$ -values for one-sided tests are significant at the 5% level. The consumption growth volatility in the model is 5.13% per annum, which is close to 5.45% in the data ( $p = 0.41$ ). Kurtosis is 8.09 in the model, which is close to 10.34 in the data ( $p = 0.18$ ). The first-order autocorrelation is 0.21 in the model, which is higher than 0.12 in the data, but the difference is insignificant ( $p = 0.78$ ). The autocorrelations at higher orders are close to zero in the model as in the data.

From Panel B, the output volatility in the model is 6.43% per annum, which is higher than 5.1% in the data, but the difference is insignificant ( $p = 0.86$ ). The model falls short in explaining the skewness, 0.09 versus  $-1.06$ , and kurtosis, 5.45 versus 14.09, of the output growth. Both differences are significant. The model comes close to match the first-order autocorrelation, 0.2 versus 0.18.

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the 2020 Coronavirus Aid, Relief, and Economic Security Act, the ratio of mean benefits to mean earnings in the data is roughly 100%. The median replacement ratio is even higher at 134%. Finally, 68% of eligible unemployed workers have replacement ratios higher than 100%, and 20% of the workers have replacement ratios higher than 200%.

From Panel C, the investment volatility in the model is only 8.59% per annum, which is lower than 13.53% in the data. The difference is significant, but none of the  $p$ -values for other investment moments are significant. The kurtosis in the model is 7.12, relative to 10.75 in the data ( $p = 0.08$ ). The first-order autocorrelation is 0.15 in the model, which is close to 0.13 in the data.

### 3.3.2 Labor Market Moments

Panel D of Table 2 shows that the model does a good job matching the first four moments of the unemployment rate. The mean unemployment rate is 8.63% in the model, which is close to 8.94% in the data ( $p = 0.37$ ). The skewness is 2.64, relative to 2.13 in the data ( $p = 0.53$ ), and the kurtosis, 13.45 versus 9.5 ( $p = 0.35$ ). The unemployment volatility is 32.2% per quarter, which is higher than 24.43% in the data. However, the difference is not significant ( $p = 0.76$ ).

The vacancy rate volatility is 33.73% per quarter in the model, which is significantly higher than 18.98% in the data. The volatility of labor market tightness is 33.98%, which is significantly lower than 61.62% in the data. However, as noted, this data moment is sensitive to detrending method and is only 38.38% with log deviations from the HP-trend. The unemployment-vacancy correlation is only  $-0.07$  in the model, which is lower in magnitude than  $-0.57$  in the data. However, this moment is also sensitive to detrending method. Using the monthly data simulated from the model with no detrending yields a  $U$ - $V$  correlation of  $-0.475$ , which is close to the matching data moment of  $-0.517$ , and the difference is insignificant ( $p = 0.66$ ). Finally, the wage elasticity to labor productivity is 0.256, and the data moment of 0.267 yields an insignificant  $p$ -value of 0.23.

### 3.3.3 Asset Pricing Moments

Most important, Panel E shows that our general equilibrium production economy succeeds in yielding an equity premium of 4.26% per annum, which is close to 4.36% in the data. The data moment lies comfortably within the model's 90% confidence interval, with a  $p$ -value of 0.34. The mean interest rate is 1.59% in the model, which is not far from 0.82% in the data. The data moment is again lies within the model's 90% confidence interval ( $p = 0.87$ ).

The model implies a stock market volatility of 11.77% per annum, which is significantly lower than the data moment of 16.04%, although the U.S. volatility of 13.66% (Table 1) falls within the model's 90% confidence interval. The model's performance in matching stock market volatility improves over prior attempts in general equilibrium production economies (Gourio 2012).

The interest rate volatility in the model is 3.13% per annum, which is significantly lower than 7.3% in the data. The most likely reason is that we do not model sovereign default and hyperinflation that are the driving forces behind the historically high interest rate volatilities in Germany, Italy, and Japan. These destructive forces play only a limited role in the U.S., which has an interest rate volatility of only 4.65% (Table 1). It is well within the model's 90% confidence interval.

### **3.4 Sources of the Equity Premium**

In this subsection we examine the driving forces behind the model's equity premium.

#### **3.4.1 Dividend Dynamics**

Rouwenhorst (1995) points out the difficulty in explaining the equity premium in production economies. Unlike endowment economies, in which dividends are exogenously specified to fit the data, dividends are often endogenously countercyclical in production economies. Dividends equal profits (output minus wages) minus investment. Intuitively, with frictionless labor market, wages equal the marginal product of labor, which is almost as procyclical as output. With the Cobb-Douglas production function, the marginal product of labor is exactly proportional to output. As such, profits are no more procyclical than output. However, due to consumption smoothing, investment is more procyclical than output and profits, rendering dividends countercyclical. Kaltenbrunner and Lochstoer (2010) demonstrate this insight in a stochastic growth model.

In contrast, dividends are endogenously procyclical in our search economy. Under the benchmark calibration, wages are more inertial than the marginal product of labor, making profits more procyclical than output. The magnified procyclical dynamics of profits then overpower the pro-

cyclical dynamics of vacancy costs and capital investment to make dividends procyclical.<sup>17</sup>

To what extent are the model’s implied dividend dynamics empirically plausible? For each country, the Jordà-Schularick-Taylor macrohistory database provides separate capital gain, dividend-to-price, and consumer price index series, from which we construct the real dividend series (the Internet Appendix). Table S4 shows that dividends are procyclical in the historical cross-country panel. The correlation between the cyclical components of annual dividends and output is on average 0.11 across the countries, ranging from  $-0.02$  from Portugal to  $0.47$  in the U.S. Only 3 out of 17 countries have negative correlations, all of which are small in magnitude. The relative volatility of dividends (the ratio of the dividend volatility over the output volatility) is 8.61 across the countries, varying from 3.06 from Portugal to 16.81 in Netherlands (3.18 in the U.S.).<sup>18</sup> Time-aggregating annual observations into 3- and 5-year observations raises the dividend-output correlation to 0.31 and 0.35 and lowers the relative volatility of dividends to 6.54 and 5.69, respectively.

The model explains procyclical dividends but overshoots the dividend-output correlation, 0.947. The model also underestimates the relative volatility of dividends at 2.89. Both differ significantly from their data moments. Time-aggregating does not materially affect the model’s estimates. The dividend-output correlations are 0.954 and 0.952, and the relative volatility of dividends 2.83 and 2.74 at the 3- and 5-year frequencies, respectively. In the historical data, there are likely measurement errors in real dividends, which tend to average out over time, yielding higher dividend-output correlations at longer horizons. In contrast, no such measurement errors exist within the model.

A possible reason why the model overshoots the dividend-output correlation is that dividends in the data refer only to cash dividends, but dividends in the model match more closely to net payouts. Net payouts in the data include not only cash dividends but also share repurchases net of

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<sup>17</sup>Petrosky-Nadeau, Zhang, and Kuehn (2018) examine this mechanism in a baseline search model without capital. However, with capital, consumption smoothing via investment strengthens the countercyclicality of dividends. We overcome this core challenge via wage inertia, for which we also provide new, supportive evidence (Section 3.2.1).

<sup>18</sup>Due to a few zero-dividend observations (7 out of 2,034), we detrend dividend and output series with HP-filtered proportional deviations from the mean. Using HP-filtered log deviations after discarding the 7 observations yields a higher dividend-output correlation of 0.24 and a relative dividend volatility of 7.92 averaged across the countries.

equity issuances (Boudoukh et al. 2007). Alas, to our knowledge, a historical sample of net payouts is not available. Perhaps more important, our model has only one shock, which drives the high dividend-output correlation, but there exist most likely multiple shocks in the data.

### 3.4.2 Disaster Dynamics

As shown in Petrosky-Nadeau, Zhang, and Kuehn (2018), the search model of equilibrium unemployment gives rise endogenously to rare disasters. To explain the equity premium, we formulate a more general model by incorporating both recursive utility and capital accumulation. Disaster risks in consumption play a key role in explaining the equity premium in our framework.

To characterize disasters in the data, we apply the Barro-Ursúa (2008) peak-to-trough method on the Jordà-Schularick-Taylor cross-country panel of consumption and output. Disasters are identified as episodes, in which the cumulative fractional decline in consumption or output exceeds a predetermined hurdle rate. We adopt two such hurdle rates, 10% and 15%.<sup>19</sup> We adjust for trend growth in the data because our model abstracts from growth. We subtract the mean log annual consumption growth of 1.62% from each consumption growth observation and subtract the mean log annual output growth of 1.78% from each output growth in the historical data (Table 1).

Table 3 shows that with a disaster hurdle rate of 10%, the consumption disaster probability is 6.4%, and the output disaster probability 5.78% in the cross-country panel. With a higher hurdle rate of 15%, the probabilities drop to 3.51% and 2.62%, respectively. The disaster size is 23.2% and 22.3% for consumption and output with a hurdle rate of 10%, but higher, 30.4 and 32.9, respectively, with a higher hurdle rate of 15%. The duration for consumption and output disasters lasts 4.2 and 4.1 years with a hurdle rate of 10%, but 4.5 and 5 years with a hurdle rate of 15%.

The model implied consumption disaster dynamics, which are crucial for the equity premium,

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<sup>19</sup>Suppose there are two states, normalcy and disaster, in a given period. The number of disaster years is the number of years in the interval between peak and trough for each disaster event. The number of normalcy years is the total number of years in the sample minus the number of disaster years. The disaster probability is the likelihood with which the economy switches from normalcy to disaster in a given year. We calculate this probability as the ratio of the number of disasters over the number of normalcy years. For each disaster event, the disaster size is the cumulative fractional decline in consumption or output from peak to trough. Duration is the number of years from peak to trough.

are empirically plausible. We simulate 10,000 artificial samples from the model’s stationary distribution, each with 1,740 months, matching the 1871–2015 sample length. On each sample, we time-aggregate monthly into annual consumption and apply the exact peak-to-trough method as in the data. From Panel A of Table 3, the disaster probabilities are 5.83% and 3.64%, which are relatively close to 6.4% and 3.51% in the data, with the hurdle rates of 10% and 15%, respectively. The size and duration of consumption disasters in the model are also close to those in the data, 23.4% versus 23.2% for size, and 4.1 versus 4.2 years for duration, with a hurdle rate of 10%, for example. The  $p$ -values all indicate that the differences between the model and data moments are insignificant.

As noted, consumption is more volatile than output in the cross-country panel, likely due to government purchases during wartime (Barro and Ursúa 2008). In contrast, consumption is naturally less volatile than output in production economies because of consumption smoothing. We focus on matching consumption dynamics because of their paramount importance for the equity premium. Consequently, the model overshoots output disasters. From Panel B, the output disaster probability is 10.9%, which is higher than 5.78% in the data ( $p = 0.97$ ), with a hurdle rate of 10%. With a higher hurdle of 15%, the disaster probability is 6.1% in the model, which is still higher than 2.62% in the data ( $p = 0.94$ ). However, disaster size and duration are relatively close to their data moments.

### 3.4.3 Consumption Dynamics

We dig deeper by comparing consumption dynamics in the search economy with those specified in the long-run risks literature (Bansal and Yaron 2004). Kaltenbrunner and Lochstoer (2010) show that long-run risks (high persistence in expected consumption growth) arise endogenously in production economies with frictionless labor market via consumption smoothing. Because of persistent aggregate productivity and consumption smoothing, long-run risks might also be present in our model. What is the relative role of long-run risks compared with disaster risks in our model? This economic question is important because different specifications of consumption dynamics can largely accord with observed moments of consumption growth, such as volatilities and autocorre-

lations, in the data. However, different specifications imply vastly different economic mechanisms.

We calculate the expected consumption growth and conditional consumption growth volatility in the model's state space. We use these solutions to simulate one million monthly periods from the model's stationary distribution. Fitting the consumption growth process specified by Bansal and Yaron (2004) on the simulated data yields:

$$g_{Ct+1} = E_t[g_{Ct+1}] + \sigma_{Ct} \epsilon_{t+1}^g \quad (20)$$

$$E_{t+1}[g_{Ct+2}] = 0.288 E_t[g_{Ct+1}] + 0.705 \sigma_{Ct} \epsilon_{t+1}^e \quad (21)$$

$$\sigma_{Ct+1}^2 = 0.008^2 + 0.964(\sigma_{Ct}^2 - 0.008^2) + 0.421 \times 10^{-5} \epsilon_{t+1}^V, \quad (22)$$

in which  $g_{Ct+1}$  is realized consumption growth,  $E_t[g_{Ct+1}]$  expected consumption growth,  $\sigma_{Ct}$  conditional volatility of  $g_{Ct+1}$ , and  $\epsilon_{t+1}^g$ ,  $\epsilon_{t+1}^e$ , and  $\epsilon_{t+1}^V$  are i.i.d. standard normal shocks. In addition, the unconditional correlation between  $\epsilon_{t+1}^g$  and  $\epsilon_{t+1}^e$  is 0.048, the unconditional correlation between  $\epsilon_{t+1}^e$  and  $\epsilon_{t+1}^V$  is 0.024, and the unconditional correlation between  $\epsilon_{t+1}^g$  and  $\epsilon_{t+1}^V$  is 0.079 in simulations.

Equation (21) shows that the persistence in expected consumption growth is only 0.288 in our model, which is substantially lower than 0.979 in Bansal and Yaron (2004).<sup>20</sup> However, our expected consumption growth is more volatile, with its conditional volatility about 70.5% of the conditional volatility of realized consumption growth. This fraction is much higher than 4.4% in Bansal and Yaron. Similarly, our persistence of expected consumption growth, 0.288, is also much lower than that implied by baseline production economies in Kaltenbrunner and Lochstoer (2010).<sup>21</sup> As such, despite recursive utility and autoregressive productivity shocks, long-run risks (in the sense of highly persistent expected consumption growth) do not play an important role in our economy.

Equation (22) shows that the search economy gives rise endogenously to time-varying volatil-

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<sup>20</sup>Bansal and Yaron (2004) specify the monthly consumption growth process to be  $E_{t+1}[g_{Ct+2}] = 0.979 E_t[g_{Ct+1}] + 0.044 \sigma_{Ct} \epsilon_{t+1}^e$ ,  $g_{Ct+1} = 0.0015 + E_t[g_{Ct+1}] + \sigma_{Ct} \epsilon_{t+1}^g$ , and  $\sigma_{Ct+1}^2 = 0.0078^2 + 0.987(\sigma_{Ct}^2 - 0.0078^2) + 0.23 \times 10^{-5} \epsilon_{t+1}^V$ , in which  $\epsilon_{t+1}^e$ ,  $\epsilon_{t+1}^g$ , and  $\epsilon_{t+1}^V$  are i.i.d. and mutually uncorrelated standard normal shocks.

<sup>21</sup>Kaltenbrunner and Lochstoer (2010, Table 6) show that the consumption growth follows  $E_{t+1}[g_{Ct+2}] = 0.986 E_t[g_{Ct+1}] + 0.093 \sigma_{Ct} \epsilon_{t+1}^e$  and  $g_{Ct+1} = 0.0013 + E_t[g_{Ct+1}] + \sigma_{Ct} \epsilon_{t+1}^g$ , with transitory productivity shocks. With permanent shocks,  $E_{t+1}[g_{Ct+2}] = 0.99 E_t[g_{Ct+1}] + 0.247 \sigma_{Ct} \epsilon_{t+1}^e$ . However,  $\sigma_{Ct}$  is largely constant in both models.



ities (Bloom 2009). The consumption conditional variance appears “stochastic” in our model. Its persistence is 0.964, which is lower than 0.987 calibrated in Bansal and Yaron (2004) and 0.999 in Bansal, Kiku, and Yaron (2012). However, the volatility of our stochastic variance is  $0.42 \times 10^{-5}$ , which is higher than  $0.23 \times 10^{-5}$  in Bansal and Yaron and  $0.28 \times 10^{-5}$  in Bansal, Kiku, and Yaron. The time-variation of volatilities is another important dimension along which our search economy differs from stochastic growth models. These models with frictionless labor market yield largely constant volatilities (Kaltenbrunner and Lochstoer 2010). Perhaps more important, our quantitative results in equation (22) suggest that long-run risks in consumption volatility can be observationally equivalent to consumption disaster risks, potentially lending support to disaster models.

### 3.5 Time-varying Risks and Risk Premiums

We quantify the model’s implications on time-varying equity premium and stock market volatility.

#### 3.5.1 Equilibrium Properties

We first evaluate qualitative implications of the model’s competitive equilibrium. From the model’s stationary distribution (after a burn-in period of 1,200 months), we simulate a long sample of one million months. Figure 1 shows the heatmaps of key conditional moments against productivity. From Panel A, the price-to-consumption ratio,  $P_t/C_t$ , increases with productivity. In the 1-million-month sample, the correlations of  $P_t/C_t$  with productivity, output, unemployment, vacancy, and the investment rate are 0.98, 0.82,  $-0.51$ , 0.91, and 0.57, respectively. Clearly,  $P_t/C_t$  is procyclical.

In contrast, Panel B shows that the expected equity premium,  $E_t[r_{St+1}] - r_{ft+1}$ , is countercyclical. Its correlations with productivity, output, unemployment, vacancy, and the investment rate are  $-0.85$ ,  $-0.87$ , 0.66,  $-0.86$ , and  $-0.39$ , respectively. In addition, the correlation between the expected equity premium and price-to-consumption is  $-0.89$ . Stock market volatility,  $\sigma_{St}$ , is also countercyclical (Panel C). Its correlations with productivity, output, unemployment, vacancy, and the investment rate are  $-0.92$ ,  $-0.86$ , 0.59,  $-0.92$ , and  $-0.44$ , respectively. In addition, its correlations with the expected equity premium and price-to-consumption are 0.98 and  $-0.95$ , respectively.

Panel D shows that the riskfree rate,  $r_{ft+1}$ , is weakly procyclical in the model. Its correlations with productivity, output, unemployment, vacancy, and the investment rate are 0.11, 0.07,  $-0.02$ , 0.03, and 0.08, respectively. In addition, its correlations with the expected equity premium, stock market volatility, and price-to-consumption are  $-0.04$ ,  $-0.02$ , and 0.21, respectively. Panel E shows that expected consumption growth,  $E_t[g_{Ct+1}]$ , behaves similarly as the risk-free rate. The correlation between  $E_t[g_{Ct+1}]$  and  $r_{ft+1}$  is 0.999. Panel F shows that consumption volatility,  $\sigma_{Ct}$ , is weakly countercyclical. Although its correlations with output and unemployment are high,  $-0.43$  and  $0.72$ , its correlations with productivity and investment rate are low,  $-0.04$  and  $-0.24$ , respectively.

In all, the model implies strong predictability for stock market excess return and volatility, some predictability for consumption volatility, and weak to no predictability for consumption growth and the interest rate. Intuitively, wage inertia yields operating leverage. In bad times, output falls, but wage inertia causes profits to drop disproportionately more than output, thereby magnifying the procyclical covariation of profits and dividends, causing the expected equity premium to rise.

More important, the impact of wage inertia is stronger in bad times, when the profits are even smaller because of low productivity. This time-varying wage inertia amplifies the risks and risk premiums, making the expected equity premium and stock market volatility countercyclical.<sup>22</sup> In contrast, consumption growth and consumption volatility are less predictable because of consumption smoothing via capital investment. Despite adjustment costs, investment absorbs a large amount of shocks to render the first two moments of consumption growth less predictable.

### 3.5.2 Data

Before quantifying the model's implications on time-varying risks and risk premiums, Table 4 shows long-horizon regressions of stock market excess returns and log consumption growth on log price-to-consumption in the historical data. We follow Beeler and Campbell (2012) but implement the

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<sup>22</sup>Relatedly, Favilukis and Lin (2016) study this time-varying mechanism in a general equilibrium production economy with (exogenously specified) infrequent wage renegotiation, long-run risks, and labor adjustment costs. In contrast, wage inertia arises endogenously in our economy, and the equity premium arises from endogenous disaster risks.

tests on the Jordá-Schularick-Taylor historical cross-country panel. We perform the regressions on log price-to-consumption, as opposed to log price-to-dividend, because dividends (net payouts) can be negative in the model. To align the data moments with the model moments, we adjust excess returns in the data for financial leverage (by multiplying unadjusted excess returns with 0.71).

Panel A shows long-horizon predictive regressions of market excess returns:

$$\sum_{h=1}^H [\log(r_{St+h}) - \log(r_{ft+h})] = a + b \log(P_t/C_t) + u_{t+H}, \quad (23)$$

in which  $H$  is the forecast horizon,  $P_t$  real market index,  $C_t$  real consumption at the beginning of period  $t$ , and  $u_{t+H}$  the residual. Panel B shows long-horizon regressions of log consumption growth:

$$\sum_{h=1}^H \log(C_{t+h}/C_t) = a + b \log(P_t/C_t) + v_{t+H}, \quad (24)$$

in which  $v_{t+H}$  is the residual. In both long-horizon regressions,  $\log(P_t/C_t)$  is standardized to have a mean of zero and a volatility of one.  $H$  ranges from one to five years. Finally, the  $t$ -values are adjusted for heteroscedasticity and autocorrelations of  $2(H - 1)$  lags.

Panel A shows some evidence of predictability of market excess returns. The slopes are largely negative across the countries and forecast horizons from one to five years, and their  $t$ -values are often significant, especially at the longer horizons. The  $R$ -squares averaged across the countries vary from 1.87% to 9% as the forecast horizon goes from one to five years. The prior asset pricing literature has mostly focused on the U.S. sample, which is an outlier in Panel A. In particular, the U.S. features the strongest evidence of predictability in terms of the  $t$ -values of slopes and  $R$ -squares. For example, in the 5-year horizon, the  $R^2$  is 33.6% in the U.S. and 28% in the U.K., in contrast to 0% in Germany, 1% in Italy and Portugal, and 2% in France.

In the Internet Appendix (Table S5, Panel A), we document stronger stock market return predictability in the post-1950 sample. The slopes are all negative and mostly significant across the countries and forecast horizons. On average, the slopes are significant for all horizons except year

one. The  $R$ -squares range from 4.9% in year one to 17.8% in year five.

Panel B of Table 4 shows that consumption growth is largely unpredictable. In the historical sample, the slopes averaged across the countries are all negative but insignificant. Even at the 5-year horizon, the  $R^2$  is only 5.77% on average. In the post-1950 sample, the average slopes all flip to positive but remain insignificant, although the average  $R$ -squares increase somewhat, for example, to 9.1% in year five (Table S5, Panel B, the Internet Appendix).

Table 5 shows long-horizon regressions of excess return and consumption growth volatilities on log price-to-consumption. For a given forecast horizon,  $H$ , we measure excess return volatility as  $\sigma_{St,t+H-1} = \sum_{h=0}^{H-1} |\epsilon_{St+h}|$ , in which  $\epsilon_{St+h}$  is the  $h$ -period-ahead residual from the first-order autoregression of log excess returns,  $\log(r_{St+1}) - \log(r_{ft+1})$  (again adjusted for financial leverage). Panel A performs long-horizon predictive regressions of excess return volatilities:

$$\log \sigma_{St+1,t+H} = a + b \log(P_t/C_t) + u_{t+H}^\sigma. \quad (25)$$

In Panel B, the consumption volatility is  $\sigma_{Ct,t+H-1} = \sum_{h=0}^{H-1} |\epsilon_{Ct+h}|$ , in which  $\epsilon_{Ct+h}$  is the  $h$ -period-ahead residual from the first-order autoregression of log consumption growth,  $\log(C_{t+1}/C_t)$ . We then perform long-horizon predictive regressions of consumption volatilities:

$$\log \sigma_{Ct+1,t+H} = a + b \log(P_t/C_t) + v_{t+H}^\sigma. \quad (26)$$

Panel A of Table 5 shows weak predictability for excess return volatilities. The average slopes are all negative and marginally significant in the first two years. The average  $R$ -squares range from 6.3% in year one to 19% in year five. However, the evidence is sensitive to sample period. In the post-1950 sample, the average slopes are all insignificant, with mixed signs (Table S6, Panel A, the Internet Appendix). Consumption volatilities are essentially unpredictable with log price-to-consumption. In the historical sample, the average slopes are all positive and, in long horizons, marginally significant. However, in the post-1950 sample, the slopes all flip to negative and insignificant.

### 3.5.3 The Model's Performance

We simulate 10,000 samples from the model's stationary distribution, each with 1,740 months. On each sample, we time-aggregate monthly returns and consumption into annual observations and implement the same procedures as in the data. Overall, the model succeeds in explaining stock market predictability but somewhat overstates consumption growth predictability, especially its volatility.

Table 6 shows the details. From Panel A, market excess returns are predictable in the model. The slopes are all significantly negative, and the  $R$ -squares range from 3.9% in year one to 13.5% in year five. None of the  $p$ -values for the slopes, their  $t$ -values, and  $R$ -squares are significant at the 5% level. From Panel B, the model overstates somewhat the consumption growth predictability. The slopes are all significantly negative. However, except for year one, the  $p$ -values for the slopes and their  $t$ -values indicate only insignificant differences between the model and data moments.

Panel C shows that stock market volatility is weakly predictable with log price-to-consumption in the model. As in the data, the slopes are all negative but insignificant. None of the  $p$ -values for slopes and their  $t$ -values suggest that the model moments deviate significantly from their data counterparts. However, the  $R$ -squares in the model are significantly lower than those in the data. More important, from Panel D, the model overstates the predictability of consumption growth volatility. While the slopes are mostly insignificant and positive in the data, the slopes in the model are significantly negative, and the  $p$ -values for the slopes and their  $t$ -values are significant.

## 3.6 Comparative Statics

In this subsection, we conduct comparative statics to shed light on the inner workings of our model. In each experiment, we vary one parameter only, while keeping all the other parameters identical to those in the benchmark calibration. (For log utility, we set both the risk aversion and intertemporal elasticity of substitution to one.) In all experiments, we recalibrate the capital scalar,  $K_0$ , to ensure the average labor share is unchanged from the benchmark calibration. Otherwise, the impact from changing a given parameter would be confounded with the impact of changing the labor share. The

only exception is the  $\alpha = 0.3$  experiment, in which we recalibrate  $K_0$  to match the average labor share of 0.7. The simulations follow the same design as in the benchmark model.

### 3.6.1 Preference Parameters

Table 7 details the results. Not surprisingly, the risk aversion,  $\gamma$ , has a quantitatively important impact on the equity premium. Reducing  $\gamma$  from 10 to 7.5 and further to 5 lowers the equity premium from 4.26% per annum in the benchmark calibration to 1.55% and further to 0.54%. Stock market volatility also falls from 11.8% to 9.5% and further to 8%.

Most important, risk aversion also affects quantities. Reducing  $\gamma$  from 10 to 7.5 and further to 5 lowers consumption volatility from 5.13% to 4.24% and further to 3.93%. The probability of consumption disasters falls from 5.83% to 4.28% and further to 3.82%, and the disaster size also drops somewhat. A lower discount rate (the equity premium plus the interest rate) raises the marginal benefit of hiring, stimulating employment. Consequently, the mean unemployment rate falls from 8.63% to 5.71% and further to 4.63%. Although the unemployment volatility remains stable, the vacancy and labor market tightness volatilities both fall by about one-third. As such, echoing Gourio (2012) and Hall (2017) but differing from Tallarini (2000), our results indicate the necessity to jointly study macro quantities and asset prices, which do not seem to be determined separately.

The intertemporal elasticity of substitution,  $\psi$ , governs the willingness of the representative investor to substitute consumption over time. A lower elasticity indicates stronger incentives for consumption smoothing. Consequently, reducing  $\psi$  from 2 to 1.5 and further to 1 lowers the consumption volatility from 5.13% per annum to 4.89% and further to 4.51%. The consumption disaster probability falls from 5.83% to 5.4% and further to 4.77%. The disaster size also drops somewhat. The lower consumption risks reduce the equity premium from 4.26% to 3.82% and further to 3.17%. The lower discount rate again raises the marginal benefit of hiring to reduce the unemployment rate to 7.9% and further to 6.87%. However, labor market volatilities remain largely unchanged.

Finally, the log utility ( $\gamma = \psi = 1$ ) implies lower consumption, output, and investment volatil-

ities, 3.83%, 5.21%, and 5.32% per annum, than the benchmark calibration with recursive utility, 5.13%, 6.43%, and 8.59%, respectively. Although the unemployment volatility is largely unaffected, the vacancy and labor market tightness volatilities both fall by about one-third. The equity premium drops from 4.26% to only 0.53%, and stock market volatility from 11.77% to 8.68%.

### 3.6.2 Labor Market Parameters

The flow value of unemployment,  $b$ , plays an important role in driving our results. Lowering its value from 0.91 to 0.85 is sufficient to reduce the unemployment rate from 8.63% to 3.45% and the unemployment volatility from 0.32 to 0.07. Intuitively, a lower  $b$  reduces wages and raises profits, stimulating hiring incentives. A lower  $b$  also enlarges the fundamental surplus allocated to the firm, dampening the unemployment volatility (Hagedorn and Manovskii 2008; Ljungqvist and Sargent 2017). This mechanism also reduces the consumption volatility from 5.13% per annum to 2.62% and the consumption disaster probability from 5.83% to 2.36%. The smaller consumption risks then reduce the equity premium to only 0.45% and stock market volatility to 7.33%.

The bargaining weight of workers,  $\eta$ , also plays an important role in driving our results. Raising  $\eta$  from 0.01 to 0.025 makes wages more sensitive to shocks. The wage elasticity to labor productivity rises from 0.26 to 0.37. Because wages become more cyclical, profits and dividends become less cyclical, and the equity premium falls to 3.98% per annum. In addition, because workers gain a larger fraction of bargaining surplus, the unemployment rate rises somewhat from 8.63% to 8.81%. However, business cycle and labor market volatilities are largely unchanged.

The results are relatively insensitive to the separation rate,  $s$ . Reducing  $s$  from 3.5% to 3.25% lowers the unemployment rate slightly from 8.63% to 8.51%. The impact on business cycle and labor market volatilities is also small. The equity premium rises slightly from 4.26% per annum to 4.41%, and stock market volatility from 11.77% to 11.91%. The results are also relatively insensitive to the curvature parameter in the matching function,  $\iota$ . Raising  $\iota$  from 1.25 to 1.35 makes the matching process less frictional. The unemployment rate falls slightly from 8.63% to 8.5%. The im-

pact on business cycle and labor market volatilities is also small. The equity premium rises slightly from 4.26% per annum to 4.3%, but stock market volatility falls slightly from 11.77% to 11.72%.

Raising the unit cost of vacancy posting,  $\kappa$ , from 0.01 to 0.025 increases the marginal cost of hiring, causing the unemployment rate to rise from 8.63% to 8.9%. The consumption, output, and investment volatilities all go up, but labor market volatilities remain largely unchanged. The equity premium falls somewhat from 4.26% per annum to 4.02%, but stock market volatility remains stable. From equation (18), a higher  $\kappa$  makes wages more sensitive to procyclical labor market tightness,  $\theta_t$ . Consequently, profits and dividends become less procyclical, dampening the equity premium.

### 3.6.3 Technology Parameters

The supply elasticity of capital,  $\nu$ , governs the magnitude of capital adjustment costs. A rising  $\nu$  from 1.25 to 1.5 means falling adjustment costs, which in turn imply a stronger mechanism of consumption smoothing via investment. Consequently, the consumption volatility falls from 5.13% per annum to 4.98%, but the investment volatility rises from 8.59% to 9.41%, even though the output volatility remains largely unchanged at 6.45% (6.43% in the benchmark calibration). The lower consumption risks give rise to a lower equity premium, 4.03%, echoing Jermann (1998). A lower discount rate then raises the marginal benefit of hiring, reducing the unemployment rate to 8.54%. However, similar to the output volatility, labor market volatilities are largely unchanged.

Lowering the rate of capital depreciation,  $\delta$ , from 1.25% to 1% per month reduces the consumption volatility from 5.13% to 4.71% per annum and the consumption disaster probability from 5.83% to 5.26%. The output volatility also falls to 5.98%, and the investment volatility to 7.3%. The lower amount of consumption risk reduces the equity premium from 4.26% to 2.56%. The lower discount rate provides stronger hiring incentives and reduces the unemployment rate to 6.86%. Intuitively, a lower  $\delta$  gives rise to a larger stochastic steady state capital than the benchmark calibration, 18.2 versus 14.7. The larger capital stock helps stabilize the economy in the presence of shocks.<sup>23</sup>

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<sup>23</sup>This effect of  $\delta$  on the capital stock is distinct from the impact of the capital share. As note, we recalibrate the capital scalar,  $K_0$ , to keep the average labor share unchanged. Scaling by their respective  $K_0$  values still yields a



Raising the elasticity of capital-labor substitution,  $e = 1/(1 - \omega)$ , from 0.4 to 0.5 increases the business cycle and labor market volatilities. The consumption volatility rises from 5.13% per annum to 5.78%, and the consumption disaster probability from 5.83% to 6.31%. From the CES production function in equation (4),  $\partial Y_t/\partial X_t$  increases with  $\omega$  (and  $e$ ). The higher amount of consumption risk implies a higher equity premium of 4.72% and a higher stock market volatility of 12.13%. Finally, a higher discount rate in turn implies a higher unemployment rate of 9.06%.

Finally, we change the distribution parameter,  $\alpha$ , from 0.25 to 0.3. The average labor share falls to 0.7 in simulations. Although the stochastic steady state capital rises to 20.64, its value scaled by  $K_0$  remains at 1.07, which is identical to the benchmark calibration. Because of a smaller labor share, labor market frictions play a less prominent role in this economy. Consequently, the business cycle and labor market volatilities all fall. The consumption volatility declines to 4.26% per annum, and the consumption disaster probability to 5.1%. As a result of the lower consumption risk, the equity premium falls to only 2.27%, and stock market volatility to 9.15%. The lower discount rate raises the marginal benefit of hiring, reducing the unemployment rate to 7.2%.

## 4 Additional Predictions

In this section, we quantify several additional implications from the model, including the term structure of the equity premium (Section 4.1), the term structure of real interest rates (Section 4.2), the timing premium (Section 4.3), and the welfare cost of business cycles (Section 4.4).

### 4.1 The Term Structure of the Equity Premium

Binsbergen, Brandt, and Kojien (2012) show that short-maturity dividend strips on the aggregate stock market have higher expected returns and volatilities than long-maturity dividend strips. This downward-sloping pattern seems difficult to reconcile with leading consumption-based models.<sup>24</sup>

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slightly higher stochastic steady state capital for the low- $\delta$  economy than the benchmark economy, 1.1 versus 1.07.

<sup>24</sup>Intuitively, in the Campbell-Cochrane (1999) external habit model, the impact of shocks on slow-moving surplus consumption is more pronounced for long-maturity dividend strips than for short-maturity strips, giving rise to an upward-sloping term structure of equity returns. In the Bansal-Yaron (2004) long-run risks model, small shocks on highly persistent expected consumption growth and to stochastic consumption volatility gradually build up

Our model yields a downward-sloping equity term structure. Let  $P_{nt}^D$  denote the price of an  $n$ -period dividend strip. For  $n = 1$ ,  $P_{1t}^D = E_t[M_{t+1}D_{t+1}]$ . For  $n > 1$ , we solve for  $P_{nt}^D$  recursively from  $P_{nt}^D = E_t[M_{t+1}P_{n-1,t+1}^D]$ . We calculate  $r_{n,t+1}^D \equiv P_{n-1,t+1}^D/P_{nt}^D$  as the return of buying the  $n$ -period dividend strip at time  $t$  and selling it at  $t+1$ . However, as noted, dividends in the model are net pay-outs, which can be negative in certain states of the world. Negative prices on these dividend strips then render their returns undefined. In practice, dividends are all positive when  $n \geq 67$  months. As such, we calculate the equity term structure from year 6 to 40. In contrast, consumption in the model is always positive in all states of the world. Accordingly, we also calculate the term structure of consumption strips from year 1 to 40. The definitions of price of an  $n$ -period consumption strip,  $P_{nt}^C$ , and its return,  $r_{n,t+1}^C$ , are exactly analogous to those of the  $n$ -period dividend strip.

Figure 2 shows that risk premiums, volatilities, and Sharpe ratios on dividend and consumption strips are largely downward-sloping in our model. From Panel A, the dividend risk premium falls from 7.91% per annum in year 6 to 6.64% in year 10 and further to 1.26% in year 40. The volatility of the dividend strip falls from 22.54% in year 6 to 18.6% in year 10 and further to 3.86% in year 40 (Panel B). The Sharpe ratio of the dividend strip starts at 0.35 in year 6, rises slightly to 0.36 in year 10, and then falls steadily to 0.32 in year 40 (Panel C). For the consumption strip, the risk premium starts at 2.37% in year 1, rises to 2.52% in year 6, and then falls gradually to 0.59% in year 40 (Panel D). Its volatility starts at 6.82% in year 1, rises to 7.04% in year 4, and then drops to 2.49% in year 40 (Panel E). The Sharpe ratio starts at 0.348 in year 1, rises slightly to 0.358 in year 8, and falls to 0.237 in year 40 (Panel F). Finally, for the wealth portfolio that pays the consumption stream as its dividends, its risk premium is 2.23%, and its volatility 5.17%.

Intuitively, short-maturity dividend and consumption strips are riskier in our model because of their higher exposures to disaster risks. When the economy slides into a disaster, short-maturity

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over longer horizons to make long-maturity dividend strips riskier than short-maturity strips, again yielding an upward-sloping equity term structure. In the Rietz-Barro baseline disaster model, dividend strips of all maturities are exposed to the same amount of disaster risks, which are specified to be i.i.d., yielding a flat equity term structure. Finally, in the Wachter (2013) model with time-varying, but highly persistent disaster probabilities, small shocks on the disaster probabilities build up over time to yield an upward-sloping equity term structure.

dividends and consumption take a big hit because of inertial wages. Long-maturity dividend and consumption strips are less impacted because disasters are followed by subsequent recoveries.<sup>25</sup>

## 4.2 The Term Structure of Real Interest Rates

We calculate the prices of real zero-coupon bonds for maturities ranging from 1 month to 10 years. Let  $P_{nt}$  denote the price of an  $n$ -period zero-coupon bond. For  $n = 1$ ,  $P_{1t} = E_t[M_{t+1}]$ . For  $n > 1$ , we solve for  $P_{nt}$  recursively from  $P_{nt} = E_t[M_{t+1}P_{n-1,t+1}]$ . The log yield-to-maturity is  $y_{nt} \equiv -\log(P_{nt})/n$ . Let  $r_{n,t+1} \equiv P_{n-1,t+1}/P_{nt}$  be the return of buying the  $n$ -period zero-coupon bond at time  $t$  and selling it at  $t+1$ . Excess returns are in excess of the 1-month interest rate,  $r_{n,t+1} - r_{ft+1}$ .

To calculate the term structure, we simulate one million months from the model's stationary distribution. The real yield curve is downward sloping in the model. The yield-to-maturity starts at 1.53% per annum for 1-month zero-coupon bond but falls to 1.29% for 1-year, 0.95% for 5-year, and further to 0.72% for 10-year zero-coupon bond. The average yield spread is  $-0.81\%$  for the 10-year zero-coupon bond relative to the 1-month bond. The real term premium is also negative,  $-1.11\%$ , for the 10-year zero-coupon bond. Intuitively, long-term bonds earn lower average returns because these bonds are hedges against disaster risks. Disasters stimulate precautionary savings, which in turn drive down real interest rates and push up real bond prices. Because the prices of long-term bonds tend to rise at the onset of disasters, these bonds provide hedges against disaster risks and, consequently, earn lower average returns (Nakamura et al. 2013; Wachter 2013).

Evidence on the slope of the real yield curve seems mixed. A large and liquid market for inflation-indexed bonds (index-linked gilts) has existed in the UK since 1982. Evans (1998) and Piazzesi and Schneider (2007) document that real yield curve is downward sloping in the U.K. In the U.S., Treasury inflation-protected securities (TIPS) start trading in 1997. Piazzesi and Schneider show that the TIPS yield curve appears to be upward sloping but caution that interpreting the evidence

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<sup>25</sup>Nakamura et al. (2013) show that a model with (exogenous) multiperiod disasters and subsequent recoveries also yields a downward-sloping equity term structure. Our work differs in that disasters and recoveries are endogenous.

might be complicated by the relatively short sample and poor liquidity in the TIPS market.<sup>26</sup>

### 4.3 The Timing Premium

Epstein, Farhi, and Strzalecki (2014) show that the representative investor in the Bansal-Yaron (2004) model would give up an implausibly high fraction, 31%, of its consumption stream for the early resolution of consumption risks. In the Wachter (2013) model with time-varying disaster probabilities, this fraction is even higher at 42%. Epstein et al. argue that the fractions (dubbed the timing premium) seem too high because the household cannot use the information from the early resolution to modify its risky consumption stream. Because we follow Bansal and Yaron when calibrating preference parameters, with risk aversion higher than the inverse of the elasticity of intertemporal substitution ( $10 > 1/2$ ), it is natural to ask what the timing premium is in our model.

The timing premium is defined as  $\pi \equiv 1 - J_0/J_0^*$ , in which  $J_0$  is the household's utility with risks resolved gradually, and  $J_0^*$  is the utility with risks resolved in the next period. Formally,

$$J_0^* = \left[ (1 - \beta)C_0^{1-\frac{1}{\psi}} + \beta (E_t [(J_1^*)^{1-\gamma}])^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}}, \quad (27)$$

in which the continuation utility  $J_1^*$  is given by

$$J_1^* = \left[ (1 - \beta) \sum_{t=1}^{\infty} \beta^{t-1} C_t^{1-\frac{1}{\psi}} \right]^{\frac{1}{1-1/\psi}}. \quad (28)$$

Following Epstein, Farhi, and Strzalecki (2014), we calculate  $J_0^*$  via Monte Carlo simulations, with the economy's stochastic steady state ( $N_t = 0.9137$ ,  $K_t = 14.6909$ , and  $x_t = 0.1887$ ) as the initial condition. Specifically, we simulate in total 100,000 sample paths, each with  $T = 2,500$  months, while pasting  $J_0$  as the continuation value at  $T$ .  $J_0$  is available from our projection algorithm. On each path, we calculate one realization of  $J_1^*$  using equation (28). The expectation in equation (27),  $E_t [(J_1^*)^{1-\gamma}]$ , is calculated as the cross-simulation average.

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<sup>26</sup>We wish to point out that the downward sloping real yield curve in our model does not necessarily contradict the upward sloping nominal yield curve in the data. Nominal bonds are subject to inflation risks, which are left outside our model. Because long-term bonds are more exposed to persistent inflation risks, a positive inflation risk premium would give rise to an upward sloping nominal yield curve. We leave such an extension of our model to future work.

The timing premium in our model is only 15.3%. We view this estimate to be empirically plausible. For comparison, Epstein, Farhi, and Strzalecki (2014) calculate the timing premium to be 9.5% with i.i.d. consumption growth, a risk aversion of 10, and an elasticity of intertemporal substitution of 1.5. In the Barro (2009) model with a constant disaster probability, a risk aversion of 4, and an elasticity of intertemporal substitution of 2, the timing premium is 18%.

Intuitively, the long-run risks model assumes extremely high persistence in expected consumption growth (Bansal and Yaron 2004) or in conditional consumption volatility (Bansal, Kiku, and Yaron 2012). Analogously, the Wachter (2013) model assumes very high persistence in time-varying disaster probabilities. Because the risks are not resolved until much later, the investor that prefers early resolution of uncertainty would pay a high timing premium for the risks to be resolved early. In contrast, in our model, the expected consumption growth and conditional consumption volatility are much less persistent, as shown in equations (21) and (22), yielding a relatively low timing premium.

#### 4.4 The Welfare Cost of Business Cycles

Lucas (1987, 2003) argues that the welfare cost of business cycles is negligible. Assuming log utility for the representative household and log-normal distribution for consumption growth, Lucas (2003) calculates that the agent would sacrifice a mere 0.05% of their consumption in perpetuity to eliminate consumption fluctuations. However, Lucas assumes log utility that fails to explain the equity premium puzzle. Atkeson and Phelan (1994), for example, argue that welfare cost calculations should be carried out within models that at least roughly replicate how asset markets price consumption risks. Because our model replicates the equity premium, we quantify its implied welfare cost.

Following Lucas (1987, 2003), we define the welfare cost of business cycles as the permanent percentage of the consumption stream that the representative household would sacrifice to eliminate aggregate consumption fluctuations. Formally, let  ${}_tC \equiv \{C_t, C_{t+1}, \dots\}$  be the consumption stream starting at time  $t$ . For a given state of the economy,  $(N_t, K_t, x_t)$ , at date  $t$ , we calculate the

welfare cost, denoted  $\chi_t \equiv \chi(N_t, K_t, x_t)$ , implicitly from:

$$J({}_tC(1 + \chi_t)) = \bar{J}, \quad (29)$$

in which  $\bar{J}$  is the recursive utility derived from the constant consumption at the deterministic steady state,  $\bar{C}$ . We solve for  $\bar{J}$  by iterating on  $\bar{J} = \left[ (1 - \beta)\bar{C}^{1-\frac{1}{\psi}} + \beta\bar{J}^{1-\frac{1}{\psi}} \right]^{\frac{1}{1-\frac{1}{\psi}}}$ . Because the recursive utility  $J_t$  is linear homogeneous,  $J({}_tC(1 + \chi_t)) = (1 + \chi_t)J({}_tC)$ , solving for  $\chi_t$  yields:

$$\chi_t = \frac{\bar{J}}{J_t} - 1. \quad (30)$$

We calculate the welfare cost,  $\chi_t$ , on the state space,  $(N_t, K_t, x_t)$ . To evaluate its magnitude, we simulate one million months of  $\chi_t$  from the model's stationary distribution. The average welfare cost in simulations is 28.7%, which is more than 580 times of the Lucas estimate of 0.05%. The consumption in the stochastic steady state is 2.57% lower than the deterministic steady state consumption.

Perhaps more important, the welfare cost is time-varying and strongly countercyclical. In simulation, its median is 24.6%, and the 2.5th, 5th, and 25th percentiles are 17.5%, 18.2%, and 21.3%, whereas the 75th, 95th, and 97.5th percentiles are 31.3%, 54.9%, and 64.4%, respectively. Figure 3 shows the heatmap of the welfare cost against the productivity in simulations. The welfare cost is clearly countercyclical. Its correlations with productivity, output, unemployment, vacancy, and the investment rate are  $-0.77$ ,  $-0.96$ ,  $0.92$ ,  $-0.66$ , and  $-0.47$ , respectively. The countercyclicality of the welfare cost imply that optimal fiscal and monetary policies aimed to dampen disaster risks are even more important than what the average welfare cost of 28.7% would suggest.

## 5 Conclusion

Labor market frictions are crucial for explaining the equity premium puzzle in general equilibrium. A dynamic stochastic general equilibrium economy with recursive utility, search frictions, and capital accumulation yields a high equity premium of 4.26% per annum and a low average interest rate

of 1.59%, while simultaneously obtaining plausible quantity dynamics. The equity premium and stock market volatility are both countercyclical, and the real interest rate and consumption growth are largely unpredictable. The welfare cost of business cycles is huge, 28.7%. Wage inertia plays a key role by amplifying the procyclical dynamics of profits, which in turn overcome the procyclical dynamics of investment and vacancy costs to make dividends endogenously procyclical.

Several directions arise for future research. First, one can embed our model into a New Keynesian framework to examine the nominal yield curve and the interaction between the equity premium and fiscal and monetary policies. Second, one can extend our model to a multi-country setting to study international asset prices and business cycles. Finally, one can incorporate heterogeneous firms to study how the cross-sectional distribution impacts on aggregate quantities and asset prices.

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## A Computational Algorithm

We adapt the globally nonlinear projection method with parameterized expectations in Petrosky-Nadeau and Zhang (2017) to our more general setting.

We approximate the  $x_t$  process with the discrete state space method of Rouwenhorst (1995) with 17 grid points, which are sufficient to cover the values of  $x_t$  within four unconditional standard deviations from its unconditional mean,  $\bar{x}$ . The Rouwenhorst grid is symmetric around  $\bar{x}$ . The grid is also even-spaced, with the distance between any two adjacent grid points,  $d_x$ , given by:

$$d_x \equiv 2\sigma/\sqrt{(1-\rho^2)(n_x-1)}, \quad (\text{A.1})$$

in which  $\rho$  is the persistence,  $\sigma$  the conditional volatility of  $x_t$ , and  $n_x = 17$ . We still need to construct the transition matrix,  $\Pi$ , in which the  $(i, j)$  element,  $\Pi_{ij}$ , is the probability of  $x_{t+1} = x_j$  conditional on  $x_t = x_i$ . To this end, we set  $p = (\rho + 1)/2$ , and:

$$\Pi^{(3)} \equiv \begin{bmatrix} p^2 & 2p(1-p) & (1-p)^2 \\ p(1-p) & p^2 + (1-p)^2 & p(1-p) \\ (1-p)^2 & 2p(1-p) & p^2 \end{bmatrix}, \quad (\text{A.2})$$

which is the transition matrix for  $n_x = 3$ . To obtain  $\Pi^{(17)}$ , we use the following recursion:

$$p \begin{bmatrix} \Pi^{(n_x)} & \mathbf{0} \\ \mathbf{0}' & 0 \end{bmatrix} + (1-p) \begin{bmatrix} \mathbf{0} & \Pi^{(n_x)} \\ 0 & \mathbf{0}' \end{bmatrix} + (1-p) \begin{bmatrix} \mathbf{0}' & 0 \\ \Pi^{(n_x)} & \mathbf{0} \end{bmatrix} + p \begin{bmatrix} 0 & \mathbf{0}' \\ \mathbf{0} & \Pi^{(n_x)} \end{bmatrix}, \quad (\text{A.3})$$

in which  $\mathbf{0}$  is a  $n_x \times 1$  column vector of zeros. We then divide all but the top and bottom rows by two to ensure that the conditional probabilities sum up to one in the resulting transition matrix,  $\Pi^{(n_x+1)}$ . Rouwenhorst (p. 306–307; p. 325–329) contains more details.

The state space of our model consists of employment, capital, and productivity,  $(N_t, K_t, x_t)$ . The goal is to solve for the indirect utility function,  $J(N_t, K_t, x_t)$ , the optimal vacancy function,  $V(N_t, K_t, x_t)$ , the multiplier function,  $\lambda(N_t, K_t, x_t)$ , and the optimal investment function,  $I(N_t, K_t, x_t)$ , from the following three functional equations:

$$J(N_t, K_t, x_t) = \left[ (1-\beta)C(N_t, K_t, x_t)^{1-\frac{1}{\psi}} + \beta \left( E_t [J(N_{t+1}, K_{t+1}, x_{t+1})^{1-\gamma}] \right)^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}} \quad (\text{A.4})$$

$$\begin{aligned} \frac{1}{a_2} \left( \frac{I(N_t, K_t, x_t)}{K_t} \right)^{1/\nu} &= E_t \left[ M_{t+1} \left[ \frac{Y(N_{t+1}, K_{t+1}, x_{t+1})}{K_{t+1}} \frac{\alpha (K_{t+1}/K_0)^\omega}{\alpha (K_{t+1}/K_0)^\omega + (1-\alpha)N_{t+1}^\omega} \right. \right. \\ &\left. \left. + \frac{1}{a_2} \left( \frac{I(N_{t+1}, K_{t+1}, x_{t+1})}{K_{t+1}} \right)^{1/\nu} (1-\delta + a_1) + \frac{1}{\nu-1} \frac{I(N_{t+1}, K_{t+1}, x_{t+1})}{K_{t+1}} \right] \right] \end{aligned} \quad (\text{A.5})$$

$$\begin{aligned} \frac{\kappa}{q(\theta_t)} - \lambda(N_t, K_t, x_t) &= E_t \left[ M_{t+1} \left[ \frac{Y(N_{t+1}, K_{t+1}, x_{t+1})}{N_{t+1}} \frac{(1-\alpha)N_{t+1}^\omega}{\alpha (K_{t+1}/K_0)^\omega + (1-\alpha)N_{t+1}^\omega} - W_{t+1} \right. \right. \\ &\left. \left. + (1-s) \left[ \frac{\kappa}{q(\theta(N_{t+1}, K_{t+1}, x_{t+1}))} - \lambda(N_{t+1}, K_{t+1}, x_{t+1}) \right] \right] \right] \end{aligned} \quad (\text{A.6})$$

in which

$$M_{t+1} = \beta \left[ \frac{C(N_{t+1}, K_{t+1}, x_{t+1})}{C(N_t, K_t, x_t)} \right]^{-\frac{1}{\psi}} \left[ \frac{J(N_{t+1}, K_{t+1}, x_{t+1})}{E_t[J(N_{t+1}, K_{t+1}, x_{t+1})^{1-\gamma}]^{\frac{1}{1-\gamma}}} \right]^{\frac{1}{\psi}-\gamma}. \quad (\text{A.7})$$

Also,  $V(N_t, K_t, x_t)$  and  $\lambda(N_t, K_t, x_t)$  must satisfy the Kuhn-Tucker conditions.

Following Petrosky-Nadeau and Zhang (2017), we deal with  $V_t \geq 0$  by exploiting a convenient mapping from the conditional expectation function,  $\mathcal{E}_t \equiv \mathcal{E}(N_t, K_t, x_t)$ , defined as the right-hand side of equation (A.6), to policy and multiplier functions to eliminate the need to parameterize the multiplier separately. After obtaining  $\mathcal{E}_t$ , we first calculate  $\tilde{q}(\theta_t) = \kappa_0 / (\mathcal{E}_t - \kappa_1)$ . If  $\tilde{q}(\theta_t) < 1$ , the  $V_t \geq 0$  constraint is not binding, we set  $\lambda_t = 0$  and  $q(\theta_t) = \tilde{q}(\theta_t)$ . We then solve  $\theta_t = q^{-1}(\tilde{q}(\theta_t))$ , in which  $q^{-1}(\cdot)$  is the inverse function of  $q(\theta_t)$ , and  $V_t = \theta_t(1 - N_t)$ . If  $\tilde{q}(\theta_t) \geq 1$ , the  $V_t \geq 0$  constraint is binding, we set  $V_t = 0$ ,  $\theta_t = 0$ ,  $q(\theta_t) = 1$ , and  $\lambda_t = \kappa_0 + \kappa_1 - \mathcal{E}_t$ . An advantage of the installation function,  $\Phi_t$ , is that when investment goes to zero, the marginal benefit of investment,  $\partial\Phi(I_t, K_t)/\partial I_t = a_2(I_t/K_t)^{-1/\nu}$ , goes to infinity. As such, the optimal investment is always positive, with no need to impose the  $I_t \geq 0$  constraint. We approximate  $I(N_t, K_t, x_t)$  directly.

We approximate  $J(N_t, K_t, x_t)$ ,  $I(N_t, K_t, x_t)$ , and  $\mathcal{E}(N_t, K_t, x_t)$  on each grid point of  $x_t$ . We use the finite element method with cubic splines on 50 nodes on the  $N_t$  space,  $[0.245, 0.975]$ , and 50 nodes on the  $K_t$  space,  $[5, 20]$ . We experiment to ensure that the bounds are not binding at a frequency higher than 0.01% in the model's simulations. We take the tensor product of  $N_t$  and  $K_t$  for each grid point of  $x_t$ . We use the Miranda-Fackler (2002) CompEcon toolbox for function approximation and interpolation. With three functional equations on the 17-point  $x_t$  grid, the 50-point  $N_t$  grid, and the 50-point  $K_t$  grid, we must solve a system of 127,500 nonlinear equations. we use such a large system to ensure the accuracy of our numerical solution. Following Judd et al. (2014), we use derivative-free fixed point iteration with a damping parameter of 0.00325. The convergence criterion is set to be  $10^{-4}$  for the maximum absolute value of the errors across the nonlinear functional equations.

**Table 1 : Basic Properties of the Real Consumption, Output, and Investment Growth and Asset Prices in the Historical Sample**

The historical cross-country panel is from the Jordà-Schularick-Taylor macrohistory database, except for Canada’s asset prices, which we obtain from the Dimson-Marsh-Staunton (2002) database purchased from Morningstar. All (annual) series end in 2015. In Panels A and B, the column “Sample” indicates the sample’s starting year. In Panels C and D, besides the starting year, the “Sample” column also reports the missing years in parentheses. For example, the real investment growth series for Australia starts in 1871 but is missing from 1947 to 1949. Other than Italy, which has missing asset prices from 1872 to 1884, in Panel D, all other missing years are in the 20th century. In Panel A,  $\bar{g}_C$ ,  $\sigma_C$ ,  $S_C$ ,  $K_C$ , and  $\rho_C^{(i)}$  denote the mean (in percent), volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation, for  $i = 1, 2, \dots, 5$ , of log real per capita consumption growth. In Panel B,  $\bar{g}_Y$ ,  $\sigma_Y$ ,  $S_Y$ ,  $K_Y$ , and  $\rho_Y^{(i)}$  denote the mean (in percent), volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation for log real per capita output growth. In Panel C,  $\bar{g}_I$ ,  $\sigma_I$ ,  $S_I$ ,  $K_I$ , and  $\rho_I^{(i)}$  denote the mean (in percent), volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation for log real per capita investment growth. Finally, in Panel D,  $E[\tilde{r}_S]$ ,  $\tilde{\sigma}_S$ , and  $E[\tilde{r}_S - r_f]$  are the average stock market return, stock market volatility, and the equity premium, respectively, without adjusting for financial leverage.  $E[r_S - r_f]$  and  $\sigma_S$  are the equity premium and stock market volatility, respectively, after adjusting for financial leverage.  $E[r_f]$  is the mean real interest rate, and  $\sigma_f$  the interest rate volatility. All asset pricing moments are in annual percent. We require nonmissing stocks, bonds, and bills.

	Panel A: Real consumption growth										Panel B: Real output growth									
	Sample	$\bar{g}_C$	$\sigma_C$	$S_C$	$K_C$	$\rho_C^{(1)}$	$\rho_C^{(2)}$	$\rho_C^{(3)}$	$\rho_C^{(4)}$	$\rho_C^{(5)}$	Sample	$\bar{g}_Y$	$\sigma_Y$	$S_Y$	$K_Y$	$\rho_Y^{(1)}$	$\rho_Y^{(2)}$	$\rho_Y^{(3)}$	$\rho_Y^{(4)}$	$\rho_Y^{(5)}$
Australia	1871	1.11	5.76	-0.77	6.35	-0.04	0.22	-0.03	0.03	-0.09	1871	1.45	4.11	-0.90	5.49	0.04	0.27	-0.10	-0.03	-0.05
Belgium	1914	1.35	8.72	-1.14	13.18	0.26	0.19	0.00	-0.40	-0.22	1871	1.63	7.45	1.26	19.01	0.33	0.05	0.00	0.03	-0.29
Canada	1872	1.77	4.62	-1.04	6.27	0.00	0.16	-0.16	-0.04	-0.14	1871	1.87	4.97	-0.78	5.11	0.26	0.11	-0.07	-0.15	-0.15
Denmark	1871	1.38	5.27	-0.83	11.44	-0.01	-0.41	0.06	0.18	-0.23	1871	1.68	3.66	-1.03	8.13	0.05	-0.17	0.08	0.08	-0.08
Finland	1871	2.07	5.54	-1.13	9.01	0.16	-0.08	0.02	-0.04	-0.23	1871	2.06	4.47	-0.78	7.15	0.25	-0.11	0.10	-0.12	-0.17
France	1871	1.37	6.57	-1.06	13.69	0.39	0.19	-0.06	-0.28	-0.14	1871	1.64	6.20	-0.60	10.30	0.09	-0.09	0.10	0.19	-0.09
Germany	1871	1.67	5.51	-0.57	7.11	0.25	0.24	0.28	-0.07	0.00	1871	1.62	10.66	-7.62	78.70	0.30	-0.04	-0.11	-0.16	-0.13
Italy	1871	1.47	3.63	0.14	7.62	0.38	0.32	0.10	0.08	0.11	1871	1.80	4.71	-1.32	13.34	0.27	-0.06	-0.03	0.14	0.01
Japan	1875	2.11	6.74	-1.53	20.90	0.21	0.10	0.18	0.20	0.20	1871	2.40	6.18	-2.23	15.50	0.27	0.03	0.16	0.09	0.01
Netherlands	1871	1.41	8.18	-0.83	19.86	0.17	0.13	-0.21	-0.21	-0.19	1871	1.54	6.75	0.97	32.58	0.25	-0.12	-0.02	-0.07	-0.16
Norway	1871	1.83	3.65	-0.32	12.65	-0.06	-0.34	0.26	0.07	-0.24	1871	2.10	3.53	-0.72	7.21	0.11	-0.08	0.12	0.06	-0.15
Portugal	1911	2.36	4.36	-0.49	3.30	0.22	0.23	-0.02	0.09	-0.16	1871	1.84	4.16	-0.01	4.23	0.01	0.18	0.02	0.18	0.04
Spain	1871	1.56	7.92	-2.20	17.20	0.00	-0.02	-0.13	-0.05	0.08	1871	1.86	4.98	-1.58	10.94	0.18	0.05	0.03	0.04	0.14
Sweden	1871	1.80	4.20	0.44	7.04	-0.15	-0.17	0.05	0.07	-0.20	1871	2.02	3.39	-1.32	7.30	-0.08	-0.04	0.02	0.18	-0.17
Switzerland	1871	1.22	5.85	0.35	7.34	-0.20	-0.10	-0.11	-0.10	0.04	1871	1.41	3.84	-0.41	4.02	0.13	-0.14	-0.05	0.09	0.05
UK	1871	1.33	2.76	-0.34	8.90	0.33	0.02	-0.06	-0.01	-0.11	1871	1.40	2.86	-0.89	5.62	0.35	0.03	-0.18	-0.22	-0.09
USA	1871	1.75	3.42	-0.07	3.99	0.08	0.09	-0.11	0.00	-0.10	1871	1.91	4.77	-0.08	4.83	0.25	0.08	-0.13	-0.19	-0.19
Mean		1.62	5.45	-0.67	10.34	0.12	0.04	0.00	-0.03	-0.09		1.78	5.10	-1.06	14.09	0.18	0.00	0.00	0.01	-0.09
Median		1.56	5.51	-0.77	8.90	0.16	0.10	-0.02	-0.01	-0.14		1.80	4.71	-0.78	7.30	0.25	-0.04	0.00	0.04	-0.09

Panel C: Real investment growth

Sample	$\bar{g}_I$	$\sigma_I$	$S_I$	$K_I$	$\rho_I^{(1)}$	$\rho_I^{(2)}$	$\rho_I^{(3)}$	$\rho_I^{(4)}$	$\rho_I^{(5)}$	
Australia	1871 (47–49)	1.60	13.56	-0.72	5.06	0.15	0.09	-0.07	-0.16	-0.07
Belgium	1901 (14–20, 40–46)	1.68	10.74	-0.20	3.44	-0.09	-0.06	-0.02	-0.23	0.14
Canada	1872	2.17	18.12	-0.18	10.68	0.27	0.02	-0.18	-0.19	-0.16
Denmark	1871 (15–22)	1.96	10.10	-0.52	6.63	0.21	-0.11	-0.05	0.00	-0.17
Finland	1871	2.40	13.24	-1.49	11.14	0.19	0.01	0.06	-0.27	-0.28
France	1871 (19–20, 45–46)	1.98	19.23	-1.33	16.16	-0.07	-0.31	-0.04	-0.08	0.15
Germany	1871 (14–20, 40–48)	2.69	14.42	-0.56	5.40	0.06	-0.01	-0.10	-0.11	-0.23
Italy	1871	2.50	12.42	1.82	23.10	0.11	-0.14	0.12	0.03	-0.08
Japan	1886 (45–46)	4.21	14.36	-0.77	13.61	0.14	-0.04	-0.07	0.00	0.08
Netherlands	1871 (14–21, 40–48)	1.78	8.23	-0.28	3.70	0.03	0.01	-0.15	-0.04	-0.21
Norway	1871 (40–46)	2.69	13.33	2.08	21.86	-0.13	-0.16	0.02	-0.04	-0.05
Portugal	1954	2.64	9.58	-0.22	3.08	0.22	0.21	0.06	-0.13	0.08
Spain	1871	2.85	13.23	-0.41	4.01	0.23	0.02	-0.23	-0.13	-0.12
Sweden	1871	2.65	12.43	0.10	4.88	0.07	-0.27	-0.08	0.01	-0.11
Switzerland	1871 (14–48)	2.58	11.02	0.69	5.33	0.37	0.17	-0.11	-0.33	-0.22
UK	1871	1.98	11.68	2.82	26.62	0.35	-0.14	-0.12	-0.03	-0.08
USA	1871	2.04	24.37	-1.71	18.02	0.17	-0.11	-0.32	-0.13	-0.02
Mean		2.38	13.53	-0.05	10.75	0.13	-0.05	-0.07	-0.11	-0.08
Median		2.40	13.23	-0.28	6.63	0.15	-0.04	-0.07	-0.11	-0.08

Panel D: Asset prices

Sample	$E[\tilde{r}_S]$	$\tilde{\sigma}_S$	$E[r_f]$	$\sigma_f$	$E[\tilde{r}_S - r_f]$	$E[r_S - r_f]$	$\sigma_S$	
Australia	1900 (45–47)	7.75	17.08	1.29	4.32	6.46	4.58	12.55
Belgium	1871 (14–19)	6.31	19.88	1.21	8.43	5.10	3.62	14.62
Canada	1900	7.01	17.00	1.60	4.79	5.41	3.84	12.26
Denmark	1875 (15)	7.47	16.43	3.08	5.68	4.39	3.12	11.91
Finland	1896	8.83	30.57	-0.74	10.93	9.57	6.80	22.98
France	1871 (15–21)	3.99	22.22	-0.47	7.78	4.45	3.16	16.75
Germany	1871 (23, 44–49)	8.83	27.59	-0.23	13.22	9.05	6.43	20.22
Italy	1871 (1872–84, 15–21)	6.63	27.21	0.58	10.50	6.05	4.29	20.41
Japan	1886 (46–47)	8.86	27.69	0.00	11.20	8.87	6.29	21.10
Netherlands	1900	6.96	21.44	0.78	4.91	6.19	4.39	15.32
Norway	1881	5.67	19.82	0.90	5.98	4.77	3.39	14.53
Portugal	1880	3.81	25.68	-0.01	9.43	3.82	2.71	19.29
Spain	1900 (36–40)	6.25	21.41	-0.04	6.90	6.29	4.47	15.94
Sweden	1871	8.00	19.54	1.77	5.60	6.23	4.42	14.26
Switzerland	1900 (15)	6.69	19.08	0.89	5.00	5.79	4.11	14.00
UK	1871	6.86	17.77	1.16	4.82	5.70	4.05	12.96
USA	1872	8.40	18.68	2.17	4.65	6.23	4.43	13.66
Mean		6.96	21.71	0.82	7.30	6.14	4.36	16.04
Median		6.96	19.88	0.89	5.98	6.05	4.29	14.62

**Table 2 : Basic Moments in the Model Under the Benchmark Calibration**

The model moments are based on 10,000 simulated samples, each with 1,740 months. On each artificial sample, we calculate the moments and report the mean as well as the 5th, 50th, and 95th percentiles across the 10,000 simulations.  $p$ -value is the fraction with which a model moment is higher than its data moment. The data moments are from Table 1. In Panel A,  $\sigma_C$ ,  $S_C$ ,  $K_C$ , and  $\rho_{C_i}$ , for  $i = 1, 2, \dots, 5$ , denote the volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation of the log consumption growth. The symbols in Panels B and C are defined analogously. In Panel D,  $E[U]$ ,  $S_U$ , and  $K_U$  are the mean, skewness, and kurtosis of monthly unemployment rates,  $\sigma_U$ ,  $\sigma_V$ , and  $\sigma_\theta$  are the volatilities of quarterly unemployment, vacancy, and labor market tightness, respectively.  $\rho_{UV}$  is the cross-correlation of quarterly unemployment and vacancy rates, and  $e_{w,y/n}$  the wage elasticity to labor productivity. In Panel E,  $E[r_S - r_f]$ ,  $E[r_f]$ ,  $\sigma_S$ , and  $\sigma_f$  are the average equity premium, average real interest rate, stock market volatility, and interest rate volatility, respectively, all of which are in annual percent.

	Data	Mean	5th	50th	95th	$p$		Data	Mean	5th	50th	95th	$p$
Panel A: Real consumption growth							Panel B: Real output growth						
$\sigma_C$	5.45	5.13	2.87	5.13	7.39	0.41	$\sigma_Y$	5.10	6.43	4.46	6.40	8.48	0.86
$S_C$	-0.67	0.03	-1.03	0.03	1.10	0.89	$S_Y$	-1.06	0.09	-0.62	0.08	0.81	0.99
$K_C$	10.34	8.09	4.38	7.30	14.44	0.18	$K_Y$	14.09	5.45	3.50	5.09	8.64	0.00
$\rho_{C1}$	0.12	0.21	-0.01	0.22	0.40	0.78	$\rho_{Y1}$	0.18	0.20	0.03	0.21	0.36	0.60
$\rho_{C2}$	0.04	-0.05	-0.26	-0.05	0.17	0.24	$\rho_{Y2}$	0.00	-0.06	-0.23	-0.06	0.12	0.31
$\rho_{C3}$	0.00	-0.04	-0.24	-0.04	0.16	0.35	$\rho_{Y3}$	0.00	-0.05	-0.22	-0.05	0.12	0.31
$\rho_{C4}$	-0.03	-0.04	-0.23	-0.04	0.15	0.44	$\rho_{Y4}$	0.01	-0.05	-0.21	-0.05	0.12	0.29
$\rho_{C5}$	-0.09	-0.04	-0.23	-0.04	0.14	0.67	$\rho_{Y5}$	-0.09	-0.05	-0.21	-0.05	0.12	0.65
Panel C: Real investment growth							Panel D: Labor market moments						
$\sigma_I$	13.53	8.59	5.29	8.61	11.83	0.00	$E[U]$	8.94	8.63	3.81	7.45	17.63	0.37
$S_I$	-0.05	0.31	-0.57	0.28	1.26	0.76	$S_U$	2.13	2.64	0.76	2.20	5.85	0.53
$K_I$	10.75	7.12	4.12	6.47	12.17	0.08	$K_U$	9.50	13.45	2.11	6.77	39.06	0.35
$\rho_{I1}$	0.13	0.15	-0.04	0.16	0.33	0.58	$\sigma_U$	0.24	0.32	0.16	0.32	0.48	0.76
$\rho_{I2}$	-0.05	-0.11	-0.29	-0.11	0.08	0.30	$\sigma_V$	0.19	0.34	0.23	0.32	0.49	1.00
$\rho_{I3}$	-0.07	-0.09	-0.27	-0.09	0.10	0.45	$\sigma_\theta$	0.62	0.34	0.23	0.32	0.50	0.01
$\rho_{I4}$	-0.11	-0.07	-0.25	-0.07	0.11	0.62	$\rho_{UV}$	-0.57	-0.07	-0.16	-0.07	0.01	1.00
$\rho_{I5}$	-0.08	-0.06	-0.24	-0.06	0.12	0.56	$e_{w,y/n}$	0.27	0.26	0.23	0.26	0.27	0.22
Panel E: Asset pricing moments													
$E[r_S - r_f]$	4.36	4.26	3.52	4.12	5.49	0.34							
$E[r_f]$	0.82	1.59	0.07	1.83	2.26	0.87							
$\sigma_S$	16.04	11.77	9.19	11.74	14.46	0.00							
$\sigma_f$	7.30	3.13	1.13	3.05	5.37	0.00							



**Table 3 : Disaster Moments in the Data and in the Model**

The data moments are obtained by applying the Barro-Ursúa (2008) peak-to-trough method on the Jordà-Schularick-Taylor cross-country panel. We adjust for trend growth in the data (no growth in our model). We subtract each log annual consumption growth observation with its mean of 1.62% and subtract each log annual output growth with the mean of 1.78% in the historical panel. For model moments, we simulate 10,000 artificial samples from the model's stationary distribution under the benchmark calibration, each with 1,740 months, matching the number of years, 145, from 1871 to 2015. On each artificial sample, we time-aggregate consumption and output into annual observations and apply the peak-to-trough method to identify disasters as cumulative fractional declines of consumption or output of at least 10% or 15%. We report the mean, 5th, 50th, and 95th percentiles across the simulations. If no disaster appears in an artificial sample, we set its disaster probability to zero and calculate the model's disaster probability moments across all the 10,000 simulations. However, we calculate disaster size and duration across samples with at least one disaster. The disaster probability and size are in percent, and duration in the number of years.

	Data	Mean	5th	50th	95th	$p$	Data	Mean	5th	50th	95th	$p$
	Disaster hurdle = 10%						Disaster hurdle = 15%					
Panel A: Consumption disasters												
Probability	6.40	5.83	1.55	5.31	11.32	0.37	3.51	3.64	0.71	3.20	7.69	0.45
Size	23.16	23.41	14.52	22.83	33.84	0.48	30.36	29.51	18.81	28.49	43.31	0.38
Duration	4.19	4.10	2.80	4.00	5.80	0.40	4.50	4.49	3.00	4.33	6.81	0.39
Panel B: Output disasters												
Probability	5.78	10.9	6.14	10.58	16.48	0.97	2.62	6.10	2.33	5.88	10.68	0.94
Size	22.34	22.31	15.91	21.89	30.13	0.46	32.9	28.50	20.07	27.88	38.86	0.20
Duration	4.14	3.73	2.89	3.67	4.78	0.23	5.04	4.25	3.00	4.17	5.75	0.15

**Table 4 : Predicting Excess Returns and Consumption Growth with Log Price-to-consumption in the Historical Sample**

The cross-country panel is from the Jordà-Schularick-Taylor macrohistory database, except for Canada. The annuals series start as early as 1870 and end in 2015 (the Internet Appendix). Panel A performs predictive regressions of stock market excess returns on log price-to-consumption,  $\sum_{h=1}^H [\log(r_{St+h}) - \log(r_{ft+h})] = a + b \log(P_t/C_t) + u_{t+H}$ , in which  $H$  is the forecast horizon,  $r_{St+1}$  the real stock market return,  $r_{ft+1}$  the real interest rate,  $P_t$  the real stock market index, and  $C_t$  real consumption.  $r_{St+1}$  and  $r_{ft+1}$  are over the course of period  $t$ , and  $P_t$  and  $C_t$  are at the beginning of period  $t$  (the end of period  $t - 1$ ). Excess returns are adjusted for a financial leverage ratio of 0.29. Panel B performs long-horizon predictive regressions of log consumption growth on  $\log(P_t/C_t)$ ,  $\sum_{h=1}^H \log(C_{t+h}/C_t) = c + d \log(P_t/C_t) + v_{t+H}$ . In both regressions,  $\log(P_t/C_t)$  is standardized to have a mean of zero and a standard deviation of one.  $H$  ranges from one year (1y) to five years (5y). The  $t$ -values of the slopes are adjusted for heteroscedasticity and autocorrelations of  $2(H - 1)$  lags. The slopes and  $R$ -squares are in percent.

	Slopes					$t$ -values					$R$ -squares				
	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y
Panel A: Predicting stock market excess returns															
Australia	-1.42	-2.49	-2.92	-3.53	-3.77	-1.97	-1.96	-1.80	-1.74	-1.62	1.80	3.14	3.56	4.20	4.29
Belgium	-1.30	-3.26	-4.79	-5.48	-5.16	-0.82	-0.98	-1.00	-0.91	-0.76	0.58	1.62	2.47	2.58	2.01
Denmark	-0.81	-1.94	-2.87	-3.74	-4.24	-0.85	-1.18	-1.43	-1.81	-2.14	0.50	1.35	2.13	3.04	3.76
Finland	-1.38	-3.79	-5.40	-6.40	-7.36	-0.77	-1.05	-1.06	-1.07	-1.22	0.55	1.78	2.55	3.05	3.78
France	-0.12	-0.34	-0.52	-0.63	-0.43	-0.11	-0.18	-0.21	-0.20	-0.11	0.01	0.03	0.05	0.05	0.02
Germany	-1.04	-2.11	-2.06	-1.54	0.13	-0.75	-0.91	-0.54	-0.28	0.02	0.19	0.34	0.21	0.08	0.00
Italy	-0.36	-0.58	-0.36	-0.07	0.38	-0.25	-0.22	-0.10	-0.01	0.07	0.04	0.05	0.01	0.00	0.01
Japan	-0.70	-1.40	-1.60	-1.73	-1.77	-0.45	-0.56	-0.45	-0.41	-0.36	0.19	0.36	0.35	0.30	0.24
Netherlands	-3.03	-6.45	-8.88	-11.06	-13.35	-1.68	-1.88	-2.11	-2.48	-2.98	4.15	9.00	12.73	16.34	20.25
Norway	-1.77	-3.59	-5.13	-6.52	-7.92	-1.55	-2.07	-2.41	-2.76	-3.24	1.75	3.61	5.60	7.68	9.84
Portugal	-0.24	-2.39	-3.87	-3.41	0.53	-0.08	-0.39	-0.50	-0.37	0.06	0.02	0.55	0.83	0.48	0.01
Spain	-1.02	-2.77	-4.90	-6.80	-8.13	-0.74	-0.92	-1.21	-1.66	-2.38	0.59	1.68	3.13	4.42	5.25
Sweden	-1.56	-3.81	-6.04	-8.31	-10.50	-1.63	-2.29	-2.91	-3.19	-3.20	1.42	3.74	6.47	9.64	13.08
Switzerland	-3.09	-6.51	-8.50	-10.67	-12.95	-1.70	-2.30	-2.85	-3.89	-4.17	4.02	8.50	11.76	15.72	20.05
UK	-2.95	-5.64	-7.62	-8.91	-10.51	-2.33	-4.92	-5.43	-5.84	-5.92	6.35	12.49	18.14	23.18	28.03
USA	-3.50	-7.45	-9.89	-12.98	-15.75	-3.83	-4.50	-4.35	-4.59	-5.16	7.71	16.13	21.01	27.48	33.59
Mean	-1.52	-3.41	-4.71	-5.74	-6.30	-1.22	-1.64	-1.77	-1.95	-2.07	1.87	4.02	5.69	7.39	9.01
Median	-1.34	-3.01	-4.84	-5.94	-6.26	-0.83	-1.11	-1.32	-1.70	-1.88	0.59	1.73	2.84	3.63	4.03
Panel B: Predicting consumption growth															
Australia	0.75	0.98	1.14	1.50	1.85	1.40	0.88	0.65	0.67	0.71	1.69	1.52	1.21	1.49	1.75
Belgium	-1.03	-1.38	-0.94	-0.68	-0.10	-0.91	-0.73	-0.41	-0.26	-0.04	1.41	1.05	0.30	0.11	0.00
Denmark	0.23	0.32	0.28	0.24	0.20	0.71	0.73	0.52	0.40	0.29	0.18	0.18	0.13	0.08	0.05
Finland	-0.91	-2.10	-2.90	-3.62	-4.07	-1.14	-1.46	-1.54	-1.67	-1.68	2.30	5.20	6.56	7.56	7.66
France	-0.84	-1.47	-2.02	-2.55	-3.18	-2.12	-1.81	-1.81	-1.85	-1.95	1.64	1.79	1.89	2.11	2.67
Germany	-0.95	-1.87	-2.88	-3.79	-4.70	-2.15	-1.85	-1.81	-1.74	-1.74	2.97	4.64	6.17	6.84	7.79
Italy	-0.60	-1.22	-1.74	-2.28	-2.91	-2.71	-2.21	-1.96	-1.87	-1.89	2.74	4.02	4.32	4.84	5.79
Japan	-1.76	-3.59	-5.38	-7.12	-8.78	-4.04	-3.35	-2.89	-2.60	-2.40	8.22	11.84	14.23	15.81	16.95
Netherlands	0.66	1.10	1.43	1.83	2.32	2.41	1.47	1.22	1.17	1.14	7.27	6.03	5.50	6.17	7.48
Norway	-0.35	-0.77	-1.21	-1.68	-2.10	-1.36	-1.80	-2.11	-2.40	-2.54	0.91	2.40	5.58	8.09	9.68
Portugal	-1.05	-2.20	-3.26	-4.08	-4.95	-2.18	-1.72	-1.67	-1.61	-1.53	4.82	8.98	10.91	11.55	11.55
Spain	-0.10	-0.18	-0.41	-0.67	-1.10	-0.14	-0.14	-0.27	-0.38	-0.55	0.02	0.02	0.08	0.17	0.40
Sweden	0.18	0.22	0.20	0.02	-0.17	0.56	0.44	0.28	0.02	-0.17	0.18	0.15	0.10	0.00	0.05
Switzerland	0.22	0.31	0.36	0.35	0.34	1.32	0.84	0.61	0.43	0.33	2.52	1.40	1.00	0.64	0.44
UK	-0.33	-0.89	-1.53	-2.32	-3.15	-1.78	-2.22	-2.77	-3.53	-4.16	1.44	3.94	7.06	11.86	17.32
USA	0.48	-0.09	-0.64	-1.05	-1.40	1.86	-0.18	-0.85	-1.08	-1.23	1.89	0.03	0.94	1.92	2.70
Mean	-0.34	-0.80	-1.22	-1.62	-1.99	-0.64	-0.82	-0.93	-1.02	-1.09	2.51	3.32	4.12	4.95	5.77
Median	-0.34	-0.83	-1.07	-1.36	-1.75	-1.02	-1.09	-1.20	-1.35	-1.38	1.79	2.09	3.10	3.48	4.25

**Table 5 : Predicting Volatilities of Stock Market Excess Returns and Consumption Growth with Log Price-to-consumption in the Historical Sample**

The cross-country panel is from the Jordà-Schularick-Taylor macrohistory database, except for Canada. The annuals series start in 1870 and end in 2015. For a given forecast horizon,  $H$ , we measure excess return volatility as  $\sigma_{St,t+H-1} = \sum_{h=0}^{H-1} |\epsilon_{St+h}|$ , in which  $\epsilon_{St+h}$  is the  $h$ -period-ahead residual from the first-order autoregression of excess returns,  $\log(r_{St+1}) - \log(r_{ft+1})$ . Excess returns are adjusted for a financial leverage ratio of 0.29. Panel A performs long-horizon predictive regressions of excess return volatilities,  $\log \sigma_{St+1,t+H} = a + b \log(P_t/C_t) + u_{t+H}^\sigma$ . Consumption growth volatility is  $\sigma_{Ct,t+H-1} = \sum_{h=0}^{H-1} |\epsilon_{Ct+h}|$ , in which  $\epsilon_{Ct+h}$  is the  $h$ -period-ahead residual from the first-order autoregression of log consumption growth,  $\log(C_{t+1}/C_t)$ . Panel B performs long-horizon predictive regressions of consumption growth volatilities,  $\log \sigma_{Ct+1,t+H} = c + d \log(P_t/C_t) + v_{t+H}^\sigma$ .  $\log(P_t/C_t)$  is standardized to have a mean of zero and a standard deviation of one.  $H$  ranges from one year (1y) to five years (5y). The  $t$ -values are adjusted for heteroscedasticity and autocorrelations of  $2(H-1)$  lags. The slopes and  $R$ -squares are in percent.

	Slopes					$t$ -values					$R$ -squares				
	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y
Panel A: Predicting stock market volatility															
Australia	20.04	16.84	15.73	16.20	15.82	1.89	1.91	1.81	1.81	1.80	2.15	3.55	4.28	5.51	6.55
Belgium	11.85	12.70	12.20	11.69	11.61	1.28	2.11	2.05	1.99	2.21	1.42	5.12	7.26	8.84	10.71
Denmark	-35.30	-37.64	-38.17	-37.40	-36.44	-3.70	-4.02	-3.95	-3.74	-3.43	7.90	16.11	21.11	24.13	25.79
Finland	6.94	3.22	5.56	5.49	3.54	0.66	0.45	0.97	1.02	0.65	0.42	0.23	1.26	1.56	0.76
France	-58.81	-60.73	-60.03	-58.54	-57.57	-6.19	-6.50	-5.93	-5.51	-5.17	20.49	37.29	42.82	45.17	46.37
Germany	-31.59	-35.33	-35.20	-34.06	-32.90	-2.89	-3.61	-3.42	-3.02	-2.67	5.44	12.60	16.61	17.96	18.71
Italy	-17.60	-23.51	-24.80	-24.34	-24.27	-1.92	-2.94	-2.86	-2.59	-2.41	2.45	8.22	12.62	15.43	17.69
Japan	8.99	7.32	9.12	10.91	11.75	0.80	0.74	0.94	1.15	1.26	0.48	0.72	1.89	3.41	4.74
Netherlands	7.49	8.46	11.28	10.93	8.97	0.50	0.67	1.03	1.18	1.15	0.48	1.43	4.60	5.52	5.30
Norway	-51.27	-54.63	-54.25	-53.32	-52.54	-5.44	-7.48	-7.26	-7.41	-7.81	20.22	39.57	51.02	56.54	60.54
Portugal	-50.20	-45.97	-44.35	-43.46	-39.43	-4.10	-3.57	-3.50	-3.56	-3.39	14.11	23.07	27.71	28.72	25.37
Spain	-37.40	-34.97	-34.23	-33.42	-32.51	-4.00	-5.24	-4.81	-4.51	-3.96	10.86	18.97	26.06	30.91	33.48
Sweden	-23.98	-22.89	-21.83	-21.84	-21.98	-2.75	-2.62	-2.16	-1.93	-1.79	4.88	8.45	9.78	10.82	11.85
Switzerland	7.05	11.57	9.51	11.11	11.03	0.39	0.87	0.90	1.18	1.30	0.27	2.01	3.01	5.79	7.64
UK	-35.31	-34.28	-33.22	-32.10	-31.62	-4.99	-4.69	-4.10	-3.58	-3.23	9.59	18.29	21.60	22.69	23.91
USA	0.30	5.54	6.58	7.08	8.06	0.03	0.87	1.57	2.13	2.51	0.00	0.65	1.77	2.89	4.86
Mean	-17.43	-17.77	-17.26	-16.57	-16.16	-1.90	-2.07	-1.80	-1.59	-1.44	6.32	12.27	15.84	17.87	19.02
Median	-20.79	-23.20	-23.32	-23.09	-23.12	-2.34	-2.78	-2.51	-2.26	-2.10	3.67	8.34	11.20	13.12	14.77
Panel B: Predicting consumption growth volatility															
Australia	3.23	-3.95	-3.07	-4.13	-5.52	0.28	-0.39	-0.27	-0.32	-0.40	0.06	0.18	0.14	0.28	0.55
Belgium	48.77	54.27	55.42	58.66	59.15	2.88	3.74	3.41	3.50	3.50	11.11	23.57	29.61	36.63	40.03
Denmark	-2.11	-1.62	0.21	0.64	1.13	-0.17	-0.15	0.02	0.05	0.09	0.02	0.03	0.00	0.01	0.03
Finland	32.87	35.10	38.93	40.82	41.42	2.38	2.84	3.27	3.61	3.79	6.84	16.21	25.65	30.35	33.31
France	84.04	78.92	77.39	76.70	76.69	9.11	9.59	9.25	8.72	8.35	37.34	53.32	60.94	65.91	68.76
Germany	11.37	11.62	13.29	14.96	16.28	1.14	0.98	0.95	0.96	0.95	0.77	1.42	2.15	3.01	3.75
Italy	6.73	7.80	8.51	9.88	11.70	0.78	1.01	1.06	1.15	1.30	0.36	0.89	1.60	2.71	4.48
Japan	37.88	39.76	39.78	39.88	39.93	3.66	3.72	3.54	3.26	3.07	8.50	15.96	21.30	23.11	24.82
Netherlands	7.04	7.92	9.68	9.26	8.42	0.60	0.73	0.85	0.89	0.90	0.58	1.51	3.20	3.47	3.56
Norway	3.69	5.69	4.34	3.81	3.63	0.34	0.50	0.37	0.33	0.32	0.09	0.38	0.28	0.27	0.29
Portugal	13.68	15.62	16.08	18.09	19.63	1.43	2.51	3.57	5.20	5.93	2.03	6.49	10.05	15.19	18.62
Spain	64.78	61.73	59.39	57.46	56.29	6.29	6.16	5.80	5.51	5.46	25.68	40.34	49.05	51.18	54.04
Sweden	-1.44	1.56	3.93	6.22	7.43	-0.14	0.17	0.39	0.57	0.64	0.01	0.03	0.26	0.79	1.32
Switzerland	-13.49	-13.67	-13.37	-9.64	-6.97	-1.01	-1.06	-1.11	-0.84	-0.69	1.40	2.71	3.78	2.63	1.61
UK	0.76	0.75	1.50	2.03	2.31	0.07	0.11	0.22	0.27	0.30	0.00	0.01	0.06	0.14	0.23
USA	-18.05	-19.66	-18.25	-17.46	-15.82	-1.89	-2.05	-1.87	-1.71	-1.45	2.44	5.14	6.30	6.70	6.07
Mean	17.49	17.62	18.36	19.20	19.73	1.61	1.78	1.84	1.95	2.00	6.08	10.51	13.40	15.15	16.34
Median	6.88	7.86	9.10	9.57	10.06	0.69	0.85	0.90	0.93	0.92	1.09	2.11	3.49	3.24	4.12

**Table 6 : Predicting Excess Returns, Consumption Growth, and Their Volatilities with Log Price-to-consumption in the Model**

The data moments are the mean estimates in Tables 4 and 5 on the Jordà-Schularick-Taylor database. For the model moments, we simulate 10,000 artificial samples from the model's stationary distribution (with a burn-in of 1,200 months), each with 1,740 months. On each artificial sample, we time-aggregate monthly market excess returns and consumption growth into annual observations and implement the exactly same procedures as in Tables 4 and 5. We report the mean, 5th, 50th, and 95th percentiles across the simulations as well as the  $p$ -value that is the fraction of simulations with which a given model moment is higher than its data moment. In all the long-horizon regressions, the log price-to-consumption ratio,  $\log(P_t/C_t)$ , is standardized to have a mean of zero and a standard deviation of one. The forecast horizon,  $H$ , ranges from one year (1y) to five years (5y). The  $t$ -values of the slopes are adjusted for heteroscedasticity and autocorrelations of  $2(H - 1)$  lags. The slopes and  $R$ -squares are in percent.

	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y
Panel A: Predicting stock market excess returns															
	Data					Mean					$p$				
$b$	-1.52	-3.41	-4.71	-5.74	-6.30	-1.82	-3.45	-4.91	-6.22	-7.40	0.33	0.50	0.47	0.42	0.34
$t$	-1.22	-1.64	-1.77	-1.95	-2.07	-2.36	-2.86	-3.17	-3.39	-3.57	0.09	0.09	0.08	0.08	0.09
$R^2$	1.87	4.02	5.69	7.39	9.01	3.86	6.83	9.40	11.59	13.52	0.77	0.76	0.78	0.77	0.76
	5th					50th					95th				
$b$	-2.96	-5.40	-7.61	-9.66	-11.55	-1.81	-3.41	-4.84	-6.13	-7.29	-0.74	-1.64	-2.41	-3.10	-3.64
$t$	-3.87	-4.49	-4.99	-5.33	-5.68	-2.33	-2.81	-3.10	-3.31	-3.48	-0.93	-1.36	-1.59	-1.71	-1.79
$R^2$	0.58	1.67	2.62	3.55	4.31	3.44	6.35	8.86	11.00	13.09	8.64	13.70	17.94	21.34	24.49
Panel B: Predicting consumption growth															
	Data					Mean					$p$				
$b$	-0.34	-0.80	-1.22	-1.62	-1.99	-1.27	-1.86	-2.44	-3.00	-3.52	0.01	0.06	0.09	0.12	0.13
$t$	-0.64	-0.82	-0.93	-1.02	-1.09	-2.69	-2.41	-2.49	-2.64	-2.79	0.01	0.07	0.10	0.13	0.13
$R^2$	2.51	3.32	4.12	4.95	5.77	7.34	7.20	8.44	9.86	11.27	0.88	0.74	0.70	0.68	0.68
	5th					50th					95th				
$b$	-2.02	-3.06	-4.09	-5.07	-6.03	-1.24	-1.83	-2.41	-2.95	-3.47	-0.61	-0.71	-0.83	-0.99	-1.12
$t$	-4.47	-4.57	-4.96	-5.41	-5.74	-2.63	-2.29	-2.32	-2.44	-2.60	-1.15	-0.69	-0.55	-0.53	-0.51
$R^2$	1.36	0.65	0.53	0.54	0.58	6.68	6.11	6.95	8.25	9.55	15.51	17.63	21.02	24.69	27.92
Panel C: Predicting excess return volatilities															
	Data					Mean					$p$				
$b$	-17.43	-17.77	-17.26	-16.57	-16.16	-15.94	-13.55	-12.03	-11.01	-10.15	0.55	0.68	0.75	0.78	0.81
$t$	-1.90	-2.07	-1.80	-1.59	-1.44	-1.48	-1.73	-1.84	-1.89	-1.88	0.64	0.62	0.49	0.41	0.37
$R^2$	6.32	12.27	15.84	17.87	19.02	2.12	3.30	4.54	5.61	6.34	0.06	0.02	0.02	0.03	0.04
	5th					50th					95th				
$b$	-36.81	-28.96	-25.35	-23.21	-21.78	-15.80	-13.46	-12.02	-10.95	-10.04	4.60	1.70	0.99	0.68	0.91
$t$	-3.43	-3.69	-3.90	-4.03	-4.06	-1.46	-1.72	-1.82	-1.85	-1.84	0.42	0.20	0.15	0.11	0.17
$R^2$	0.02	0.04	0.06	0.07	0.08	1.37	2.37	3.38	4.24	4.80	6.73	9.73	13.01	15.98	18.01
Panel D: Predicting consumption growth volatilities															
	Data					Mean					$p$				
$b$	17.49	17.72	18.36	19.20	19.73	-34.67	-32.89	-31.47	-30.14	-28.85	0.00	0.00	0.00	0.00	0.00
$t$	1.61	1.78	1.84	1.95	2.00	-3.36	-3.98	-4.03	-3.95	-3.82	0.00	0.00	0.00	0.00	0.00
$R^2$	6.08	10.51	13.40	15.15	16.34	7.69	13.16	15.89	17.19	17.73	0.58	0.62	0.60	0.57	0.54
	5th					50th					95th				
$b$	-56.53	-51.99	-49.84	-47.99	-46.64	-35.58	-34.16	-32.69	-31.32	-29.94	-8.95	-9.24	-8.75	-7.93	-7.04
$t$	-5.81	-6.88	-7.22	-7.23	-7.15	-3.39	-4.02	-4.01	-3.88	-3.72	-0.77	-0.98	-0.98	-0.96	-0.91
$R^2$	0.58	1.31	1.80	1.94	1.88	7.06	12.80	15.58	16.84	17.38	16.72	26.19	30.99	33.55	34.79

**Table 7 : Comparative Statics**

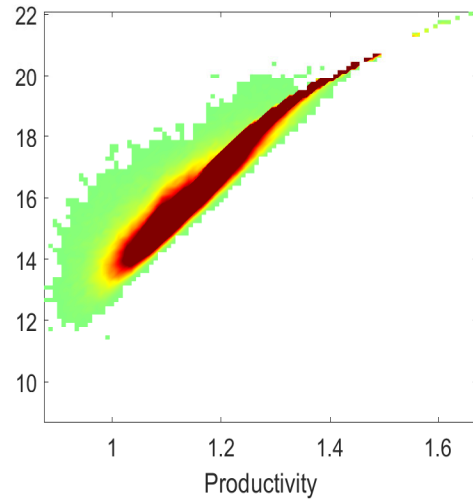
The first column of numbers shows the model moments from the benchmark calibration. The remaining columns show the model moments from 14 comparative statics.  $\gamma$  is relative risk aversion;  $\psi$  the intertemporal elasticity of substitution;  $b$  the flow value of unemployment;  $\eta$  the bargaining weight for workers;  $s$  the separation rate;  $\iota$  the curvature of the matching function;  $\kappa$  the unit cost of vacancy posting;  $\nu$  the adjustment cost parameter;  $\delta$  the capital depreciation rate;  $1/(1 - \omega)$  the elasticity of capital-labor substitution; and  $\alpha$  the distribution parameter. In each experiment, all the other parameters are identical to those in the benchmark calibration. For the model moments,  $\sigma_C$  is the consumption growth volatility per annum,  $\rho_{C1}$  the first-order autocorrelation of consumption growth, and  $\text{Prob}_C$ ,  $\text{Size}_C$ , and  $\text{Dur}_C$  the probability, size, and duration of consumption disasters with a cumulative decline hurdle rate of 10%.  $\sigma_Y$  is the output growth volatility,  $\rho_{Y1}$  the first-order autocorrelation of output growth, and  $\text{Prob}_Y$ ,  $\text{Size}_Y$ , and  $\text{Dur}_Y$  the probability, size, and duration of output disasters with a cumulative decline hurdle rate of 10%.  $\sigma_I$  is the investment growth volatility,  $\rho_{I1}$  the first-order autocorrelation of investment growth. The consumption, output, and investment volatilities, and the probability and size of consumption and output disasters are in percent. Their durations are in years.  $E[U]$  is mean unemployment rate,  $\sigma_U$ ,  $\sigma_V$ , and  $\sigma_\theta$  the quarterly volatilities of unemployment, vacancy, and labor market tightness, respectively,  $\rho_{UV}$  the cross-correlation of unemployment and vacancy, and  $e_{w,y/n}$  the wage elasticity to labor productivity. Finally,  $E[r_S - r_f]$  is the average equity premium,  $E[r_f]$  the average interest rate,  $\sigma_S$  stock market volatility, and  $\sigma_f$  the interest rate volatility, all of which are in annual percent.

	Benchmark	$\gamma$	$\gamma$	$\psi$	$\psi$	$\gamma, \psi$	$b$	$\eta$	$s$	$\iota$	$\kappa$	$\nu$	$\delta$	$\omega$	$\alpha$
		7.5	5	1.5	1	1	0.85	0.025	0.0325	1.35	0.025	1.5	0.01	-1	0.3
$\sigma_C$	5.13	4.24	3.94	4.89	4.51	3.83	2.62	5.19	5.17	5.09	5.24	4.98	4.71	5.78	4.26
$\rho_{C1}$	0.21	0.18	0.15	0.20	0.19	0.16	0.14	0.22	0.21	0.21	0.22	0.23	0.17	0.19	0.21
$\text{Prob}_C$	5.83	4.28	3.82	5.40	4.77	3.54	2.36	6.42	5.89	5.74	5.93	5.46	5.26	6.31	5.10
$\text{Size}_C$	23.41	20.69	19.36	22.68	21.68	19.70	13.80	22.65	23.36	23.23	23.70	23.68	21.34	25.04	20.27
$\text{Dur}_C$	4.10	4.46	4.46	4.16	4.29	4.52	4.98	4.12	4.12	4.11	4.10	4.21	4.12	3.95	4.34
$\sigma_Y$	6.43	5.58	5.17	6.23	5.91	5.21	4.11	6.37	6.45	6.40	6.52	6.45	5.98	6.97	5.62
$\rho_{Y1}$	0.20	0.18	0.16	0.20	0.19	0.17	0.15	0.21	0.21	0.20	0.21	0.21	0.17	0.20	0.20
$\text{Prob}_Y$	10.90	9.37	8.61	10.47	9.99	8.66	7.44	10.91	10.85	10.80	10.99	10.76	10.17	11.31	9.99
$\text{Size}_Y$	22.31	20.03	18.94	21.76	20.91	19.13	16.00	22.12	22.32	22.15	22.50	22.44	20.84	23.38	20.27
$\text{Dur}_Y$	3.73	3.84	3.88	3.74	3.78	3.88	4.00	3.73	3.73	3.73	3.72	3.75	3.72	3.66	3.81
$\sigma_I$	8.59	6.27	4.56	8.13	7.36	5.32	2.55	8.45	8.67	8.54	8.66	9.41	7.30	8.91	6.71
$\rho_{I1}$	0.15	0.13	0.11	0.15	0.14	0.11	0.09	0.16	0.16	0.15	0.16	0.15	0.14	0.16	0.15
$E[U]$	8.63	5.71	4.63	7.90	6.87	4.90	3.45	8.81	8.51	8.50	8.90	8.54	6.86	9.06	7.20
$\sigma_U$	0.32	0.35	0.35	0.33	0.34	0.34	0.07	0.31	0.33	0.32	0.32	0.32	0.35	0.36	0.30
$\sigma_V$	0.34	0.27	0.24	0.32	0.30	0.24	0.16	0.34	0.34	0.34	0.33	0.33	0.30	0.35	0.31
$\sigma_\theta$	0.34	0.27	0.25	0.32	0.30	0.24	0.16	0.34	0.34	0.34	0.34	0.33	0.31	0.35	0.31
$\rho_{UV}$	-0.07	-0.08	-0.09	-0.08	-0.08	-0.09	-0.30	-0.07	-0.07	-0.07	-0.08	-0.07	-0.08	-0.08	-0.08
$e_{w,y/n}$	0.26	0.26	0.26	0.26	0.26	0.26	0.27	0.37	0.26	0.26	0.26	0.26	0.26	0.25	0.26
$E[r_S - r_f]$	4.26	1.55	0.54	3.82	3.17	0.53	0.45	3.98	4.41	4.30	4.02	4.03	2.57	4.72	2.27
$E[r_f]$	1.59	2.45	2.75	1.58	1.54	2.68	2.82	1.67	1.49	1.51	1.83	1.62	2.26	1.38	2.29
$\sigma_S$	11.77	9.50	7.99	11.32	10.61	8.68	7.33	11.13	11.91	11.72	11.79	11.05	10.01	12.13	9.15
$\sigma_f$	3.13	2.27	1.78	3.74	4.60	3.32	0.64	2.95	3.09	3.25	2.81	3.11	2.36	3.46	2.23

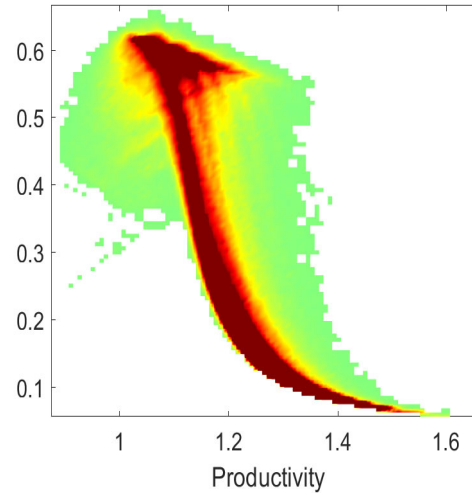
**Figure 1 : Heatmaps of Key Moments Against Productivity**

From the model's stationary distribution with the benchmark calibration (after a burn-in period of 1,200 monthly periods), we simulate a long sample path with one million months. The equity premium, stock market volatility, and consumption volatility are in percent.

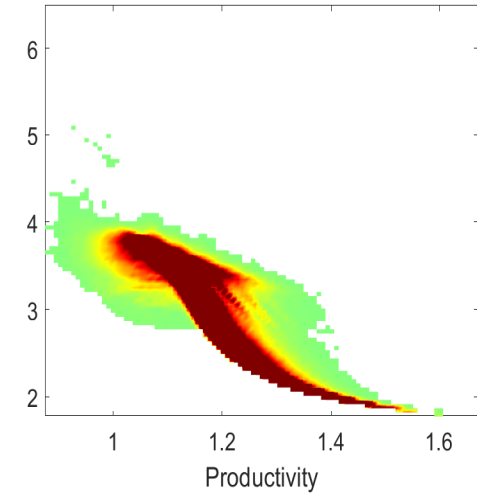
Panel A: Price-to-consumption,  $P_t/C_t$



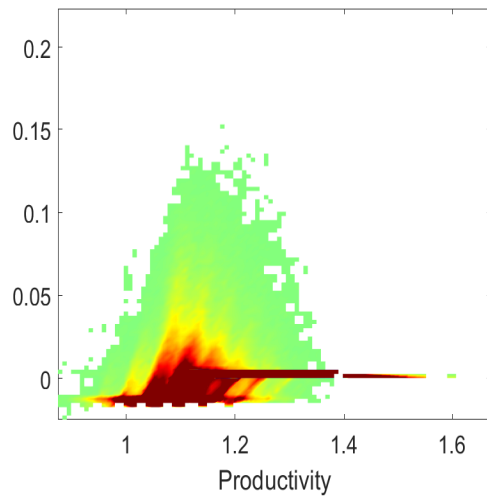
Panel B: The equity premium,  $E_t[r_{St+1} - r_{ft+1}]$



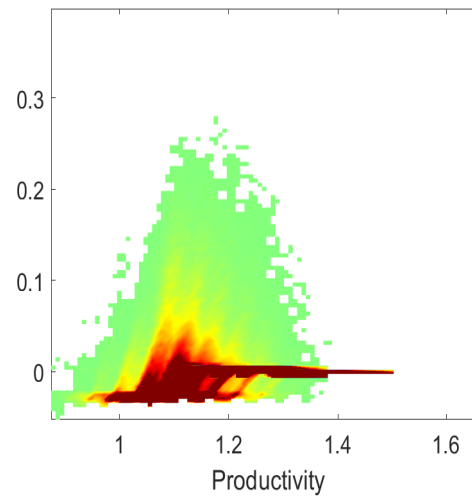
Panel C: Stock market volatility,  $\sigma_{St}$



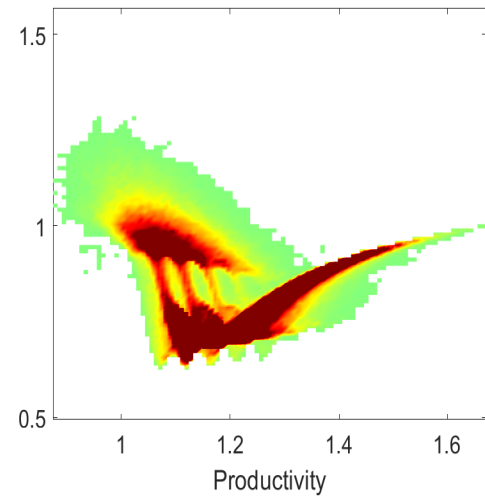
Panel D: The risk free rate,  $r_{ft+1}$



Panel E: Expected consumption growth,  $E_t[g_{Ct+1}]$



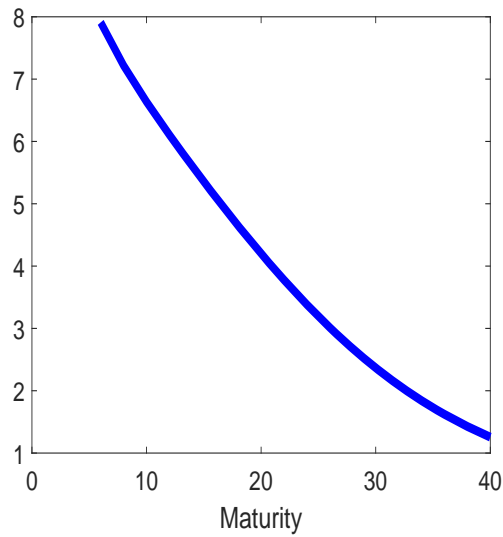
Panel F: Consumption volatility,  $\sigma_{Ct}$



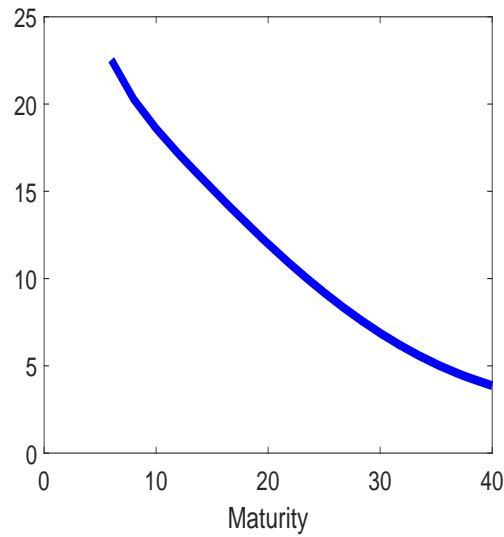
**Figure 2 : The Term Structure of the Equity Premium**

From the model's stationary distribution with the benchmark calibration (after a burn-in period of 1,200 monthly periods), we simulate a long sample path with one million months. Risk premiums and volatilities are in annualized percentage. Maturity is in years.

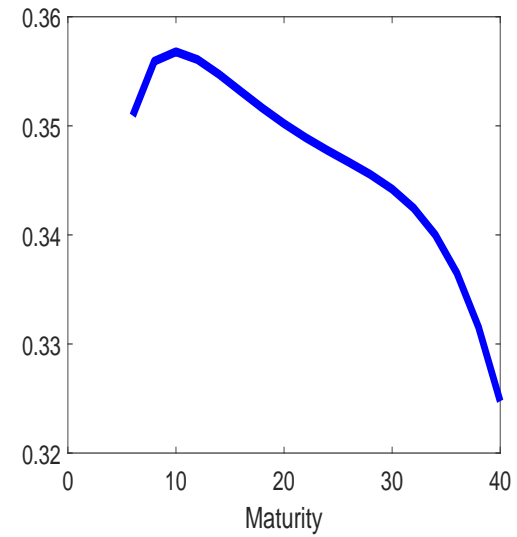
Panel A: Risk premium, dividend strip



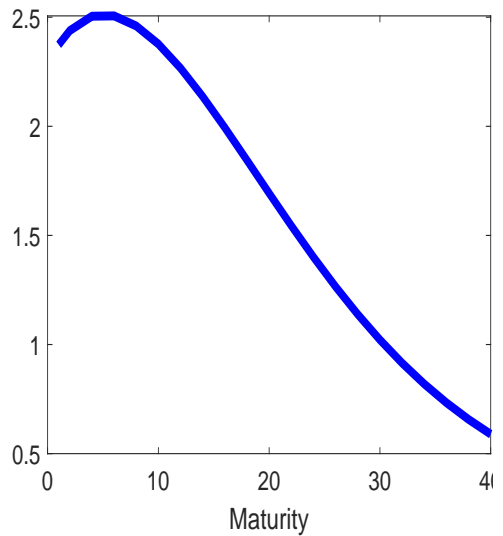
Panel B: Volatility, dividend strip



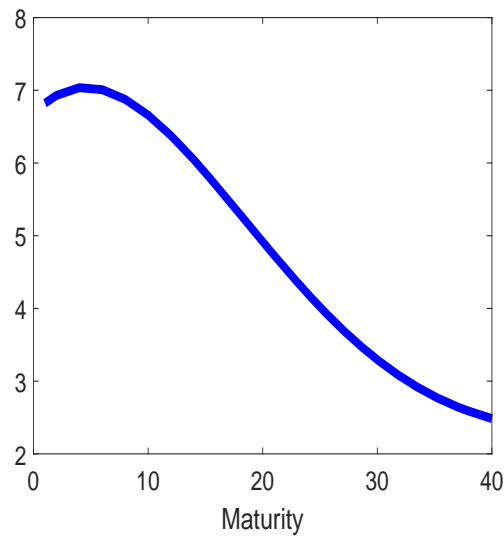
Panel C: Sharpe ratio, dividend strip



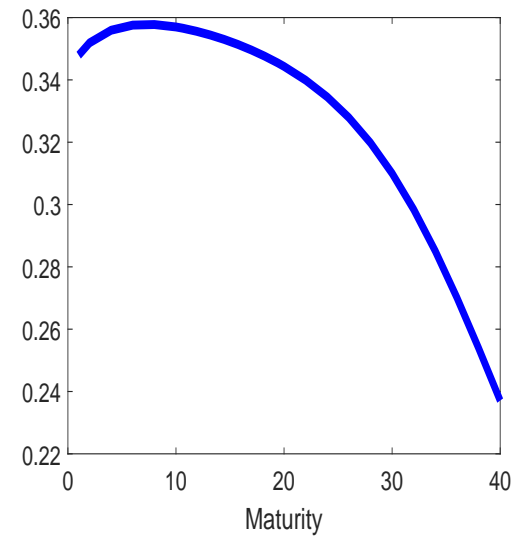
Panel D: Risk premium, consumption strip



Panel E: Volatility, consumption strip

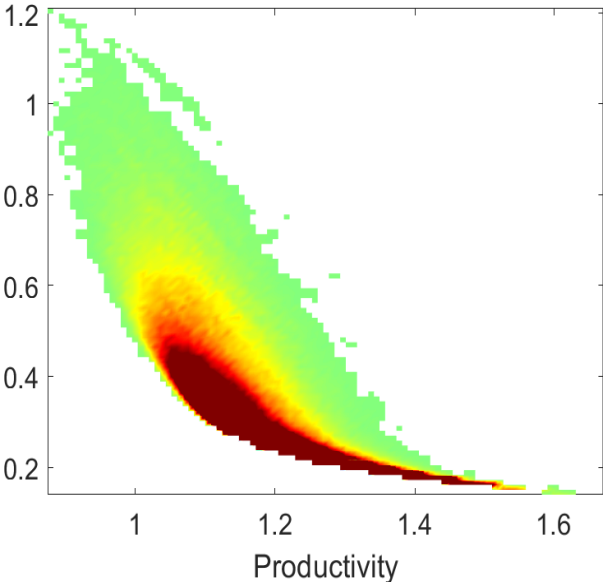


Panel F: Sharpe ratio, consumption strip



**Figure 3 : Heatmap of the Welfare Cost Against Productivity**

From the model's stationary distribution with the benchmark calibration (after a burn-in period of 1,200 monthly periods), we simulate a long sample path with one million months. The vertical axis is the welfare cost,  $\chi_t$ , and the horizontal axis is the productivity,  $\exp(x_t)$ .





# Internet Appendix (for Online Publication Only): “Searching for the Equity Premium”

## A Data

For each country, we construct its dividend index based on three series in the Jordà-Schularick-Taylor macrohistory database, including capital gain ( $P_t/P_{t-1}$ ), in which  $P_t$  is the nominal price level of a stock market index; dividend-to-price ( $D_t/P_t$ ), in which  $D_t$  is nominal dividends delivered by the index; and consumer price index. We first back out the  $P_t$  series by cumulating the capital gain series and then construct the  $D_t$  series by multiplying  $P_t$  with the dividend-to-price series. We scale nominal dividends by consumer price index to yield real dividends. The total number of nonmissing dividends between 1870 and 2015 in the Jordà-Schularick-Taylor dataset is 2,034. Three countries have in total seven dividend observations that equal zero, Germany, Portugal, and Spain. For Switzerland, the capital gain series runs from 1900 to 2015, with 1926–1959 missing. As such, its constructed dividends series starts in 1960. For Netherlands, both its capital gain and dividend-to-price series are missing from 1918 to 1949. As such, its dividends series starts in 1950.

In predicting market excess returns, consumption growth, and their volatilities, we drop Canada from Jordà-Schularick-Taylor macrohistory database. The reason is that its capital gain series (required to construct the price-to-consumption ratio) is incompatible with its total return series from the Dimson-Marsh-Staunton (2002) database. The implied dividend series are frequently negative, unlike the other countries, all of which have nonnegative dividends.

## B Derivations

### B.1 The Stock Return

Equation (4) implies that the marginal products of capital and labor are given by, respectively:

$$\frac{\partial Y_t}{\partial K_t} = \frac{Y_t}{K_t} \frac{\alpha (K_t/K_0)^\omega}{\alpha (K_t/K_0)^\omega + (1-\alpha)N_t^\omega}, \quad (\text{S1})$$

$$\frac{\partial Y_t}{\partial N_t} = \frac{Y_t}{N_t} \frac{(1-\alpha)N_t^\omega}{\alpha (K_t/K_0)^\omega + (1-\alpha)N_t^\omega}, \quad (\text{S2})$$

As such,  $Y_t$  is of constant returns to scale, i.e.,  $K_t \partial Y_t / \partial K_t + N_t \partial Y_t / \partial N_t = Y_t$ . From equation (9):

$$\frac{\partial \Phi_t}{\partial I_t} = a_2 \left( \frac{I_t}{K_t} \right)^{-\frac{1}{\nu}} \quad (\text{S3})$$

$$\frac{\partial \Phi_t}{\partial K_t} = a_1 + \frac{a_2}{\nu - 1} \left( \frac{I_t}{K_t} \right)^{1-\frac{1}{\nu}} \quad (\text{S4})$$

It follows that  $\Phi(I_t, K_t)$  is of constant returns to scale, i.e.,  $I_t \partial \Phi_t / \partial I_t + K_t \partial \Phi_t / \partial K_t = \Phi_t$ .

The Lagrangian for the firm's problem is:

$$\begin{aligned} \mathcal{L} = & \dots + Y_t - W_t N_t - \kappa V_t - I_t - \mu_{N_t} [N_{t+1} - (1-s)N_t - q(\theta_t)V_t] - \mu_{K_t} [K_{t+1} - (1-s)K_t - \Phi(I_t, K_t)] \\ & + \lambda_t q(\theta_t)V_t + E_t [M_{t+1} (Y_{t+1} - W_{t+1}N_{t+1} - \kappa V_{t+1} - I_{t+1} - \mu_{N_{t+1}} [N_{t+2} - (1-s)N_{t+1} - q(\theta_{t+1})V_{t+1}] \\ & - \mu_{K_{t+1}} [K_{t+2} - (1-s)K_{t+1} - \Phi(I_{t+1}, K_{t+1})] + \lambda_{t+1} q(\theta_{t+1})V_{t+1} + \dots)] \end{aligned} \quad (\text{S5})$$

The first-order conditions with respect to  $V_t$  and  $N_{t+1}$  are given by, respectively,

$$\mu_{N_t} = \frac{\kappa}{q(\theta_t)} - \lambda_t \quad (\text{S6})$$

$$\mu_{N_t} = E_t \left[ M_{t+1} \left[ \frac{\partial Y_{t+1}}{\partial N_{t+1}} - W_{t+1} + (1-s)\mu_{N_{t+1}} \right] \right] \quad (\text{S7})$$

Combining the two equations yields the intertemporal job creation condition in equation (14). The first-order conditions with respect to  $I_t$  and  $K_{t+1}$  are given by, respectively,

$$\mu_{K_t} = \frac{1}{\partial \Phi_t / \partial I_t} \quad (\text{S8})$$

$$\mu_{K_t} = E_t \left[ M_{t+1} \left[ \frac{\partial Y_{t+1}}{\partial K_{t+1}} + \left( 1 - \delta + \frac{\partial \Phi_{t+1}}{\partial K_{t+1}} \right) \frac{1}{\partial \Phi_{t+1} / \partial I_{t+1}} \right] \right] \quad (\text{S9})$$

Combining equations (S3)–(S9) yields equation (12).

We first show  $P_t = \mu_{K_t} K_{t+1} + \mu_{N_t} N_{t+1}$ , in which  $P_t = S_t - D_t$  is ex-dividend equity value, with a guess-and-verify approach (Goncalves, Xue, and Zhang 2020). We first assume it holds for  $t+1$ :  $P_{t+1} = \mu_{K_{t+1}} K_{t+2} + \mu_{N_{t+1}} N_{t+2}$ . We then show it also holds for  $t$ . It then follows that the equation must hold for all periods. We start with recursively formulating equation (11):  $P_t = E_t [M_{t+1} (P_{t+1} + D_{t+1})]$ . Using  $P_{t+1} = \mu_{K_{t+1}} K_{t+2} + \mu_{N_{t+1}} N_{t+2}$  to rewrite the right-hand side yields:

$$\begin{aligned} P_t &= E_t [M_{t+1} [\mu_{K_{t+1}} K_{t+2} + \mu_{N_{t+1}} N_{t+2} + D_{t+1}]] \\ &= E_t [M_{t+1} [\mu_{K_{t+1}} [(1-\delta)K_{t+1} + \Phi_{t+1}] + \mu_{N_{t+1}} [(1-s)N_{t+1} + q(\theta_{t+1})V_{t+1}] \\ & \quad + Y_{t+1} - W_{t+1}N_{t+1} - \kappa V_{t+1} - I_{t+1}]] \\ &= E_t \left[ M_{t+1} \left[ \mu_{K_{t+1}} \left[ (1-\delta)K_{t+1} + \frac{\partial \Phi_{t+1}}{\partial I_{t+1}} I_{t+1} + \frac{\partial \Phi_{t+1}}{\partial K_{t+1}} K_{t+1} \right] + \mu_{N_{t+1}} [(1-s)N_{t+1} + q(\theta_{t+1})V_{t+1}] \right. \right. \\ & \quad \left. \left. + \frac{\partial Y_{t+1}}{\partial K_{t+1}} K_{t+1} + \frac{\partial Y_{t+1}}{\partial N_{t+1}} N_{t+1} - W_{t+1}N_{t+1} - \kappa V_{t+1} - I_{t+1} \right] \right] \\ &= K_{t+1} E_t \left[ M_{t+1} \left[ \frac{\partial Y_{t+1}}{\partial K_{t+1}} + \left( 1 - \delta + \frac{\partial \Phi_{t+1}}{\partial K_{t+1}} \right) \mu_{K_{t+1}} \right] \right] + \mu_{K_{t+1}} \frac{\partial \Phi_{t+1}}{\partial I_{t+1}} I_{t+1} \\ & \quad + N_{t+1} E_t \left[ M_{t+1} \left[ \frac{\partial Y_{t+1}}{\partial N_{t+1}} - W_{t+1} + (1-s)\mu_{N_{t+1}} \right] \right] + \mu_{N_{t+1}} q(\theta_{t+1})V_{t+1} - \kappa V_{t+1} - I_{t+1} \\ &= \mu_{K_t} K_{t+1} + \mu_{N_t} N_{t+1}, \end{aligned} \quad (\text{S10})$$

in which the third equality follows from constant returns to scale for  $Y_{t+1}$  and  $\Phi_{t+1}$ , and the last

equality follows from equations (S6), (S7), (S8), (S9), and the Kuhn-Tucker condition (16).

To prove equation (17),

$$\begin{aligned}
r_{St+1} &= \frac{P_{t+1} + D_{t+1}}{P_t} = \frac{\mu_{Kt+1}K_{t+2} + \mu_{Nt+1}N_{t+2} + D_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} \\
&= \frac{\mu_{Kt+1}[(1-\delta)K_{t+1} + \Phi_{t+1}] + \mu_{Nt+1}[(1-s)N_{t+1} + q(\theta_{t+1})V_{t+1}] + Y_{t+1} - W_{t+1}N_{t+1} - \kappa V_{t+1} - I_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} \\
&= \frac{\mu_{Kt+1} \left[ (1-\delta)K_{t+1} + \frac{\partial \Phi_{t+1}}{\partial I_{t+1}} I_{t+1} + \frac{\partial \Phi_{t+1}}{\partial K_{t+1}} K_{t+1} \right] + \mu_{Nt+1} [(1-s)N_{t+1} + q(\theta_{t+1})V_{t+1}] + \frac{\partial Y_{t+1}}{\partial K_{t+1}} K_{t+1} + \frac{\partial Y_{t+1}}{\partial N_{t+1}} N_{t+1} - W_{t+1}N_{t+1} - \kappa V_{t+1} - I_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} \\
&= \frac{\left[ \frac{\partial Y_{t+1}}{\partial K_{t+1}} + \left(1 - \delta + \frac{\partial \Phi_{t+1}}{\partial K_{t+1}}\right) \mu_{Kt+1} \right] K_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} + \frac{\left[ \frac{\partial Y_{t+1}}{\partial N_{t+1}} - W_{t+1} + (1-s)\mu_{Nt+1} \right] N_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} \\
&= \frac{\mu_{Kt}K_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} r_{Kt+1} + \frac{\mu_{Nt}N_{t+1}}{\mu_{Kt}K_{t+1} + \mu_{Nt}N_{t+1}} r_{Nt+1}. \tag{S11}
\end{aligned}$$

## B.2 Wages

We extend the derivation in Petrosky-Nadeau, Zhang, and Kuehn (2018) to our setting with capital accumulation. Let  $\partial J_t / \partial N_t$  be the marginal value of an employed worker to the representative household,  $\partial J_t / \partial U_t$  the marginal value of an unemployed worker to the household,  $\phi_t$  the marginal utility of the household,  $\partial S_t / \partial N_t$  the marginal value of an employed worker to the representative firm, and  $\partial S_t / \partial V_t$  the marginal value of an unfilled vacancy to the firm. A worker-firm match turns an unemployed worker into an employed worker for the household as well as an unfilled vacancy into an employed worker for the firm. As such, the total surplus from the Nash bargain is:

$$H_t \equiv \left( \frac{\partial J_t}{\partial N_t} - \frac{\partial J_t}{\partial U_t} \right) / \phi_t + \frac{\partial S_t}{\partial N_t} - \frac{\partial S_t}{\partial V_t}. \tag{S12}$$

The equilibrium wage arises from the Nash worker-firm bargain as follows:

$$\max_{\{W_i\}} \left[ \left( \frac{\partial J_t}{\partial N_t} - \frac{\partial J_t}{\partial U_t} \right) / \phi_t \right]^\eta \left( \frac{\partial S_t}{\partial N_t} - \frac{\partial S_t}{\partial V_t} \right)^{1-\eta}, \tag{S13}$$

in which  $0 < \eta < 1$  is the worker's bargaining power. The outcome is the surplus-sharing rule:

$$\left( \frac{\partial J_t}{\partial N_t} - \frac{\partial J_t}{\partial U_t} \right) / \phi_t = \eta H_t = \eta \left[ \left( \frac{\partial J_t}{\partial N_t} - \frac{\partial J_t}{\partial U_t} \right) / \phi_t + \frac{\partial S_t}{\partial N_t} - \frac{\partial S_t}{\partial V_t} \right]. \tag{S14}$$

As such, the worker receives a fraction of  $\eta$  of the total surplus from the wage bargain.

### B.2.1 Workers

Tradeable assets consist of risky shares and a riskfree asset. Let  $r_{ft+1}$  denote the risk-free interest rate,  $\xi_t$  the household's financial wealth,  $\chi_t$  the fraction of the household's wealth invested in the risky shares,  $r_{\xi t+1} \equiv \chi_t r_{St+1} + (1 - \chi_t)r_{ft+1}$  the return on wealth, and  $T_t$  the taxes raised by the government. The household's budget constraint is given by:

$$\frac{\xi_{t+1}}{r_{\xi t+1}} = \xi_t - C_t + W_t N_t + U_t b - T_t. \quad (\text{S15})$$

The household's dividends income,  $D_t$ , is included in the current financial wealth,  $\xi_t$ .

Let  $\phi_t$  denote the Lagrange multiplier for the household's budget constraint (S15). The household's maximization problem is given by:

$$J_t = \left[ (1 - \beta)C_t^{1-\frac{1}{\psi}} + \beta \left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}} - \phi_t \left( \frac{\xi_{t+1}}{r_{\xi t+1}} - \xi_t + C_t - W_t N_t - U_t b + T_t \right), \quad (\text{S16})$$

The first-order condition for consumption yields:

$$\phi_t = (1 - \beta)C_t^{-\frac{1}{\psi}} \left[ (1 - \beta)C_t^{1-\frac{1}{\psi}} + \beta \left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}-1}, \quad (\text{S17})$$

which gives the marginal utility of consumption. Using  $N_{t+1} = (1 - s)N_t + f(\theta_t)U_t$  and  $U_{t+1} = sN_t + (1 - f(\theta_t))U_t$ , we differentiate  $J_t$  in equation (S16) with respect to  $N_t$ :

$$\begin{aligned} \frac{\partial J_t}{\partial N_t} &= \phi_t W_t + \frac{1}{1 - \frac{1}{\psi}} \left[ (1 - \beta)C_t^{1-\frac{1}{\psi}} + \beta \left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}-1} \\ &\quad \times \frac{1 - \frac{1}{\psi}}{1 - \gamma} \beta \left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1-1/\psi}{1-\gamma}-1} E_t \left[ (1 - \gamma) J_{t+1}^{-\gamma} \left[ (1 - s) \frac{\partial J_{t+1}}{\partial N_{t+1}} + s \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] \right]. \end{aligned} \quad (\text{S18})$$

Dividing both sides by  $\phi_t$ :

$$\frac{\partial J_t}{\partial N_t} / \phi_t = W_t + \frac{\beta}{(1 - \beta)C_t^{-\frac{1}{\psi}}} \left[ \frac{1}{\left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1}{1-\gamma}}} \right]^{\frac{1}{\psi}-\gamma} E_t \left[ J_{t+1}^{-\gamma} \left[ (1 - s) \frac{\partial J_{t+1}}{\partial N_{t+1}} + s \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] \right]. \quad (\text{S19})$$

Dividing and multiplying by  $\phi_{t+1}$ :

$$\begin{aligned}\frac{\partial J_t}{\partial N_t}/\phi_t &= W_t + E_t \left[ \beta \left( \frac{C_{t+1}}{C_t} \right)^{-\frac{1}{\psi}} \left[ \frac{J_{t+1}}{\left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1}{1-\gamma}}} \right]^{\frac{1}{\psi}-\gamma} \left[ (1-s) \frac{\partial J_{t+1}}{\partial N_{t+1}} + s \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] / \phi_{t+1} \right] \\ &= W_t + E_t \left[ M_{t+1} \left[ (1-s) \frac{\partial J_{t+1}}{\partial N_{t+1}} + s \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] / \phi_{t+1} \right].\end{aligned}\quad (\text{S20})$$

Similarly, differentiating  $J_t$  in equation (S16) with respect to  $U_t$  yields:

$$\begin{aligned}\frac{\partial J_t}{\partial U_t} &= \phi_t b + \frac{1}{1-\frac{1}{\psi}} \left[ (1-\beta) C_t^{1-\frac{1}{\psi}} + \beta \left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1-1/\psi}{1-\gamma}} \right]^{\frac{1}{1-1/\psi}-1} \\ &\quad \times \frac{1-\frac{1}{\psi}}{1-\gamma} \beta \left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1-1/\psi}{1-\gamma}-1} E_t \left[ (1-\gamma) J_{t+1}^{-\gamma} \left[ f(\theta_t) \frac{\partial J_{t+1}}{\partial N_{t+1}} + (1-f(\theta_t)) \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] \right].\end{aligned}\quad (\text{S21})$$

Dividing both sides by  $\phi_t$ :

$$\frac{\partial J_t}{\partial U_t}/\phi_t = b + \frac{\beta}{(1-\beta) C_t^{-\frac{1}{\psi}}} \left[ \frac{1}{\left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1}{1-\gamma}}} \right]^{\frac{1}{\psi}-\gamma} E_t \left[ J_{t+1}^{-\gamma} \left[ f(\theta_t) \frac{\partial J_{t+1}}{\partial N_{t+1}} + (1-f(\theta_t)) \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] \right].\quad (\text{S22})$$

Dividing and multiplying by  $\phi_{t+1}$ :

$$\begin{aligned}\frac{\partial J_t}{\partial U_t}/\phi_t &= b + E_t \left[ \beta \left( \frac{C_{t+1}}{C_t} \right)^{-\frac{1}{\psi}} \left[ \frac{J_{t+1}}{\left[ E_t \left( J_{t+1}^{1-\gamma} \right) \right]^{\frac{1}{1-\gamma}}} \right]^{\frac{1}{\psi}-\gamma} \left[ f(\theta_t) \frac{\partial J_{t+1}}{\partial N_{t+1}} + (1-f(\theta_t)) \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] / \phi_{t+1} \right] \\ &= b + E_t \left[ M_{t+1} \left[ f(\theta_t) \frac{\partial J_{t+1}}{\partial N_{t+1}} + (1-f(\theta_t)) \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] / \phi_{t+1} \right].\end{aligned}\quad (\text{S23})$$

## B.2.2 The Representative Firm

We start by reformulating the firm's problem recursively as:

$$S_t = Y_t - W_t N_t - \kappa V_t - I_t + \lambda_t q(\theta_t) V_t + E_t [M_{t+1} S_{t+1}],\quad (\text{S24})$$

subject to  $N_{t+1} = (1-s)N_t + q(\theta_t)V_t$  and  $K_{t+1} = (1-\delta)K_t + \Phi(I_t, K_t)$ .

The first-order condition with respect to  $V_t$  says:

$$\frac{\partial S_t}{\partial V_t} = -\kappa + \lambda_t q(\theta_t) + E_t \left[ M_{t+1} \frac{\partial S_{t+1}}{\partial N_{t+1}} q(\theta_t) \right] = 0.\quad (\text{S25})$$

Equivalently,

$$\frac{\kappa}{q(\theta_t)} - \lambda_t = E_t \left[ M_{t+1} \frac{\partial S_{t+1}}{\partial N_{t+1}} \right]. \quad (\text{S26})$$

In addition, differentiating  $S_t$  with respect to  $N_t$  yields:

$$\frac{\partial S_t}{\partial N_t} = \frac{\partial Y_t}{\partial N_t} - W_t + (1-s)E_t \left[ M_{t+1} \frac{\partial S_{t+1}}{\partial N_{t+1}} \right]. \quad (\text{S27})$$

Combining the last two equations yields the job creation condition.

### B.2.3 The Wage Rate

From equations (S20), (S23), and (S27), the total surplus of the worker-firm relationship is:

$$\begin{aligned} H_t &= W_t + E_t \left[ M_{t+1} \left[ (1-s) \frac{\partial J_{t+1}}{\partial N_{t+1}} + s \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] / \phi_{t+1} \right] - b \\ &\quad - E_t \left[ M_{t+1} \left[ f(\theta_t) \frac{\partial J_{t+1}}{\partial N_{t+1}} + (1-f(\theta_t)) \frac{\partial J_{t+1}}{\partial U_{t+1}} \right] / \phi_{t+1} \right] + \frac{\partial Y_t}{\partial N_t} - W_t + (1-s)E_t \left[ M_{t+1} \frac{\partial S_{t+1}}{\partial N_{t+1}} \right] \\ &= \frac{\partial Y_t}{\partial N_t} - b + (1-s)E_t \left[ M_{t+1} \left[ \left( \frac{\partial J_{t+1}}{\partial N_{t+1}} - \frac{\partial J_{t+1}}{\partial U_{t+1}} \right) / \phi_{t+1} + \frac{\partial S_{t+1}}{\partial N_{t+1}} \right] \right] \\ &\quad - f(\theta_t)E_t \left[ M_{t+1} \left( \frac{\partial J_{t+1}}{\partial N_{t+1}} - \frac{\partial J_{t+1}}{\partial U_{t+1}} \right) / \phi_{t+1} \right] \\ &= \frac{\partial Y_t}{\partial N_t} - b + (1-s-\eta f(\theta_t))E_t [M_{t+1}H_{t+1}]. \end{aligned} \quad (\text{S28})$$

The sharing rule implies  $\partial S_t / \partial N_t = (1-\eta)H_t$ , which, combined with equation (S27), yields:

$$(1-\eta)H_t = \frac{\partial Y_t}{\partial N_t} - W_t + (1-\eta)(1-s)E_t [M_{t+1}H_{t+1}]. \quad (\text{S29})$$

Combining equations (S28) and (S29) yields:

$$\begin{aligned} \frac{\partial Y_t}{\partial N_t} - W_t + (1-\eta)(1-s)E_t [M_{t+1}H_{t+1}] &= (1-\eta) \left( \frac{\partial Y_t}{\partial N_t} - b \right) + (1-\eta)(1-s)E_t [M_{t+1}H_{t+1}] \\ &\quad - (1-\eta)\eta f(\theta_t)E_t [M_{t+1}H_{t+1}] \\ W_t &= \eta \frac{\partial Y_t}{\partial N_t} + (1-\eta)b + (1-\eta)\eta f(\theta_t)E_t [M_{t+1}H_{t+1}]. \end{aligned}$$

Using equations (S14) and (S26) to simplify further:

$$W_t = \eta \frac{\partial Y_t}{\partial N_t} + (1-\eta)b + \eta f(\theta_t)E_t \left[ M_{t+1} \frac{\partial S_{t+1}}{\partial N_{t+1}} \right] \quad (\text{S30})$$

$$W_t = \eta \frac{\partial Y_t}{\partial N_t} + (1-\eta)b + \eta f(\theta_t) \left[ \frac{\kappa}{q(\theta_t)} - \lambda_t \right]. \quad (\text{S31})$$

If  $V_t > 0$ , then  $\lambda_t = 0$ , and equation (S31) reduces to equation (18) because  $f(\theta_t) = \theta_t q(\theta_t)$ . If  $V_t \geq 0$  is binding,  $\lambda_t > 0$ , but  $V_t = 0$  means  $\theta_t = 0$  and  $f(\theta_t) = 0$ . Equation (S31) reduces to  $W_t = \eta \partial Y_t / \partial N_t + (1 - \eta)b$ . Because  $\theta_t = 0$ , equation (18) continues to hold.

## References

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**Table S1 : Basic Properties of Asset Prices in the Historical Sample, with the Longest Possible Sample for Each Moment**

The historical cross-country panel is from the Jordà-Schularick-Taylor macrohistory database, except for Canada's asset prices, which we obtain from the Dimson-Marsh-Staunton (2002) database purchased from Morningstar. All (annual) series end in 2015.  $E[\tilde{r}_S]$ ,  $\tilde{\sigma}_S$ , and  $E[\tilde{r}_S - r_f]$  are the average stock market return, stock market volatility, and the equity premium, respectively, without adjusting for financial leverage.  $E[r_S - r_f]$  and  $\sigma_S$  are the equity premium and stock market volatility, respectively, after adjusting for financial leverage.  $E[r_f]$  is the mean real interest rate, and  $\sigma_f$  the interest rate volatility. All asset pricing moments are in annual percent. We use the longest possible samples of stocks, bills, and bonds described in the second, third, and fourth column, respectively, to calculate each moment. For example, in Australia, the sample for stock market returns starts in 1871, the sample for real interest rates start in 1871, with missing observations from 1945 to 1947, and the sample for long-term government bonds starts in 1900. Other than Italy, which has missing asset prices from 1872 to 1884, all other missing years are in the 20th century.

	Sample, $\tilde{r}_S$	Sample, $r_f$	Sample, $r_B$	$E[\tilde{r}_S]$	$\tilde{\sigma}_S$	$E[r_f]$	$\sigma_f$	$E[\tilde{r}_S - r_f]$	$E[r_S - r_f]$	$\sigma_S$	
∞	Australia	1871	1871 (45–47)	1900	8.39	15.77	2.02	4.44	6.33	4.49	11.76
	Belgium	1871	1871 (15–18)	1871 (14–19)	5.89	21.97	1.68	9.94	5.25	3.73	16.22
	Canada	1900	1900	1900	7.01	17.00	1.60	4.79	5.41	3.84	12.26
	Denmark	1873	1875	1871 (15)	7.54	16.36	2.98	5.77	4.59	3.26	11.88
	Finland	1896	1871	1871	8.83	30.57	0.15	10.50	9.57	6.80	22.98
	France	1871	1871 (15–21)	1871	3.21	22.14	−0.47	7.78	4.45	3.16	16.75
	Germany	1871	1871 (23, 45–49)	1871 (44–48)	9.44	32.04	−0.23	13.17	9.00	6.39	20.15
	Italy	1871	1871 (1872–1884, 15–21)	1871	5.75	26.18	0.58	10.50	6.05	4.29	20.41
	Japan	1886 (46–47)	1876	1881	8.86	27.69	−0.41	12.90	8.87	6.29	21.10
	Netherlands	1900	1871	1871	6.96	21.44	1.37	5.04	6.19	4.39	15.32
	Norway	1881	1871	1871	5.67	19.82	1.10	5.96	4.77	3.39	14.53
	Portugal	1871	1880	1871	4.05	25.20	−0.01	9.43	3.82	2.71	19.29
	Spain	1900	1871 (36–38)	1900 (37–40)	5.77	21.07	0.70	6.83	6.28	4.46	15.88
	Sweden	1871	1871	1871	8.00	19.54	1.77	5.60	6.23	4.42	14.26
	Switzerland	1900	1871	1900 (15)	6.50	19.09	1.64	5.88	5.70	4.05	14.04
	UK	1871	1871	1871	6.86	17.77	1.16	4.82	5.70	4.05	12.96
	USA	1872	1871	1871	8.40	18.68	2.23	4.71	6.23	4.43	13.66
	Mean				6.89	21.90	1.05	7.53	6.14	4.36	16.08
	Median				6.96	21.07	1.16	5.96	6.05	4.29	15.32



**Table S2 : Basic Properties of the Real Consumption, Output, and Investment Growth and Asset Prices, 1950–2015**

The historical cross-country panel is from the Jordà-Schularick-Taylor macrohistory database. The only exception is asset prices data for Canada, which we obtain from the Dimson-Marsh-Staunton (2002) database purchased from Morningstar. All (annual) series end in 2015. In Panel A,  $\bar{g}_C$ ,  $\sigma_C$ ,  $S_C$ ,  $K_C$ , and  $\rho_C^{(i)}$  denote the mean (in percent), volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation, for  $i = 1, 2, \dots, 5$ , of real per capita consumption growth. In Panel B,  $\bar{g}_Y$ ,  $\sigma_Y$ ,  $S_Y$ ,  $K_Y$ , and  $\rho_Y^{(i)}$  denote the mean (in percent), volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation for real per capita output growth. In Panel C,  $\bar{g}_I$ ,  $\sigma_I$ ,  $S_I$ ,  $K_I$ , and  $\rho_I^{(i)}$  denote the mean (in percent), volatility (in percent), skewness, kurtosis, and  $i$ th-order autocorrelation for real per capita investment growth. Finally, in Panel D,  $E[\tilde{r}_S]$ ,  $\tilde{\sigma}_S$ , and  $E[\tilde{r}_S - r_f]$  are the average stock market return, stock market volatility, and the equity premium, respectively, without adjusting for financial leverage.  $E[r_S - r_f]$  and  $\sigma_S$  are the equity premium and stock market volatility, respectively, after adjusting for financial leverage.  $E[r^f]$  is the mean real interest rate, and  $\sigma_f$  the interest rate volatility. All asset pricing moments are in annual percent.

	Panel A: Real consumption growth									Panel B: Real output growth								
	$\bar{g}_C$	$\sigma_C$	$S_C$	$K_C$	$\rho_C^{(1)}$	$\rho_C^{(2)}$	$\rho_C^{(3)}$	$\rho_C^{(4)}$	$\rho_C^{(5)}$	$\bar{g}_Y$	$\sigma_Y$	$S_Y$	$K_Y$	$\rho_Y^{(1)}$	$\rho_Y^{(2)}$	$\rho_Y^{(3)}$	$\rho_Y^{(4)}$	$\rho_Y^{(5)}$
Australia	1.78	2.02	-0.14	3.55	0.17	-0.24	-0.11	0.19	0.30	1.95	1.86	-0.56	4.19	0.19	-0.03	-0.07	0.09	0.24
Belgium	1.89	1.92	0.20	3.42	0.34	0.21	0.41	0.18	0.21	2.22	2.01	-0.28	2.95	0.28	0.27	0.20	0.23	0.05
Canada	2.01	1.81	-0.61	4.00	0.31	0.07	0.17	-0.07	-0.26	1.94	2.25	-0.73	3.73	0.25	-0.04	0.05	0.05	-0.01
Denmark	1.24	2.43	-0.03	2.95	0.22	0.01	0.03	-0.17	-0.30	1.85	2.33	-0.05	3.88	0.26	0.09	0.16	0.16	0.09
Finland	2.62	3.17	-0.40	3.04	0.40	-0.08	-0.05	-0.05	-0.03	2.54	3.24	-0.93	5.23	0.42	0.01	0.08	0.02	0.03
France	2.34	1.79	0.19	2.18	0.65	0.48	0.40	0.42	0.41	2.37	1.87	-0.27	3.35	0.56	0.41	0.47	0.44	0.40
Germany	2.81	2.46	0.71	2.98	0.73	0.53	0.50	0.51	0.49	2.80	2.69	0.18	3.93	0.48	0.17	0.31	0.48	0.36
Italy	2.51	2.72	-0.30	2.97	0.67	0.46	0.52	0.48	0.41	2.69	2.71	-0.79	3.56	0.51	0.35	0.42	0.39	0.39
Japan	3.90	3.53	0.72	3.00	0.74	0.62	0.69	0.66	0.61	3.80	3.69	0.26	2.72	0.69	0.59	0.61	0.53	0.48
Netherlands	1.92	2.47	-0.16	2.45	0.67	0.32	0.15	0.08	0.13	2.22	2.20	-0.12	3.78	0.39	0.05	0.05	0.13	0.12
Norway	2.39	2.19	0.21	3.76	0.23	-0.02	-0.18	-0.14	-0.13	2.53	1.87	-0.52	2.73	0.51	0.28	0.16	0.20	0.19
Portugal	3.05	3.56	-0.58	4.03	0.36	0.16	0.08	-0.14	-0.18	2.93	3.48	-0.34	3.87	0.51	0.23	0.26	-0.01	0.02
Spain	2.79	3.54	0.08	3.20	0.51	0.25	0.20	0.23	0.23	3.15	3.21	0.07	2.62	0.50	0.32	0.23	0.22	0.14
Sweden	1.55	1.92	-0.59	3.12	0.38	0.18	0.08	-0.09	-0.16	2.09	2.14	-1.13	5.31	0.32	-0.02	0.03	0.12	0.15
Switzerland	1.44	1.42	0.11	2.59	0.61	0.24	0.14	0.10	0.11	1.62	2.29	-0.65	4.06	0.30	-0.04	-0.03	0.08	0.02
UK	1.97	2.09	-0.13	3.11	0.45	0.05	-0.11	-0.11	0.00	1.88	1.90	-0.85	4.89	0.33	-0.13	-0.12	-0.01	0.02
USA	2.08	1.73	-0.21	2.49	0.32	0.03	-0.06	0.02	-0.04	1.91	2.21	-0.43	2.88	0.12	-0.01	-0.15	0.06	-0.07
Mean	2.25	2.40	-0.05	3.11	0.46	0.19	0.17	0.12	0.11	2.38	2.47	-0.42	3.75	0.39	0.15	0.16	0.19	0.15
Median	2.08	2.19	-0.13	3.04	0.40	0.18	0.14	0.08	0.11	2.22	2.25	-0.43	3.78	0.39	0.09	0.16	0.13	0.12

Panel C: Real investment growth											Panel D: Asset prices					
	$\bar{y}_I$	$\sigma_I$	$S_I$	$K_I$	$\rho_I^{(1)}$	$\rho_I^{(2)}$	$\rho_I^{(3)}$	$\rho_I^{(4)}$	$\rho_I^{(5)}$	$E[\tilde{r}_S]$	$\tilde{\sigma}_S$	$E[r_f]$	$\sigma_f$	$E[\tilde{r}_S - r_f]$	$E[r_S - r_f]$	$\sigma_S$
Australia	2.33	5.70	-0.45	2.82	0.09	-0.29	-0.08	0.16	0.07	7.33	20.46	1.44	3.97	5.89	4.18	14.90
Belgium	2.63	7.08	-0.73	3.95	0.05	-0.13	-0.09	-0.01	-0.16	8.07	21.05	1.60	2.91	6.47	4.59	15.02
Canada	2.10	5.65	-0.46	3.15	0.23	0.02	-0.21	-0.20	-0.28	7.47	16.33	1.80	3.12	5.66	4.02	11.51
Denmark	1.32	9.06	-1.34	6.86	0.24	0.07	0.06	-0.13	-0.19	9.60	21.37	2.24	2.85	7.36	5.22	15.19
Finland	2.41	9.01	-0.66	4.25	0.49	0.04	-0.19	-0.20	-0.09	12.17	33.86	0.76	4.50	11.41	8.10	24.47
France	1.86	6.18	-2.56	14.73	0.14	-0.03	-0.18	-0.13	-0.19	6.45	26.13	1.08	3.29	5.38	3.82	18.71
Germany	2.60	6.41	0.28	3.78	0.39	-0.06	-0.08	-0.02	0.03	12.09	27.71	1.72	1.78	10.37	7.36	19.62
Italy	2.37	5.53	-0.63	3.12	0.41	0.11	0.18	0.22	0.10	6.02	25.99	1.23	3.09	4.79	3.40	18.69
Japan	4.11	7.86	0.56	2.84	0.52	0.19	0.30	0.30	0.28	9.58	22.37	1.21	3.40	8.37	5.94	16.04
Netherlands	2.21	6.11	0.10	3.42	0.24	0.00	-0.07	-0.11	-0.27	9.43	21.81	1.15	2.83	8.28	5.88	15.58
Norway	2.18	8.58	0.29	4.50	0.13	-0.14	-0.03	-0.10	-0.22	7.25	25.99	-0.21	3.26	7.46	5.30	18.69
Portugal	2.64	9.58	-0.22	3.08	0.22	0.21	0.06	-0.13	0.08	4.86	33.53	-0.73	4.85	5.59	3.97	24.38
Spain	3.60	9.32	-0.20	3.40	0.45	0.30	-0.07	-0.12	-0.27	7.93	24.53	-0.22	4.43	8.15	5.79	17.91
Sweden	2.49	5.32	-1.41	5.32	0.28	-0.09	-0.13	-0.08	0.03	11.14	24.01	0.82	2.58	10.32	7.33	17.23
Switzerland	2.25	7.93	0.46	5.96	0.35	0.03	-0.04	-0.21	-0.24	8.33	21.41	0.06	2.13	8.27	5.87	15.33
UK	2.61	5.75	-0.76	4.16	0.38	0.02	-0.03	0.02	0.05	9.13	22.94	1.21	3.63	7.92	5.62	16.27
USA	1.91	4.98	-0.89	4.45	0.27	-0.12	-0.27	-0.21	-0.08	8.56	16.83	1.41	2.25	7.15	5.08	12.03
Mean	2.45	7.06	-0.51	4.69	0.29	0.01	-0.05	-0.06	-0.08	8.55	23.90	0.97	3.23	7.58	5.38	17.15
Median	2.37	6.41	-0.46	3.95	0.27	0.02	-0.07	-0.11	-0.09	8.33	22.94	1.21	3.12	7.46	5.30	16.27

**Table S3 : Gollin’s (2002) Labor Share Calculations**

For the 12 countries that are in both Gollin (2002) and Jordà-Schularick-Taylor macrohistory database, this table reports the labor shares reported in Gollin’s Table 2. The three columns correspond to the last three columns labeled “Adjustment 1,” “Adjustment 2,” and “Adjustment 3,” respectively, in Gollin’s table.

	Method 1	Method 2	Method 3
Australia	0.719	0.669	0.676
Belgium	0.791	0.743	0.740
Finland	0.765	0.734	0.680
France	0.764	0.717	0.681
Italy	0.804	0.717	0.707
Japan	0.727	0.692	0.725
Netherlands	0.721	0.680	0.643
Norway	0.678	0.643	0.569
Portugal	0.825	0.748	0.602
Sweden	0.800	0.774	0.723
UK	0.815	0.782	0.719
US	0.773	0.743	0.664
Mean	0.765	0.720	0.677
Median	0.769	0.726	0.681

Table S4 : Dividend Dynamics in the Historical and Post-1950 Samples

Real output is from the Jordà-Schularick-Taylor macrohistory database. Appendix A describes our construction of dividends from their database. We use two detrending methods for real dividends and output. “Prop. dev.” means the HP-filtered proportional deviations from the mean, and “Log dev.” means log deviations from the HP-trend.  $\rho_{DY}$  is the correlation between the cyclical components of dividends and output, and  $\sigma_D/\sigma_Y$  the volatility of the cyclical component of dividends divided by that of output. We examine three frequencies, annual, 3-year, and 5-year. For the 3-year frequency, we sum up the three annual observations within a given 3-year interval. The 3-year intervals are nonoverlapping. The 5-year series are constructed analogously. The HP smoothing parameters for the 1-, 3-, and 5-year series are  $1600/4^4 = 6.25$ ,  $1600/12^4 = 0.077$ , and  $1600/20^4 = 0.01$ , respectively, all of which correspond to 1,600 in the quarterly frequency. In Panel A, the column “Sample” indicates the starting year of a country. For Japan, the annual observations from 1946 and 1947 are missing. In Panel B, all countries start their samples in 1950, except for Switzerland, which starts in 1960. In calculating log deviations, the zero-dividend observations are removed.

		Panel A: The historical sample											
		1-year frequency		3-year frequency		5-year frequency							
Sample		$\rho_{DY}$	$\sigma_D/\sigma_Y$	Log dev.	$\rho_{DY}$	$\sigma_D/\sigma_Y$	Log dev.	$\rho_{DY}$	$\sigma_D/\sigma_Y$	Log dev.			
Australia	1870	0.109	6.943	0.121	3.430	0.231	5.144	0.295	2.565	0.551	4.596	0.633	2.593
Belgium	1870	0.183	8.501	0.498	4.706	0.419	9.797	0.825	5.718	0.765	5.622	0.923	2.830
Denmark	1872	0.191	14.885	0.182	6.836	0.263	12.065	0.226	6.513	0.027	10.580	0.092	6.031
Finland	1912	0.083	10.143	0.308	6.883	0.670	8.464	0.504	5.754	0.815	4.225	0.437	5.477
France	1870	0.169	5.590	0.119	2.658	0.234	5.311	-0.029	3.564	0.479	4.443	-0.204	3.234
Germany	1870	0.018	6.052	0.211	20.321	0.114	3.821	0.552	2.924	0.241	1.952	0.894	3.652
Italy	1870	0.035	5.097	0.396	6.373	0.262	5.925	0.847	10.566	0.571	5.603	0.764	7.340
Japan	1886 (46-47)	0.027	10.673	0.612	8.949	0.058	6.347	0.806	10.513	0.110	7.107	0.882	7.470
Netherlands	1950	-0.001	16.807	0.203	14.904	0.548	13.768	0.390	13.042	0.369	18.404	0.258	13.533
Norway	1880	0.216	10.520	0.214	8.517	0.348	5.638	0.440	6.574	0.342	5.413	0.656	5.580
Portugal	1870	-0.021	3.062	0.007	7.762	0.043	1.572	0.597	12.343	0.108	1.570	0.454	14.630
Spain	1899	0.035	11.598	0.269	8.865	0.176	6.008	0.562	11.541	0.266	4.142	0.625	5.039
Sweden	1871	-0.019	9.309	0.152	5.664	0.091	5.756	0.440	5.112	0.565	4.616	0.701	5.631
Switzerland	1960	0.026	11.061	0.051	13.165	0.429	8.658	0.342	7.725	0.034	7.987	0.014	9.190
UK	1871	0.272	4.314	0.094	5.072	0.570	3.001	0.399	2.788	0.114	2.735	0.044	2.538
USA	1871	0.472	3.176	0.415	2.626	0.527	3.367	0.419	2.682	0.307	2.099	0.458	2.118
Mean		0.112	8.608	0.241	7.921	0.312	6.540	0.476	6.870	0.354	5.693	0.477	6.055
Median		0.059	8.905	0.207	6.860	0.262	5.840	0.440	6.133	0.325	4.606	0.542	5.529

Panel B: The post-1950 sample

	1-year frequency			3-year frequency			5-year frequency					
	Prop. dev.	$\sigma_D/\sigma_Y$	Log dev.	Prop. dev.	$\sigma_D/\sigma_Y$	Log dev.	Prop. dev.	$\sigma_D/\sigma_Y$	Log dev.			
Australia	0.166	10.847	0.206	9.315	0.220	10.371	0.217	8.048	0.667	6.390	0.732	4.997
Belgium	-0.037	15.171	-0.020	11.548	-0.064	13.081	0.000	9.053	0.263	11.680	0.368	9.798
Denmark	0.200	37.696	0.127	15.578	0.336	29.277	0.351	14.641	0.369	14.957	0.406	8.189
Finland	0.054	12.063	0.182	11.121	0.573	8.375	0.874	9.303	0.795	5.395	0.712	7.865
France	-0.113	9.507	-0.060	10.510	0.082	9.709	0.105	9.099	0.096	5.515	0.277	5.893
Germany	-0.232	10.350	0.059	10.676	0.126	9.745	0.257	12.919	-0.326	12.597	0.338	11.169
Italy	0.019	8.131	-0.058	10.659	-0.009	11.848	0.157	11.149	0.268	10.223	0.362	14.628
Japan	0.287	4.826	0.393	5.584	0.198	5.750	0.192	4.645	0.489	4.724	0.556	4.506
Netherlands	-0.001	16.807	0.203	14.904	0.548	13.768	0.390	13.042	0.369	18.404	0.258	13.533
Norway	0.188	33.166	0.076	23.009	0.085	19.021	0.070	16.454	0.574	4.214	0.287	6.402
Portugal	-0.243	6.067	0.073	16.699	0.156	5.767	0.720	26.052	0.510	2.865	0.812	20.826
Spain	-0.052	16.567	0.027	12.367	0.044	6.939	0.055	5.929	0.196	5.250	0.109	4.727
Sweden	-0.033	11.772	0.182	8.797	0.615	9.721	0.816	9.321	0.436	3.884	0.513	5.503
Switzerland	0.026	11.061	0.051	13.165	0.429	8.658	0.342	7.725	0.034	7.987	0.014	9.190
UK	0.634	3.837	0.639	3.695	0.734	4.251	0.735	4.165	0.411	3.593	0.482	3.336
USA	0.645	3.801	0.497	2.962	0.710	4.377	0.646	3.508	0.371	3.302	0.506	2.671
Mean	0.094	13.229	0.161	11.287	0.299	10.666	0.370	10.316	0.345	7.561	0.421	8.327
Median	0.022	10.954	0.101	10.898	0.209	9.715	0.299	9.201	0.370	5.455	0.387	7.134

**Table S5 : Predicting Excess Returns and Consumption Growth with Log Price-to-consumption in the post-1950 Sample**

The historical cross-country panel is from the Jordà-Schularick-Taylor macrohistory database, except for Canada. The annuals series start in 1950 and end in 2015. Panel A performs predictive regressions of stock market excess returns on log price-to-consumption,  $\sum_{h=1}^H [\log(r_{St+h}) - \log(r_{ft+h})] = a + b \log(P_t/C_t) + u_{t+h}$ , in which  $H$  is the forecast horizon,  $r_{St+1}$  real stock market return,  $r_{ft+1}$  real interest rate,  $P_t$  real market index, and  $C_t$  real consumption.  $r_{St+1}$  and  $r_{ft+1}$  are over the course of period  $t$ , and  $P_t$  and  $C_t$  are at the beginning of  $t$ . Excess returns are adjusted for a financial leverage ratio of 0.29. Panel B performs long-horizon predictive regressions of log consumption growth on  $\log(P_t/C_t)$ ,  $\sum_{h=1}^H \log(C_{t+h}/C_t) = c + d \log(P_t/C_t) + v_{t+h}$ . In both regressions,  $\log(P_t/C_t)$  is standardized to have a mean of zero and a standard deviation of one.  $H$  ranges from one year (1y) to five years (5y). The  $t$ -values of the slopes are adjusted for heteroscedasticity and autocorrelations of  $2(H - 1)$  lags. The slopes and  $R$ -squares are in percent.

	Slopes					$t$ -values of slopes					$R$ -squares				
	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y
Panel A: Predicting stock market excess returns															
Australia	-4.79	-7.74	-8.35	-9.52	-9.70	-3.03	-4.13	-4.19	-3.06	-2.46	12.17	19.86	21.17	22.51	21.26
Belgium	-2.39	-5.00	-6.91	-9.44	-10.86	-1.45	-1.57	-1.61	-1.89	-2.39	2.46	5.64	8.16	11.80	15.00
Denmark	-0.43	-1.76	-2.32	-3.05	-3.08	-0.17	-0.41	-0.46	-0.67	-0.76	0.08	0.61	0.79	1.13	1.13
Finland	-3.76	-9.48	-14.03	-17.33	-19.08	-1.36	-2.46	-4.08	-5.30	-5.33	3.68	9.66	14.50	18.23	20.25
France	-1.85	-4.05	-5.95	-8.59	-11.47	-0.97	-1.17	-1.09	-1.21	-1.48	1.26	3.10	4.85	7.24	11.90
Germany	-6.24	-11.41	-14.93	-18.14	-19.06	-2.78	-3.21	-3.15	-3.20	-3.40	12.48	20.22	24.99	29.08	29.57
Italy	-0.98	-2.51	-4.20	-5.61	-6.34	-0.52	-0.63	-0.77	-0.80	-0.76	0.32	0.93	1.76	2.40	2.76
Japan	-4.00	-9.60	-13.90	-17.98	-21.83	-2.30	-2.96	-4.35	-5.80	-5.96	8.19	18.14	25.40	31.70	36.39
Netherlands	-3.04	-6.48	-8.91	-11.12	-13.51	-1.68	-1.87	-2.09	-2.46	-3.06	4.13	8.98	12.71	16.31	20.65
Norway	-3.89	-7.14	-8.74	-9.80	-11.69	-1.99	-2.68	-2.70	-2.59	-2.87	4.99	9.69	12.52	14.56	18.57
Portugal	-2.16	-8.22	-14.17	-17.85	-17.39	-0.48	-0.94	-1.30	-1.51	-1.66	0.77	3.93	6.64	7.60	5.75
Spain	-0.32	-2.18	-4.83	-7.32	-9.22	-0.17	-0.54	-0.86	-1.17	-1.32	0.04	0.78	2.22	3.64	4.76
Sweden	-1.57	-3.12	-4.06	-5.13	-6.09	-0.75	-0.84	-0.91	-1.10	-1.24	0.95	1.88	2.46	3.28	4.10
Switzerland	-3.09	-6.51	-8.50	-10.67	-12.95	-1.70	-2.30	-2.85	-3.89	-4.17	4.02	8.50	11.76	15.72	20.05
UK	-6.50	-11.41	-13.92	-14.44	-16.54	-3.01	-4.32	-4.54	-5.95	-6.68	17.37	30.67	38.71	42.28	49.39
USA	-2.89	-5.59	-7.18	-9.65	-12.36	-2.18	-2.27	-2.24	-2.47	-2.79	5.83	10.67	13.61	18.59	23.90
Mean	-2.99	-6.39	-8.81	-10.98	-12.57	-1.53	-2.02	-2.32	-2.69	-2.90	4.92	9.58	12.64	15.38	17.84
Median	-2.96	-6.49	-8.42	-9.73	-12.02	-1.56	-2.07	-2.16	-2.47	-2.63	3.85	8.74	12.14	15.14	19.31
Panel B: Predicting consumption growth															
Australia	0.40	0.41	0.36	0.81	1.20	1.79	0.93	0.58	1.35	1.85	4.04	1.78	1.08	5.54	10.21
Belgium	0.09	0.09	0.21	0.41	0.54	0.42	0.25	0.43	0.68	0.76	0.24	0.09	0.27	0.62	0.78
Denmark	-0.08	-0.42	-0.69	-1.05	-1.38	-0.27	-0.55	-0.61	-0.79	-0.94	0.10	1.04	1.61	2.57	3.51
Finland	0.31	0.06	-0.40	-0.73	-0.90	0.95	0.08	-0.39	-0.63	-0.72	0.97	0.01	0.37	0.89	1.10
France	0.95	1.81	2.68	3.51	4.37	4.45	3.67	3.84	4.18	4.69	28.51	32.88	37.06	40.26	43.62
Germany	-0.10	-0.47	-1.05	-1.43	-1.84	-0.29	-0.51	-0.69	-0.72	-0.73	0.15	1.07	2.65	3.20	3.74
Italy	1.58	3.04	4.43	5.68	6.84	5.69	4.47	4.07	3.74	3.51	33.87	37.49	40.15	40.67	40.62
Japan	0.51	0.86	1.44	1.86	2.17	1.48	0.89	0.90	0.80	0.71	2.12	1.79	2.65	2.63	2.30
Netherlands	0.67	1.12	1.46	1.87	2.35	2.43	1.49	1.24	1.17	1.14	7.43	6.49	5.94	6.42	7.60
Norway	0.23	0.38	0.56	0.73	1.00	0.78	0.65	0.77	0.95	1.29	1.16	1.26	1.78	2.36	3.78
Portugal	0.19	0.05	0.13	0.62	1.54	0.36	0.04	0.08	0.38	0.98	0.26	0.01	0.03	0.53	2.66
Spain	1.75	3.04	4.02	4.90	5.62	4.78	3.94	3.36	2.99	2.72	24.75	26.39	25.77	24.87	23.66
Sweden	0.00	-0.22	-0.39	-0.56	-0.74	-0.01	-0.44	-0.46	-0.48	-0.53	0.00	0.45	0.74	1.01	1.30
Switzerland	0.22	0.31	0.36	0.35	0.34	1.32	0.84	0.61	0.43	0.33	2.52	1.40	1.00	0.64	0.44
UK	0.45	0.46	0.45	0.23	-0.12	2.14	1.14	0.80	0.30	-0.13	4.78	1.73	0.99	0.19	0.04
USA	0.28	0.16	0.11	0.19	0.22	1.34	0.31	0.15	0.20	0.20	2.69	0.30	0.09	0.19	0.20
Mean	0.47	0.67	0.86	1.09	1.33	1.71	1.07	0.92	0.91	0.95	7.10	7.14	7.64	8.29	9.10
Median	0.30	0.34	0.36	0.51	0.77	1.33	0.74	0.59	0.56	0.73	2.32	1.33	1.35	2.46	3.08

**Table S6 : Predicting Volatilities of Stock Market Excess Returns and Consumption Growth with Log Price-to-consumption in the Post-1950 Sample**

The historical cross-country panel is from the Jordà-Schularick-Taylor macrohistory database, except for Canada. The annuals series start in 1950 and end in 2015. For a given horizon,  $H$ , we measure excess return volatility as  $\sigma_{St,t+H-1} = \sum_{h=0}^{H-1} |\epsilon_{St+h}|$ , in which  $\epsilon_{St+h}$  is the  $h$ -period-ahead residual from the first-order autoregression of excess returns,  $\log(r_{St+1}) - \log(r_{ft+1})$  (adjusted for a financial leverage ratio of 0.29). Panel A performs long-horizon predictive regressions of excess return volatilities,  $\log \sigma_{St+1,t+H} = a + b \log(P_t/C_t) + u_{t+H}^\sigma$ . For a given  $H$ , consumption growth volatility is  $\sigma_{Ct,t+H-1} = \sum_{h=0}^{H-1} |\epsilon_{Ct+h}|$ , in which  $\epsilon_{Ct+h}$  is the  $h$ -period-ahead residual from the first-order autoregression of log consumption growth,  $\log(C_{t+1}/C_t)$ . Panel B performs long-horizon predictive regressions of consumption growth volatilities,  $\log \sigma_{Ct+1,t+H} = c + d \log(P_t/C_t) + v_{t+H}^\sigma$ .  $\log(P_t/C_t)$  is standardized to have a mean of zero and a standard deviation of one.  $H$  ranges from one year (1y) to five years (5y). The  $t$ -values are adjusted for heteroscedasticity and autocorrelations of  $2(H-1)$  lags. The slopes and  $R$ -squares are in percent.

	Slopes					$t$ -values of slopes					$R$ -squares				
	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y	1y	2y	3y	4y	5y
Panel A: Predicting stock market volatility															
Australia	1.71	6.76	3.98	4.74	2.83	0.11	0.55	0.31	0.36	0.21	0.01	0.59	0.36	0.62	0.27
Belgium	1.96	2.38	1.97	1.08	-0.63	0.20	0.32	0.28	0.15	-0.10	0.04	0.17	0.19	0.08	0.03
Denmark	13.67	11.12	11.79	11.24	10.74	1.14	0.91	0.82	0.73	0.66	1.95	2.30	3.25	3.28	3.18
Finland	19.65	14.49	14.23	11.41	8.21	1.48	1.48	1.85	2.04	1.72	2.78	5.01	6.96	5.39	3.28
France	-9.75	-10.93	-9.49	-10.00	-10.89	-0.74	-1.43	-1.64	-2.47	-3.97	0.97	3.74	6.17	10.88	16.47
Germany	17.77	15.12	15.12	15.11	13.28	1.07	1.76	1.92	1.93	1.74	1.56	5.04	10.80	16.58	16.29
Italy	-33.16	-28.63	-23.29	-19.12	-18.45	-1.75	-2.07	-2.52	-2.80	-3.46	4.55	10.16	15.51	20.36	27.24
Japan	6.13	12.73	12.65	11.56	10.48	0.41	1.24	1.25	1.22	1.16	0.33	4.57	6.30	6.41	6.37
Netherlands	6.06	8.47	11.33	11.06	8.98	0.42	0.67	1.04	1.20	1.16	0.32	1.44	4.74	5.73	5.26
Norway	-34.27	-29.37	-25.24	-25.28	-26.05	-2.43	-4.10	-3.70	-3.45	-3.36	3.56	12.38	22.44	28.85	35.65
Portugal	-42.17	-42.76	-43.85	-46.49	-46.10	-2.14	-2.42	-2.93	-3.25	-2.89	11.85	22.46	28.69	34.92	31.02
Spain	-18.04	-22.59	-19.14	-18.62	-17.79	-1.41	-2.40	-2.09	-2.05	-1.94	2.42	9.73	11.80	15.50	17.10
Sweden	15.21	17.32	19.29	18.48	19.27	1.48	1.88	2.37	2.46	2.73	3.54	9.61	19.61	22.61	28.04
Switzerland	7.05	11.57	9.51	11.11	11.03	0.39	0.87	0.90	1.18	1.30	0.27	2.01	3.01	5.79	7.64
UK	1.05	6.22	11.23	14.44	16.17	0.07	0.56	1.26	2.11	2.62	0.01	0.88	3.89	7.43	11.03
USA	12.24	10.13	11.34	12.42	13.72	0.83	1.17	1.93	2.60	3.07	1.42	2.42	5.21	9.98	17.62
Mean	-2.18	-1.12	0.09	0.20	-0.32	-0.06	-0.06	0.07	0.12	0.04	2.23	5.78	9.31	12.15	14.16
Median	4.01	7.62	10.37	11.08	8.59	0.30	0.62	0.86	0.95	0.91	1.49	4.15	6.23	8.71	13.66
Panel B: Predicting consumption growth volatility															
Australia	-4.80	12.99	14.07	13.44	12.20	-0.20	1.60	1.88	2.03	2.09	0.17	4.54	8.03	9.83	9.27
Belgium	-4.34	0.39	5.59	10.58	12.26	-0.33	0.04	0.65	1.26	1.63	0.24	0.00	1.16	5.51	8.86
Denmark	-23.77	-22.00	-16.49	-14.52	-15.41	-1.83	-2.23	-1.65	-1.55	-1.85	3.69	7.15	5.85	6.89	12.03
Finland	-25.16	-14.09	-8.95	-5.96	-5.41	-1.84	-1.03	-0.63	-0.42	-0.40	4.60	3.10	1.74	0.91	0.89
France	16.54	17.63	16.51	16.50	16.37	1.28	1.95	2.11	2.74	3.44	2.07	6.56	9.91	13.57	18.08
Germany	-6.27	-1.99	-0.64	1.33	4.44	-0.47	-0.18	-0.07	0.17	0.57	0.21	0.07	0.01	0.07	1.11
Italy	8.31	5.18	5.95	7.19	9.02	0.73	0.56	0.65	0.93	1.56	0.73	0.79	1.33	2.60	5.04
Japan	1.35	-8.36	-6.69	-7.02	-8.53	0.06	-0.67	-0.55	-0.59	-0.73	0.01	1.09	1.05	1.36	2.26
Netherlands	6.40	9.28	11.58	11.02	10.08	0.54	0.80	0.96	1.02	1.05	0.42	2.10	4.59	5.09	5.23
Norway	-22.89	-23.25	-24.00	-21.67	-19.13	-1.86	-1.76	-2.01	-2.28	-2.66	3.70	8.06	11.96	12.72	12.60
Portugal	-18.51	-12.71	-10.28	-9.25	-9.76	-2.00	-1.38	-1.02	-0.82	-0.77	5.10	3.87	3.57	3.38	3.57
Spain	41.05	34.10	31.91	30.02	29.87	2.88	2.55	2.50	2.32	2.22	11.21	14.65	18.82	23.51	28.32
Sweden	-12.16	-20.44	-17.17	-13.44	-12.42	-0.78	-1.43	-1.41	-1.44	-1.60	0.91	6.08	6.43	5.21	6.27
Switzerland	-13.49	-13.67	-13.37	-9.64	-6.97	-1.01	-1.06	-1.11	-0.84	-0.69	1.40	2.71	3.78	2.63	1.61
UK	-24.73	-16.02	-16.09	-16.80	-16.53	-1.91	-1.85	-2.24	-2.79	-2.77	3.67	4.52	7.87	11.74	14.83
USA	-4.93	-13.20	-10.05	-10.31	-10.96	-0.31	-1.14	-0.98	-1.02	-1.07	0.12	2.32	2.44	3.14	4.42
Mean	-5.46	-4.14	-2.38	-1.16	-0.68	-0.44	-0.33	-0.18	-0.08	0.00	2.39	4.23	5.53	6.76	8.40
Median	-5.60	-10.54	-7.82	-6.49	-6.19	-0.40	-0.85	-0.59	-0.50	-0.55	1.16	3.48	4.19	5.15	5.75